

---

# Introduction to FETToy Simulator

James K Fodor  
University of Florida  
ECE Graduate Student

# Introduction to FETToy

---

## Description of the FETToy Simulator

- Computes ballistic I-V characteristics for:
  - Conventional MOSFETs – single or double gate
  - Nanowire MOSFETs – cylindrical geometry
  - Carbon Nanotube (CNT) MOSFETS – cylindrical geometry

A. Rahman, J. Guo, S. Datta, and M. Lundstrom, “Theory of Ballistic Nanotransistors,” IEEE Trans. on Electron Devices, 50, p. 1853, 2003

# Introduction to FETToy

---

## Description of the FETToy Examples

- Example 1: Role of Gate Oxide Thickness on MOSFET characteristics
- Example 2: Role of Carrier Effective Mass on MOSFET characteristics
- Example 3: New Channel Materials
- Example 4: Two-dimensional Electrostatics
- Example 5: Compare p-type and n-type MOSFETs
- Example 6: Figures of Merit for MOSFETs
- Example 7: Figures of Merit for Nanowire MOSFETs

# Problem 1

---

*Traditional MOSFET models tell us that  $ID \propto Cox$ , so reducing the oxide thickness by a factor of two doubles the current. Let's see what happens for nanotransistors.*

1) Explore the role of gate oxide thickness on the on-current of a ballistic silicon MOSFET. For these calculations, you should use **1D electrostatics** (gate control parameter = 1 and drain control parameter = 0) and vary the oxide thickness from **10nm** to the unphysically small value of **0.01nm**. Assume  $VDD = 1V$  and room temperature operation.

1a) Produce a plot of the on-current (the current for  $VG = VD = VDD$ ) vs. oxide thickness. Compare the computed results to the result expected from conventional MOSFET theory ( $ID \sim COX$ ) by appropriately plotting the actual result and the trend expected from traditional theory.

1b) Provide a physical explanation for the shape of your plot. The characteristic should change when the oxide thickness is smaller than a certain value. Can you give a simple equation to estimate that value? (HINT: It is the gate capacitance that matters. The oxide capacitance is in series with a semiconductor or "quantum" capacitance)

Acknowledgement: The problem is provided by Prof. Mark Lundstrom, Purdue University

# 1a) Conventional Plot: $I_{ON}$ vs. $T_{OX}$

## Common Material Parameters and Settings:

$T_{OX} = 10\text{nm}$

$I_{D0} = ?$

Device | Models | Environment

Model: MOSFET

Single Gate/Double Gate: Single Gate

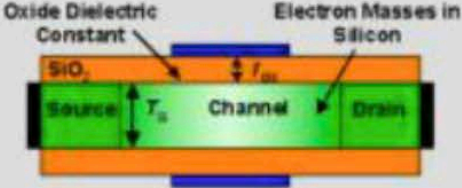
Transport Effective Mass: 0.19

Valley Degeneracy: 2

Floating Boundary Flag: no

Body Thickness: 10nm

Source Doping Density:  $1.0e29/\text{cm}^3$



Oxide Dielectric Constant:  $\text{SiO}_2$

Electron Masses in Silicon

Source Channel Drain

$T_{ox}$

Refresh Screen CopyPaste with Desktop

Device | Models | Environment

Gate Insulator Thickness: 10nm

Insulator Dielectric Constant: 3.9

Threshold Voltage: 0.32V

Gate Control Parameter: 1

Drain Control Parameter: 0

Series Resistance (ohm-cm): 0

Refresh Screen CopyPaste with Desktop

Device | Models | Environment

Ambient Temperature: 300K

Initial Gate Voltage: 0V

Final Gate Voltage: 2V

Number of Gate Voltage Bias Points: 13

Initial Drain Voltage: 0V

Final Drain Voltage: 1V

Number of Drain Voltage Bias Points: 30

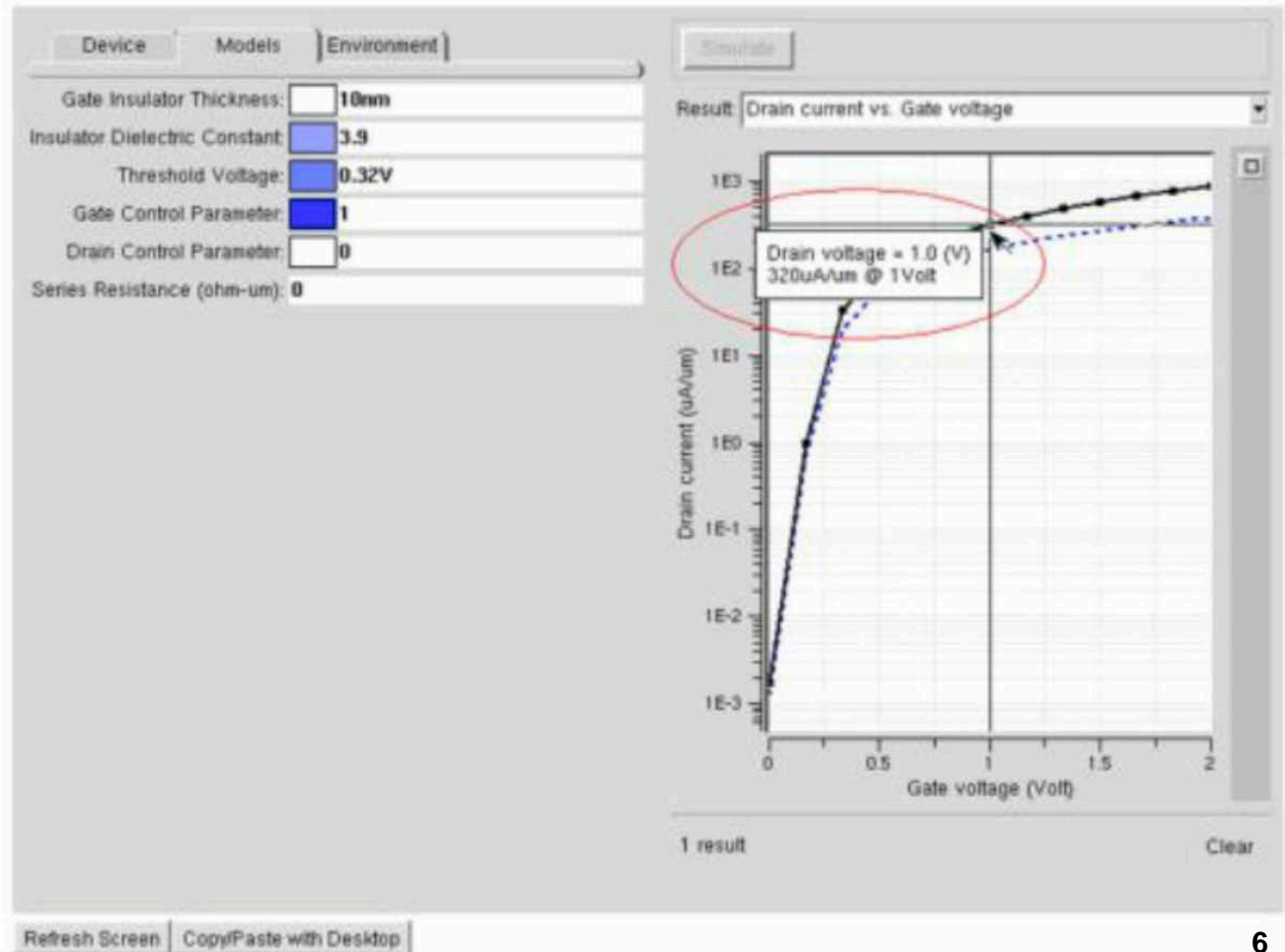
Refresh Screen CopyPaste with Desktop

# 1a) Conventional Plot: $I_{ON}$ vs. $T_{OX}$

Result for ID0:

$T_{OX} = 10\text{nm}$

$I_{D0} = 320\mu\text{A}/\mu\text{m}$



# 1a) Conventional Plot: $I_{ON}$ vs. $T_{OX}$

---

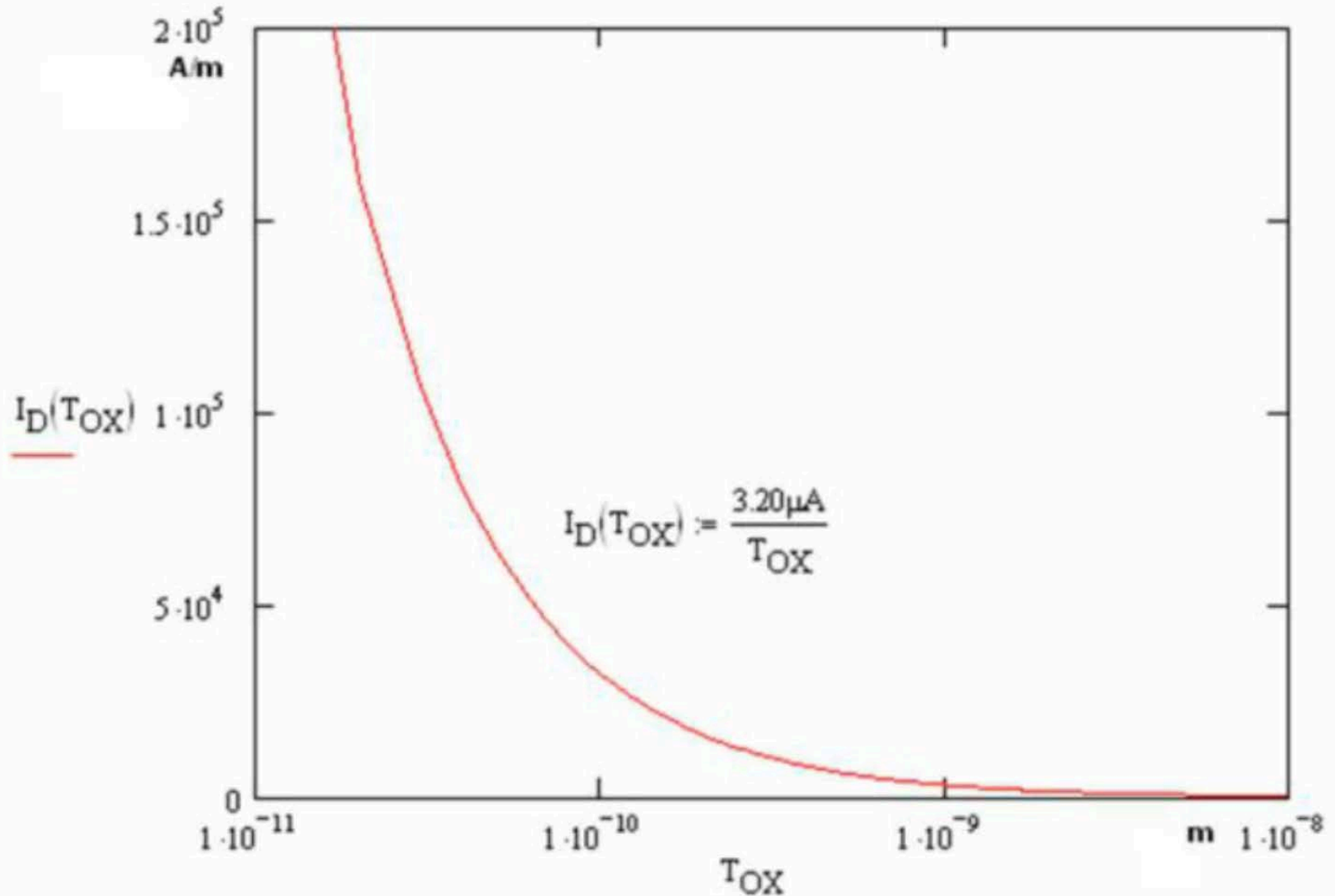
$$I_D \sim C_{OX}$$

$$I_D \sim \epsilon_{OX}/T_{OX}$$

$$I_D \sim 1/T_{OX}$$

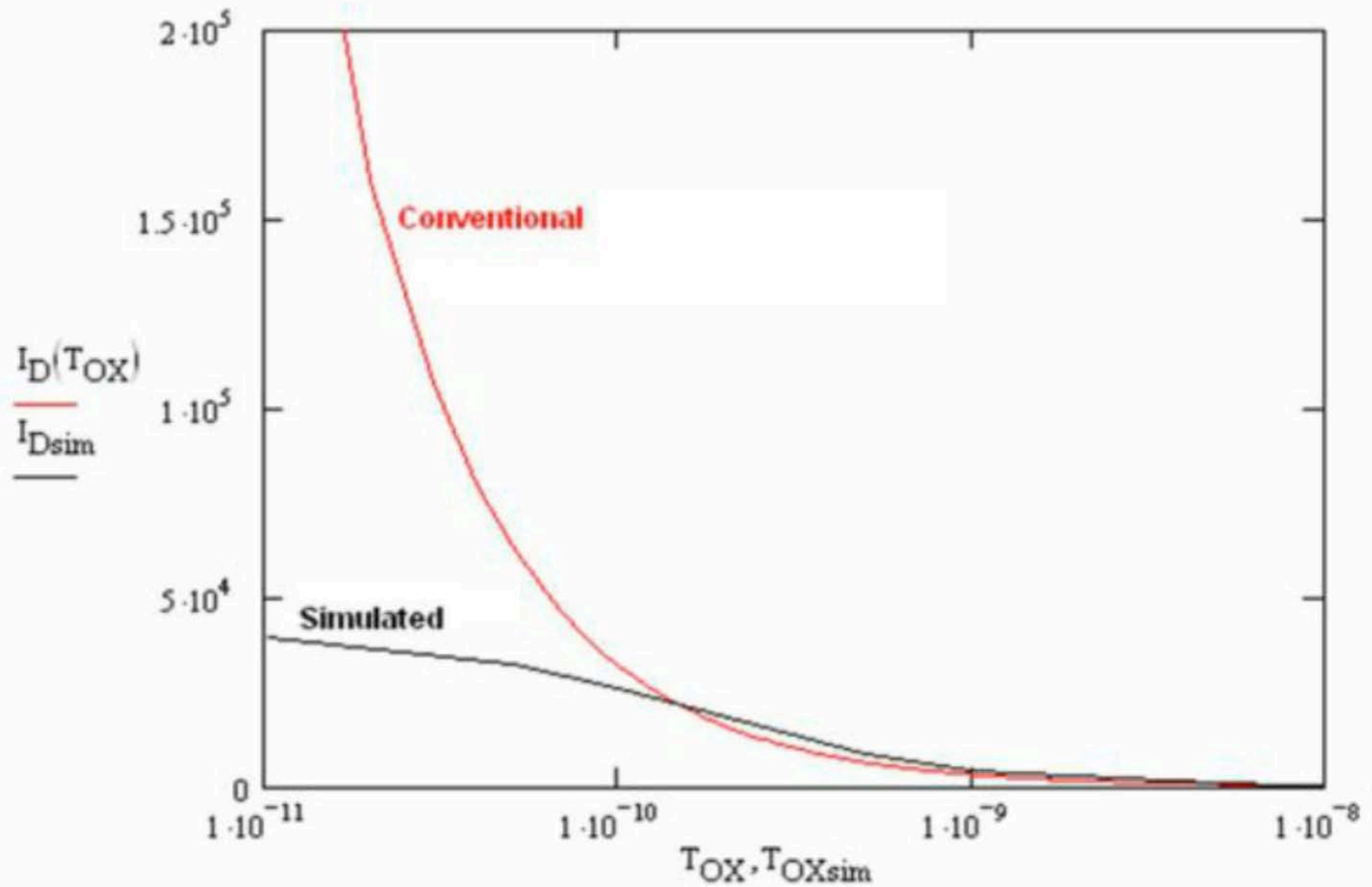
$$I_D = 320\mu A/\mu m * (10nm/T_{OX})$$

# 1a) Conventional Plot: $I_{ON}$ vs. $T_{OX}$





# 1a) Simulated Plot: $I_{ON}$ vs. $T_{OX}$



# 1b) Conventional vs. Simulated

---

## Conventional Theory:

$$I_D \sim C_{OX}$$

## FETToy:

$$I_D \sim C_G = C_{OX}C_Q/(C_{OX}+C_Q)$$

$$C_G \rightarrow C_{OX} \quad \text{if } C_Q \gg C_{OX} \quad \text{(Conventional holds)}$$

$$C_G = C_{OX}C_Q/(C_{OX}+C_Q) \quad \text{otherwise} \quad \text{(Conventional fails)}$$

Decreasing  $T_{OX} \rightarrow$  Increasing  $C_{OX} \rightarrow$  Failure of  $C_Q \gg C_{OX}$  condition

$$C_Q = q^2D = q^2 \cdot 2m_{eff}/(\pi h_{bar}) = 2.54E-5F/cm^2$$

$$C_{OX} \gg C_Q \quad \text{(Conventional holds)}$$

Fails when:  $C_{OX} = C_Q$

$$C_{OX} = C_Q$$

$$\epsilon_{OX}/T_{OX} = C_Q$$

$$T_{OX} = \epsilon_{OX}/C_Q$$

$$\underline{T_{OX} = .136nm}$$

# Problem 2

---

*One might think that a lighter effective mass would give a transistor higher current, because with a lighter mass, carriers travel faster. This exercise will demonstrate that this is not always the case.*

2) Explore the role of effective mass on the on-current of a ballistic silicon MOSFET. For this calculation, you should also use **1D electrostatics** (gate control parameter = 1 and drain control parameter = 0) and vary the effective mass from  **$10m_0$**  to  **$0.01m_0$** . Assume  $V_{DD} = 1V$  and room temperature operation.

2a) Produce a plot of the on-current (the current for  $V_G = V_D = V_{DD}$ ) vs. effective mass. You might expect the on-current to be proportional to the velocity (which is inversely proportional to the square root of the effective mass). Compare your plot against this expectation by appropriately plotting the results.

2b) Provide a physical explanation for the shape of your plot. That is, explain why the plot of  $I_D(\text{on})$  vs.  $m^*$  has a maximum. Hint: consider the influence of the quantum capacitance.

## 2a) Conventional Plot: $I_{ON}$ vs. $m_{eff}$

Common Material Parameters and Settings:  
 $m_{eff} = 10m_0$        $I_{D0} = ??$

Device | Models | Environment

Model: MOSFET

Single Gate/Double Gate: Single Gate

Transport Effective Mass: 10

Valley Degeneracy: 2

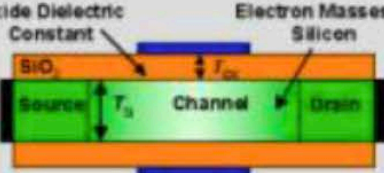
Floating Boundary Flag: no

Body Thickness: 10nm

Source Doping Density:  $1.0e20/cm^3$

Oxide Dielectric Constant

Electron Masses in Silicon



Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Gate Insulator Thickness: 1.5nm

Insulator Dielectric Constant: 3.9

Threshold Voltage: 0.32V

Gate Control Parameter: 1

Drain Control Parameter: 0

Series Resistance (ohm-um): 0

Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Ambient Temperature: 300K

Initial Gate Voltage: 0V

Final Gate Voltage: 2V

Number of Gate Voltage Bias Points: 13

Initial Drain Voltage: 0V

Final Drain Voltage: 1V

Number of Drain Voltage Bias Points: 30

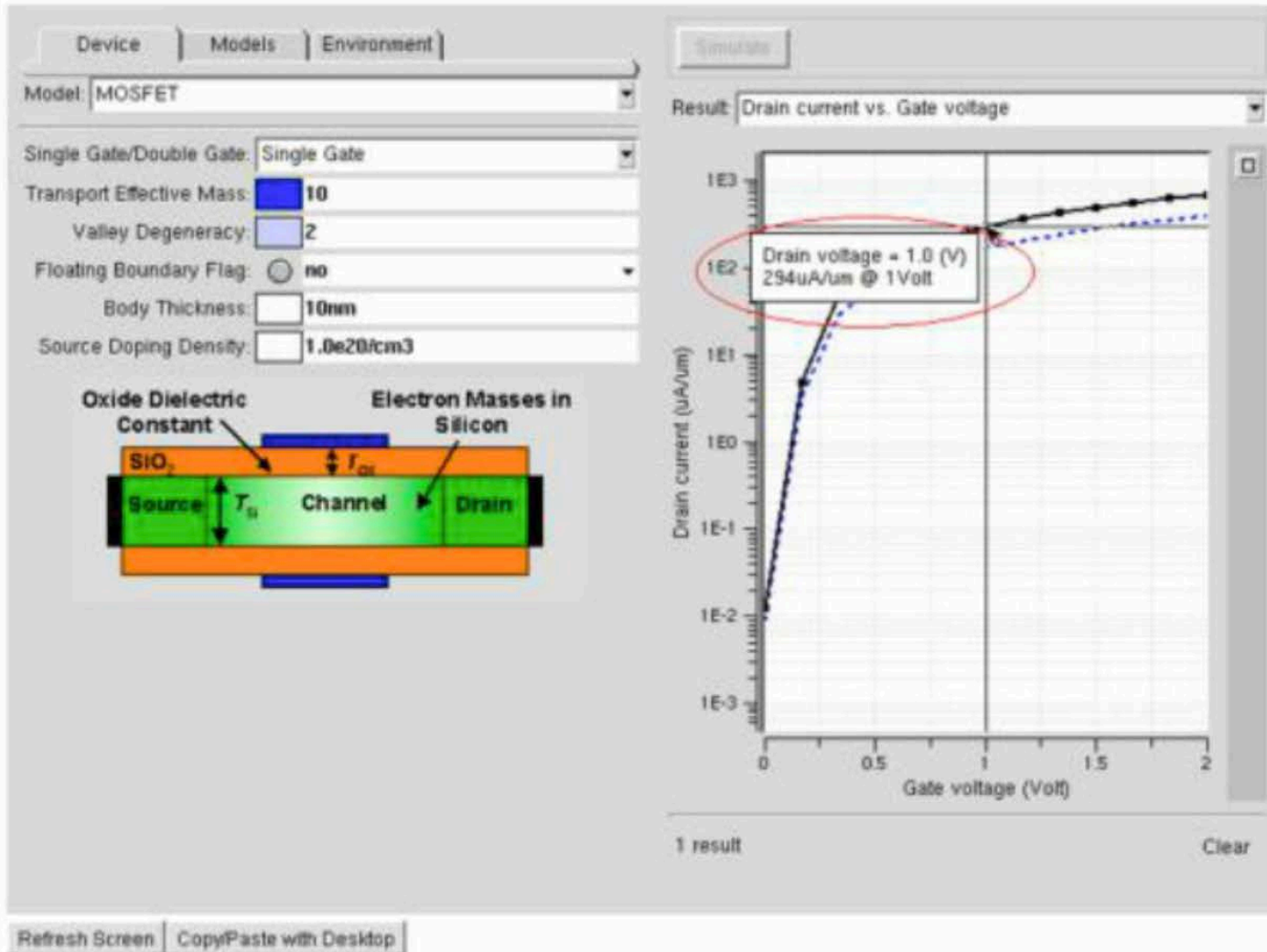
Refresh Screen | Copy/Paste with Desktop

## 2a) Conventional Plot: $I_{ON}$ vs. $m_{eff}$

Result for ID0:

$$m_{eff} = 10m_0$$

$$I_{D0} = 294 \mu A/\mu m$$



## 2a) Conventional Plot: $I_{ON}$ vs. $m_{eff}$

---

$$I_D = Q \cdot v$$

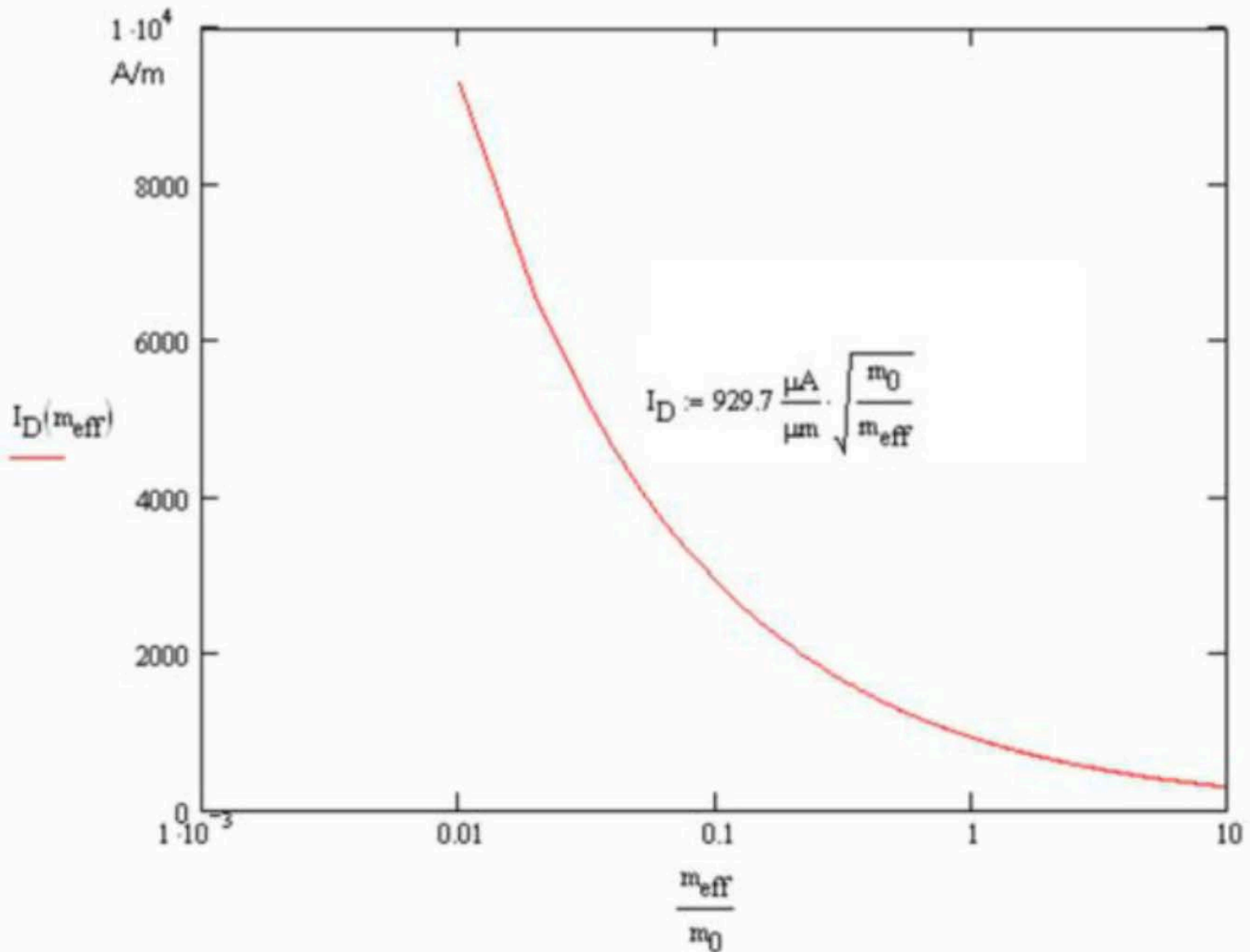
$$v \sim \frac{1}{\sqrt{m_{eff}}}$$

$$I_D \sim \frac{1}{\sqrt{m_{eff}}}$$

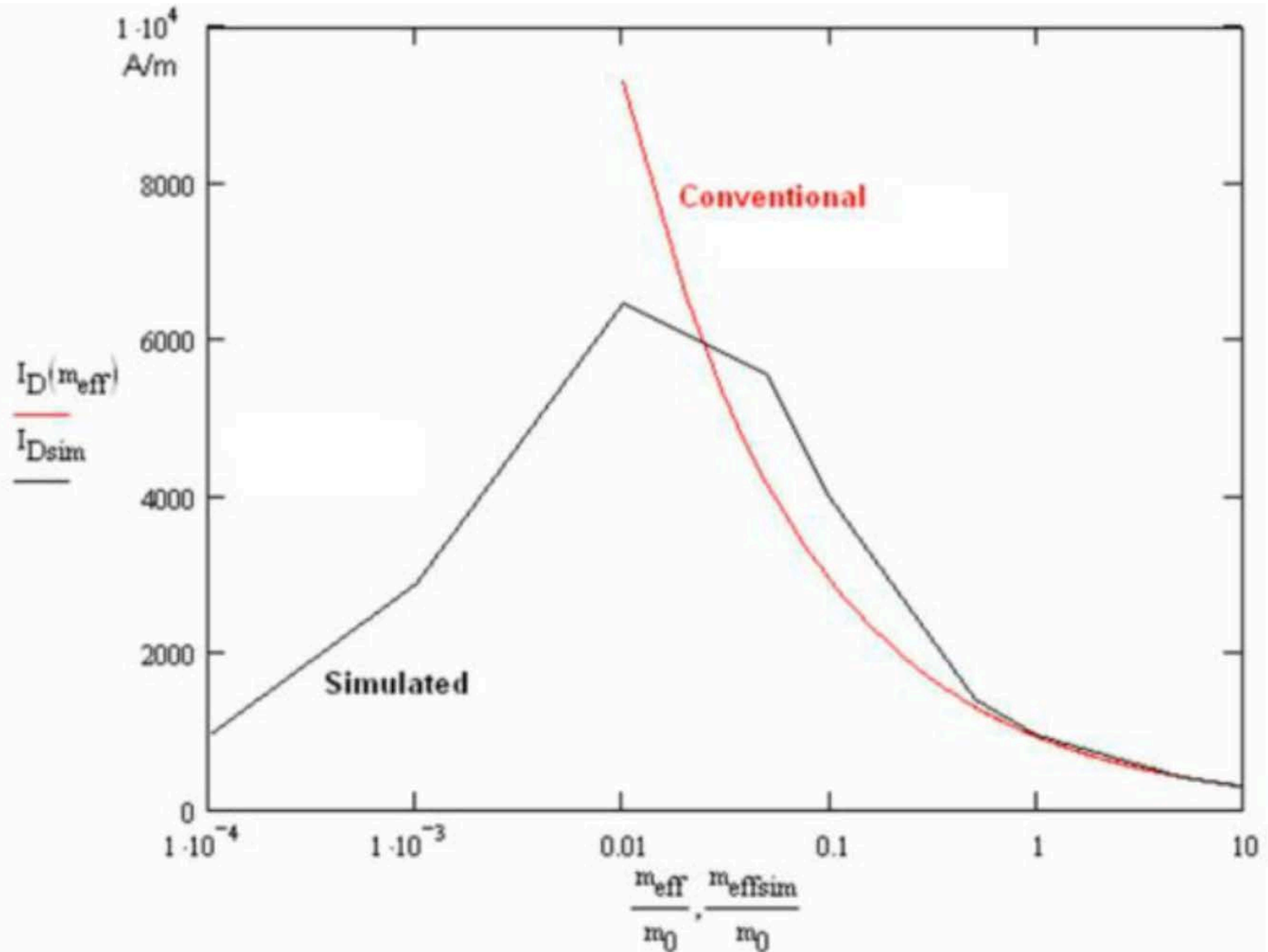
$$I_D = \frac{8.874 \cdot 10^{-13} \frac{\mu A}{\mu m} \cdot \sqrt{kg}}{\sqrt{m_{eff}}}$$

$$I_D = 929.7 \frac{\mu A}{\mu m} \cdot \sqrt{\frac{m_0}{m_{eff}}}$$

## 2a) Conventional Plot: $I_{ON}$ vs. $m_{eff}$



## 2a) Conventional vs. Simulated





## 2b) Conventional vs. Simulated

---

Recall:

$$I_D = Q \cdot v_{inj} \quad \text{where} \quad Q = C_G(V_G - V_T)$$

Conventional Theory:

$$C_G = C_{OX}$$

FETToy:

$$C_G = C_{OX} C_Q / (C_{OX} + C_Q) \quad \text{where} \quad C_Q = 2 \cdot q^2 \cdot m_{eff} / (\pi \cdot h_{bar}^2) \rightarrow C_Q \sim m_{eff}$$

$$C_G \rightarrow C_{OX} \quad \text{if} \quad C_Q \gg C_{OX} \quad (\text{conventional holds})$$

Decrease  $m_{eff} \rightarrow$  failure of  $C_Q \gg C_{OX}$  condition  $\rightarrow$  Decrease  $C_G$

$$I_D = C_G(V_G - V_T)v_{inj} \quad \text{Decrease } C_G \rightarrow \text{Decrease } I_D$$

## 2b) Conventional vs. Simulated

---

Further decreasing  $m_{\text{eff}}$ :

Decreasing  $m_{\text{eff}}$  will eventually lead to  $C_Q \ll C_{\text{OX}} \rightarrow C_G \rightarrow C_Q$

$$I_D = C_Q \cdot (V_G - V_T) \cdot v_{\text{inj}}$$

$$I_D \sim m_{\text{eff}} \cdot v_{\text{inj}}$$

$$I_D \sim m_{\text{eff}} / \sqrt{m_{\text{eff}}}$$

$$I_D \sim \sqrt{m_{\text{eff}}}$$

**Conclusion:**

$$I_D \sim 1/\sqrt{m_{\text{eff}}} \quad \text{if } C_Q \gg C_{\text{OX}}$$

$$I_D \sim \sqrt{m_{\text{eff}}} \quad \text{if } C_Q \ll C_{\text{OX}}$$

# Problem 3

---

*There is considerable interest these days in exploring the use of alternative channel materials such as Ge, GaAs, and InAs. How much performance advantage can be expected from these “new” materials?*

*3) Compare the on-currents of ballistic silicon, germanium, gallium arsenide, and indium arsenide n-MOSFETs. For this calculation, you should also use **1D electrostatics** (gate control parameter = 1 and drain control parameter = 0) Assume  $V_{DD} = 1.0V$ , room temperature operation, and select the appropriate effective mass and valley degeneracies for each case.*

*3a) Assume an insulator thickness of 5 nm and a dielectric constant of 3.9. Simulate the four ballistic MOSFETs and compare their on-currents.*

*3b) Assume an insulator thickness of 0.5 nm and a dielectric constant of 3.9. Simulate the four ballistic MOSFETs and compare their on-currents.*

Acknowledgement: The problem is provided by Prof. Mark Lundstrom, Purdue University

### 3a) On-currents with $T_{ox} = 5\text{nm}$

---

Required Material Parameters:

Material	Effective Electron Mass	Valley Degeneracy
Si	$.19m_0$	2
Ge	$.082m_0$	1
GaAs	$.067m_0$	1
InAs	$.023m_0$	1

# 3a) On-currents with $T_{ox} = 5\text{nm}$

## Common Material Parameters and Settings:

Device | Models | Environment

Gate Insulator Thickness:

Insulator Dielectric Constant:

Threshold Voltage:

Gate Control Parameter:

Drain Control Parameter:

Series Resistance (ohm-um):

Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Ambient Temperature:

Initial Gate Voltage:

Final Gate Voltage:

Number of Gate Voltage Bias Points:

Initial Drain Voltage:

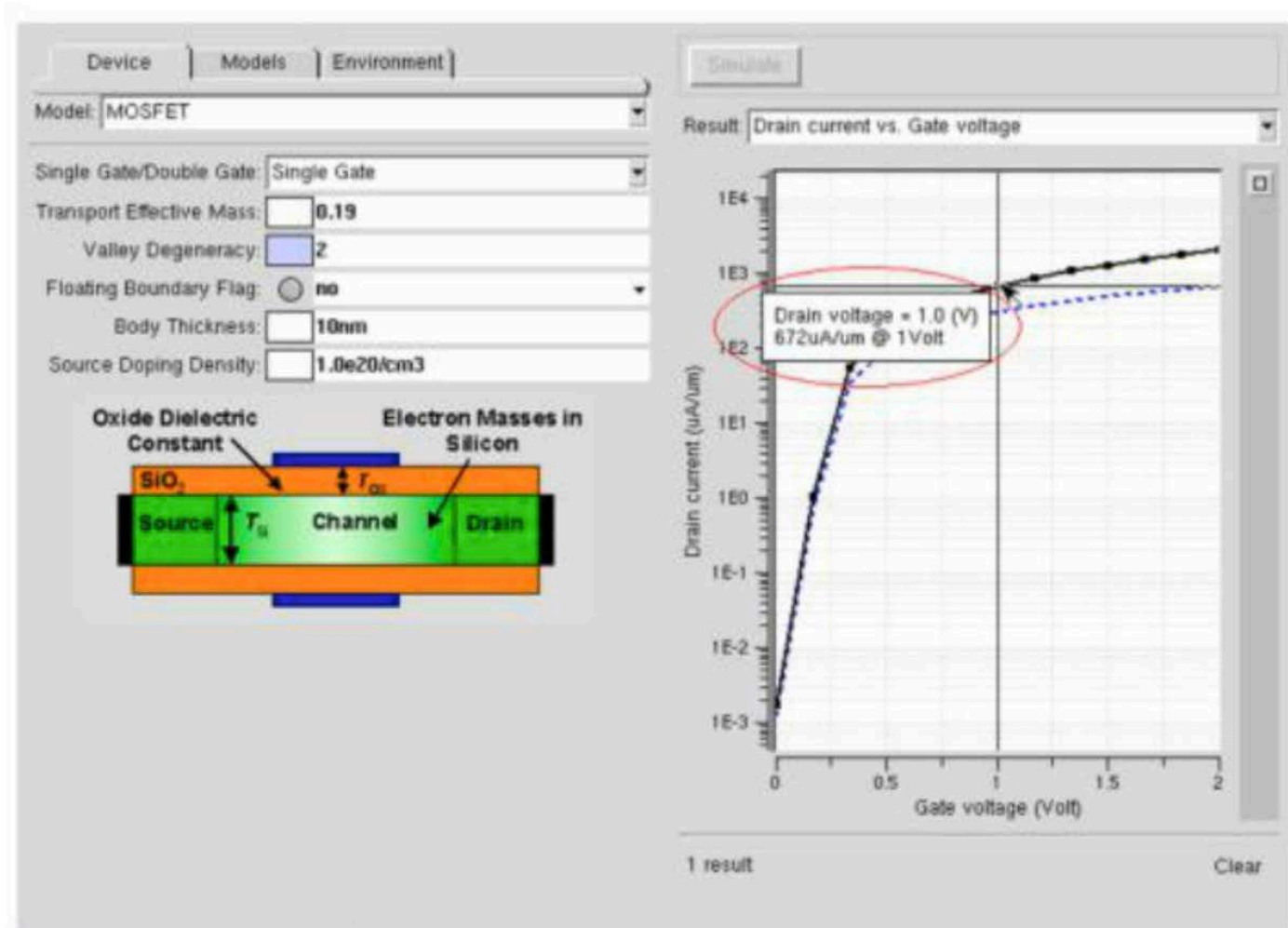
Final Drain Voltage:

Number of Drain Voltage Bias Points:

Refresh Screen | Copy/Paste with Desktop

# 3a) On-currents with $T_{ox} = 5\text{nm}$

Material Parameters and Settings for Si,  
Result for Si MOSFET:  $I_{ON\_Si} = 672\text{A/m}$



### 3a) On-currents with $T_{OX} = 5\text{nm}$

---

Table of Results:

Material	Effective Electron Mass	Valley Degeneracy	$I_{ON}(\text{A/m})$ $T_{OX} = 5\text{nm}$
Si	$.19m_0$	2	672
Ge	$.082m_0$	1	1270
GaAs	$.067m_0$	1	1450
InAs	$.023m_0$	1	2350

## 3b) On-currents with $T_{OX} = .5\text{nm}$

Table of Results:

Material	Effective Electron Mass	Valley Degeneracy	$I_{ON}(\text{A/m})$ $T_{OX} = 5\text{nm}$	$I_{ON}(\text{A/m})$ $T_{OX} = .5\text{nm}$
Si	$.19m_0$	2	672	8730
Ge	$.082m_0$	1	1270	8230
GaAs	$.067m_0$	1	1450	8060
InAs	$.023m_0$	1	2350	6140



# 3c) Comparison: 5nm vs. 0.5nm

$T_{OX} = 5\text{nm}$

Decreasing  $m_{\text{eff}} \rightarrow$  Increasing  $I_{ON}$

Implies:  $C_Q \gg C_{OX}$  or  $C_Q \approx C_{OX}$

$C_Q \sim m_{\text{eff}}$

For InAs with  $T_{OX} = 5\text{nm}$

$C_Q$ :

$$C_Q = q^2 m_{\text{eff}} / (\pi \cdot \hbar^2) \cdot n_v$$

$$C_Q = 1.54\text{E-}6\text{F/cm}^2$$

$C_{OX}$ :

$$C_{OX} = \epsilon_{OX} / T_{OX} = 3.9\epsilon_0 / T_{OX}$$

$$C_{OX} = 6.91\text{E-}7\text{F/cm}^2$$

Conclusion:

$$C_Q > C_{OX}$$

At conventional limit,  $CG \approx COX$

$$I_D = Q \cdot v \sim 1/\sqrt{m_{\text{eff}}}$$

## 3c) Comparison: 5nm vs. 0.5nm

---

$$T_{OX} = 0.5\text{nm}$$

Decreasing  $m_{\text{eff}} \rightarrow$  Decreasing  $I_{ON}$

Implies:  $C_Q \ll C_{OX}$

For InAs with  $T_{OX} = 0.5\text{nm}$

$$C_Q = 1.54\text{E-}6\text{F/cm}^2$$

$C_{OX}$ :

$$C_{OX} = 6.91\text{E-}6\text{F/cm}^2$$

Conclusion:

$$C_{OX} \gg C_Q$$

At  $C_Q$  limit,  $C_G \ll C_{OX}$

$$I_D = Q \cdot v \sim \sqrt{m_{\text{eff}}}$$

See Problem 2 Part b for more details on the relationship between  $C_Q$  and  $m_{\text{eff}}$ .

# Problem 4

---

*The on-current is commonly used as a device metric, but the entire I-V characteristic is important in a switching transient. How do the shapes of the  $I_{DS}$  vs.  $V_{DS}$  characteristics of different MOSFETs compare?*

4) Simulate ballistic silicon, germanium, gallium arsenide, and indium arsenide n-MOSFETs using an insulator thickness of 1nm. For this calculation, you should also use **1D electrostatics** (gate control parameter = 1 and drain control parameter = 0) Assume  $V_{DD} = 1V$ , room temperature operation and select the appropriate effective mass and valley degeneracies for each case. For this exercise, you only need to consider  $V_G = V_{DD}$ .

4a) Normalize each  $I_{DS}$  vs.  $V_{DS}$  characteristic by plotting  $(I_{DS}/I_{ON})$  vs.  $V_{DS}$ . Plot all four results on the same set of axes and compare the shape.

4b) Discuss your results and provide a physical explanation for any difference that you observe.

## 4a) Simulated Plot of $I_D/I_{ON}$ vs. $V_{DS}$

---

Required Material Parameters:

Material	Effective Electron Mass	Valley Degeneracy
Si	.19 $m_0$	2
Ge	.082 $m_0$	1
GaAs	.067 $m_0$	1
InAs	.023 $m_0$	1

# 4a) Simulated Plot of $I_D/I_{ON}$ vs. $V_{DS}$

## Common Material Parameters and Settings:

Device | Models | Environment

Gate Insulator Thickness:

Insulator Dielectric Constant:

Threshold Voltage:

Gate Control Parameter:

Drain Control Parameter:

Series Resistance (ohm-um):

Device | Models | Environment

Ambient Temperature:

Initial Gate Voltage:

Final Gate Voltage:

Number of Gate Voltage Bias Points:

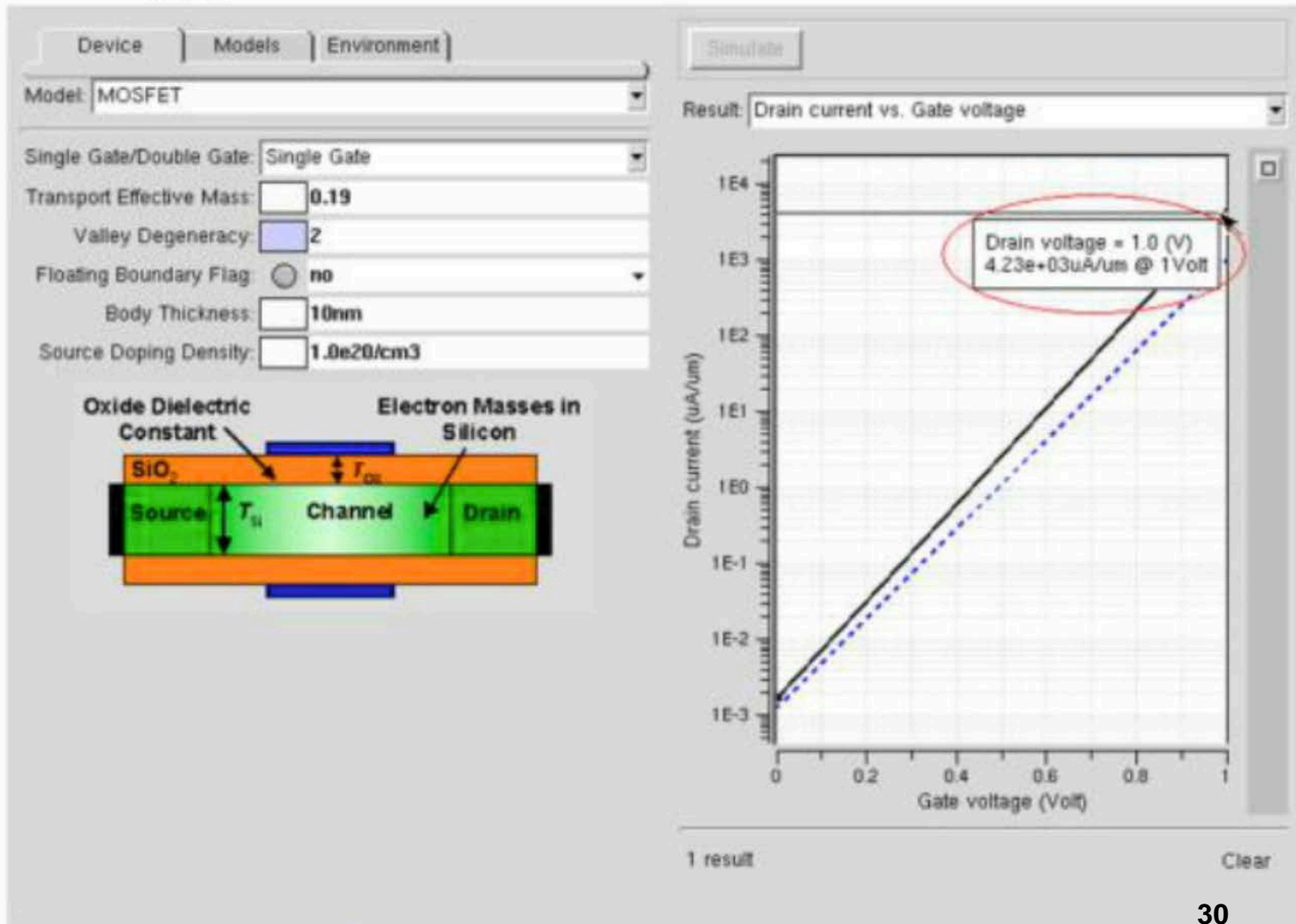
Initial Drain Voltage:

Final Drain Voltage:

Number of Drain Voltage Bias Points:

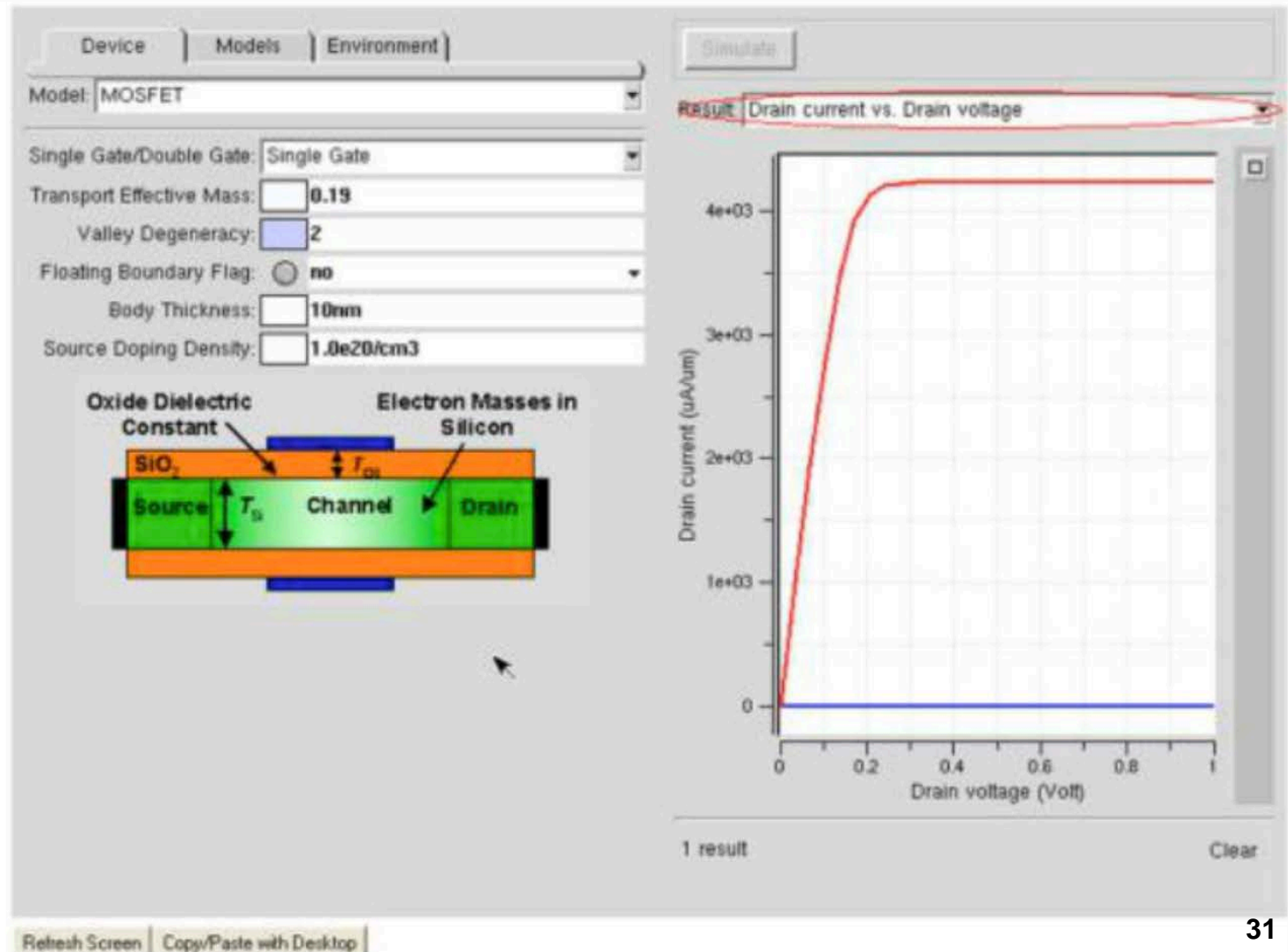
# 4a) Simulated Plot of $I_D/I_{ON}$ vs. $V_{DS}$

Material Parameters and Settings for Si,  
Result for Si MOSFET:  $I_{ON\ Si} = 4230A/m$



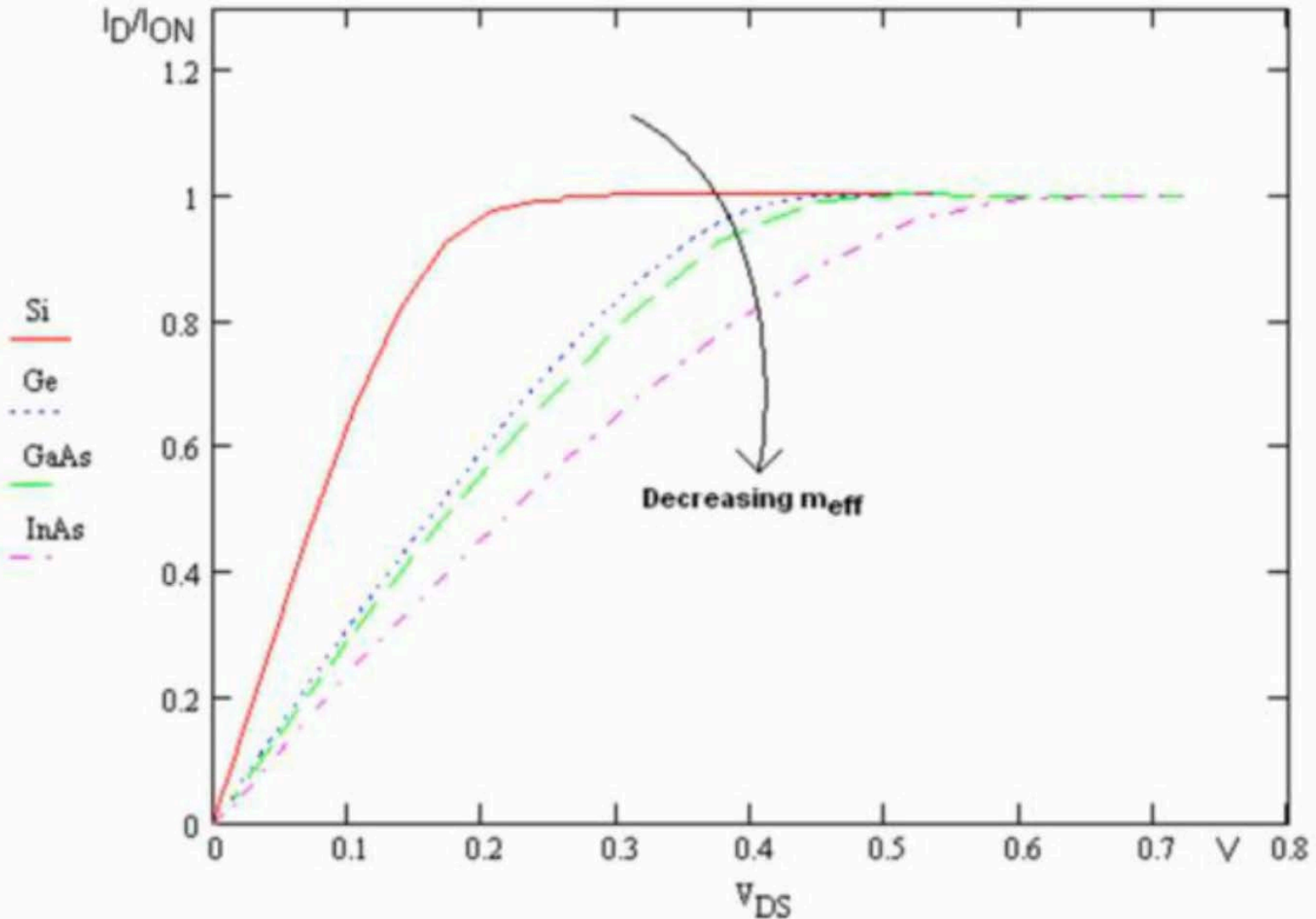
# 4a) Simulated Plot of $I_D/I_{ON}$ vs. $V_{DS}$

Obtaining IDS vs. VDS Data Points for Si MOSFET:



## 4a) Simulated Plot of $I_D/I_{ON}$ vs. $V_{DS}$

Simulated Plot of  $I_D/I_{ON}$  vs.  $V_{DS}$  for all MOSFETs:





## 4b) Explanation for difference in $V_{Dsat}$

Observation:

$m_{eff}$  decreases  $\rightarrow V_{Dsat}$  increases

Explanation:

1D Electrostatics:  $Q = V_G C_G$   $C_G$  is the series capacitance of  $C_q$  and  $C_{ox}$

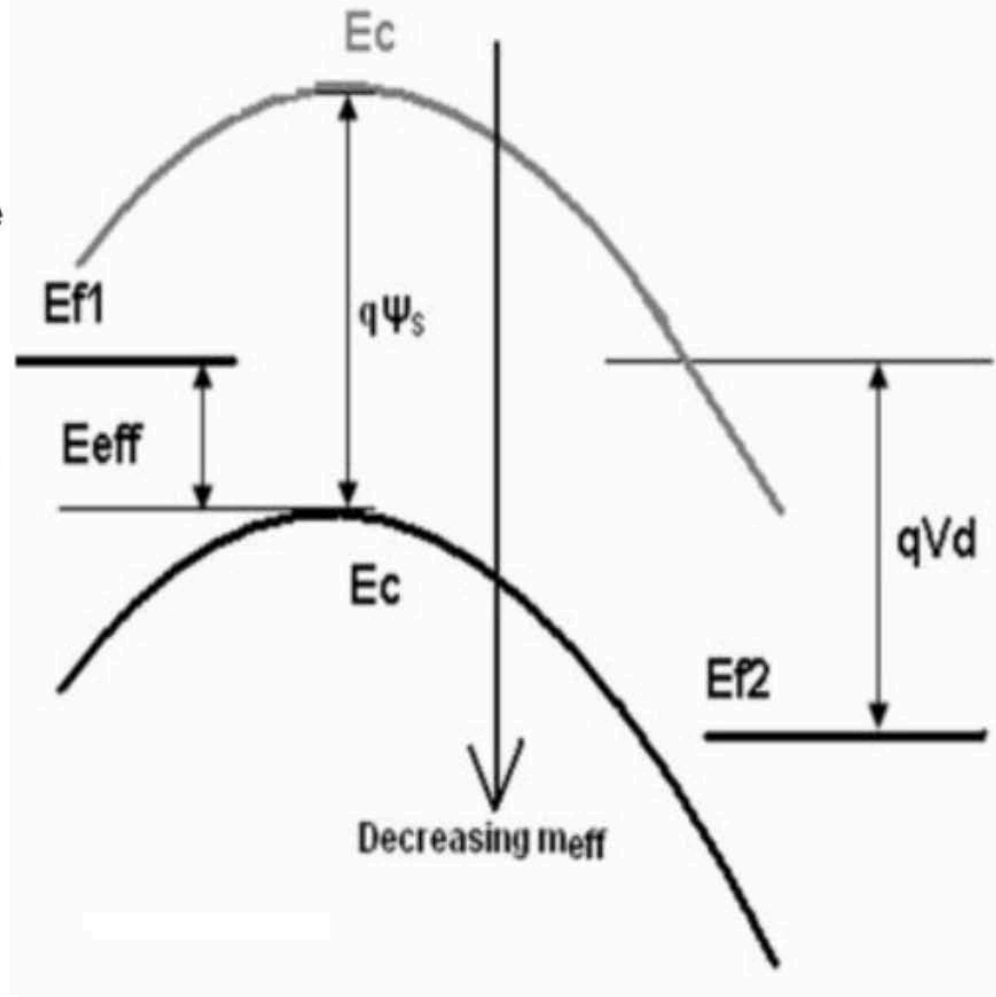
So  $\psi_s = C_{ox} / (C_{ox} + C_q) * V_G$

And  $C_q = \text{Const} * m_{eff}$ ,

The smaller  $C_q$  is, the larger  $\psi_s$  is, the lower the potential barrier height is.

The current saturates when drain voltage exceeds the difference between the source Fermi level and the top of the barrier.

Lower barrier height  $\rightarrow$  higher  $V_{Dsat}$



# Problem 5

---

*A silicon n-MOSFET typically delivers about twice the on-current of a silicon p-MOSFET. This difference is commonly attributed to difference in carrier mobility and saturation velocity. What does a ballistic model predict?*

5) Simulate a ballistic silicon, n-MOSFET and a ballistic p-MOSFET using 2nm of SiO<sub>2</sub> for the gate insulator,  $V_{DD} = 1V$ , and assuming room temperature operation. For this calculation, you should also use **1D electrostatics** (gate control parameter = 1 and drain control parameter = 0). You will need to identify the appropriate hole effective mass and valley degeneracy.

- a) Compare the on-currents of the two MOSFETs and explain the difference. Why does the n-MOSFET give higher current?
- b) Compare the low  $V_{DS}$  channel resistances of the two MOSFETs and explain the difference. Is the ratio of the channel resistances the same as the ratio of the on-currents? Provide a physical explanation for the result.
- c) Repeat parts a) and b) for a 0.5nm gate insulator.

Acknowledgement: The problem is provided by Prof. Mark Lundstrom, Purdue University

## 5a) n- vs. p-type on-current comparison, 2nm

---

Required Material Parameters:

	Si nMOSFET	Si pMOSFET
Transport Effective Mass	$0.19m_0$	$0.49m_0$
Valley Degeneracy	2	1

# 5a) n- vs. p-type on-current comparison, 2nm

## Common Material Parameters and Settings:

Device | Models | Environment

Gate Insulator Thickness:

Insulator Dielectric Constant:

Threshold Voltage:

Gate Control Parameter:

Drain Control Parameter:

Series Resistance (ohm-um):

Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Ambient Temperature:

Initial Gate Voltage:

Final Gate Voltage:

Number of Gate Voltage Bias Points:

Initial Drain Voltage:

Final Drain Voltage:

Number of Drain Voltage Bias Points:

Refresh Screen | Copy/Paste with Desktop

# 5a) n- vs. p-type on-current comparison, 2nm

## Material Parameters and Settings for Si nMOSFET:

The screenshot displays the configuration window for a Si nMOSFET simulation. The 'Device' tab is active, showing the following parameters:

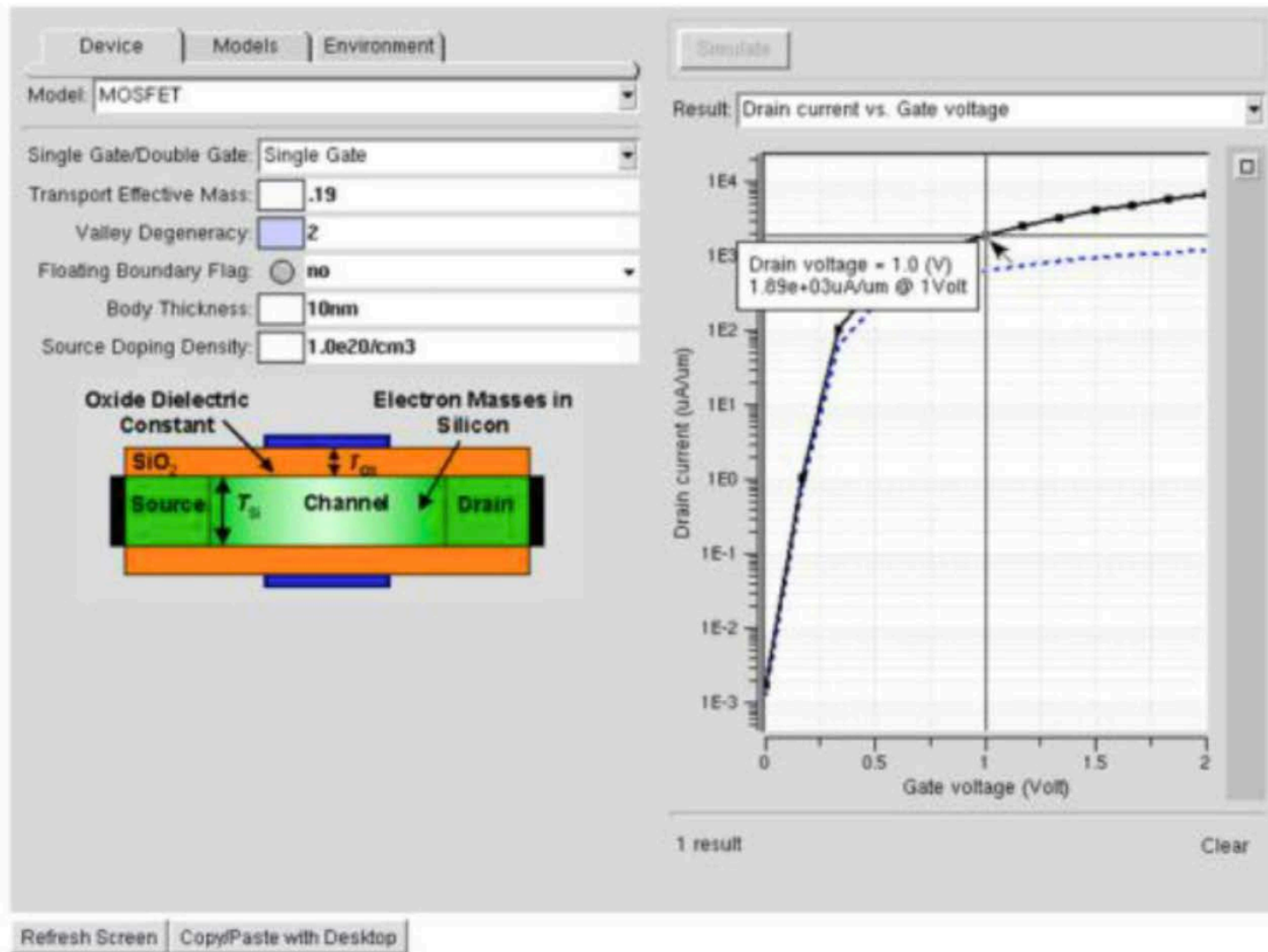
- Model: MOSFET
- Single Gate/Double Gate: Single Gate
- Transport Effective Mass: .19
- Valley Degeneracy: 2
- Floating Boundary Flag: no
- Body Thickness: 10nm
- Source Doping Density: 1.0e20/cm3

Below the parameters is a schematic diagram of the MOSFET structure. It shows a cross-section with a gate stack on top, a channel region in the middle, and source and drain regions at the bottom. Labels include 'Oxide Dielectric Constant' pointing to the gate stack, 'Electron Masses in Silicon' pointing to the channel, 'SiO<sub>2</sub>' for the gate dielectric, 'Source', 'Channel', and 'Drain' for the regions, and  $T_{ox}$  and  $T_{si}$  for the thicknesses of the oxide and silicon layers respectively.

The simulation area on the right is currently empty, showing 'No results' and a 'Clear' button. A 'Simulate' button with the text 'new input parameters' is visible at the top right of the interface.

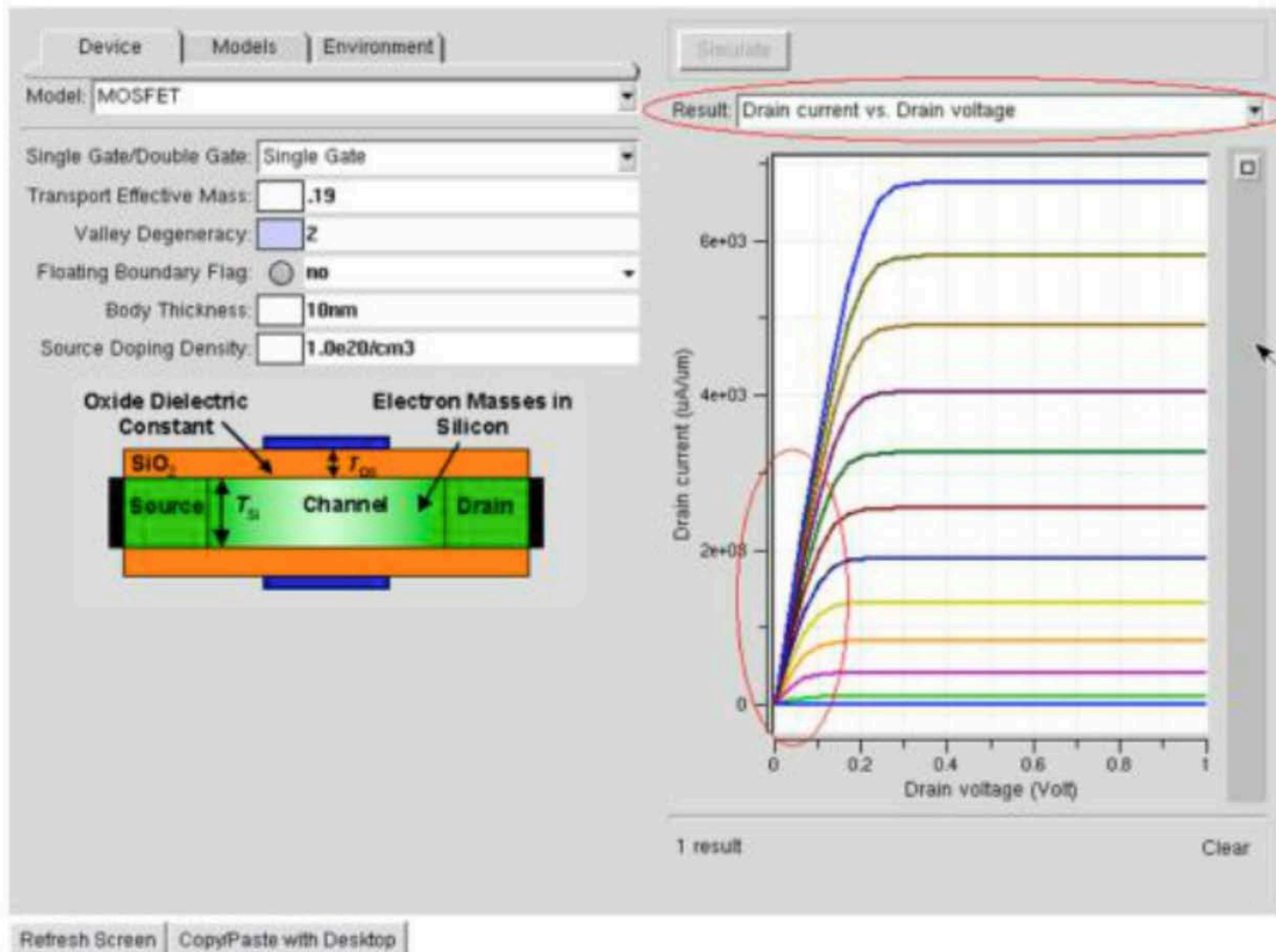
# 5a) n- vs. p-type on-current comparison, 2nm

Result for Si nMOSFET:  $I_{ON} = 1.89E3\mu A/\mu m$



# 5a) n- vs. p-type on-current comparison, 2nm

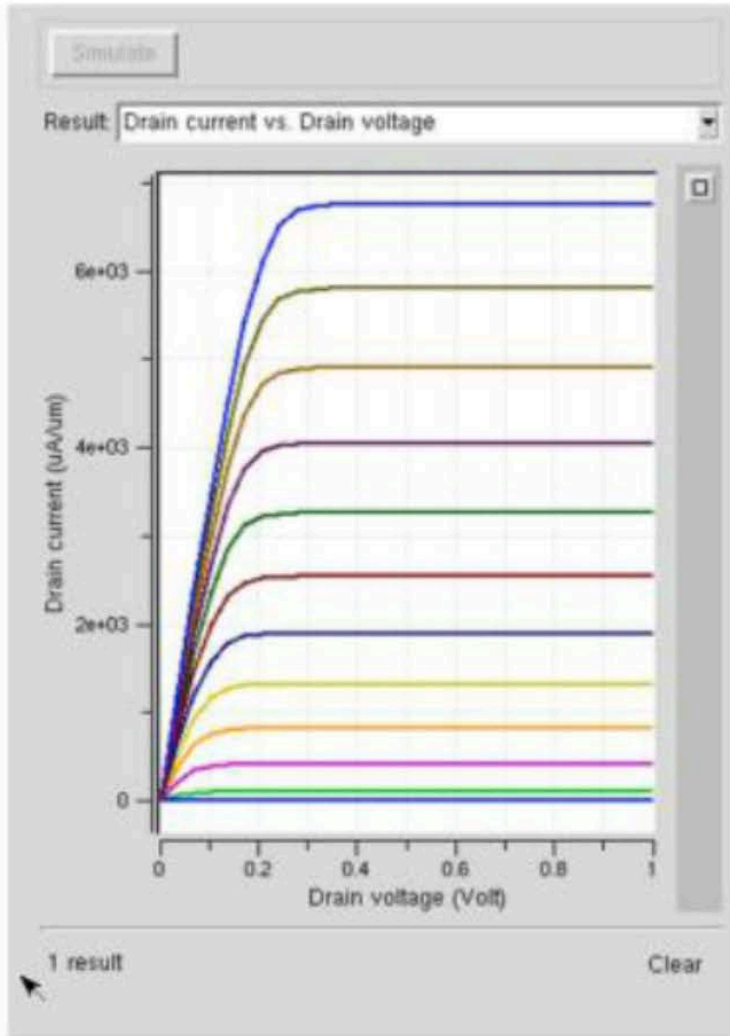
Result for Si nMOSFET:  $R_{\text{CHANNEL}} = ??$  for  $V_G = 1V$





# 5a) n- vs. p-type on-current comparison, 2nm

Result for Si nMOSFET:  $R_{\text{CHANNEL}} = 6.26\text{E-}5\Omega\text{m}$  for  $V_G = 1\text{V}$



$$I_D(0.0345\text{V}) = 649\text{uA/um}$$

$$I_D(0.069\text{V}) = 1.2\text{E}3\text{uA/um}$$

$$R_{\text{CHANNEL}} = (0.069\text{V} - 0.0345\text{V}) / (1.2\text{E}3\text{A/m} - 649\text{A/m})$$

$$\underline{R_{\text{CHANNEL}} = 6.26\text{E-}5\Omega\text{m}}$$



# 5a) n- vs. p-type on-current comparison, 2nm

---

Results for Si nMOSFET and pMOSFET:

	Si nMOSFET	Si pMOSFET
$I_{ON}$	1.89E3 $\mu$ A/ $\mu$ m	1.13E3 $\mu$ A/ $\mu$ m
$R_{Channel}$	6.26E-5 $\Omega$ m	2.1E-4 $\Omega$ m

# 5a) n- vs. p-type on-current comparison, 2nm

Comparison for Si nMOSFET and pMOSFET  $I_{ON}$ :

	Si nMOSFET	Si pMOSFET
$I_{ON}$	1.89E3uA/um	1.13E3uA/um
$R_{Channel}$	6.26E-5Ωm	2.1E-4Ωm

$$I_{ONn}/I_{ONp} = 1.67$$

$$I_{ON} \sim 1/\sqrt{m_{eff}}$$

$$I_{ONn}/I_{ONp} \sim (1/\sqrt{m_{effn}})^*(1/\sqrt{m_{effp}})^{-1} = \sqrt{m_{effp}}/\sqrt{m_{effn}}$$

$$\sqrt{m_{effp}}/\sqrt{m_{effn}} = 1.54$$

## 5b) n- vs. p-type $R_{\text{CHANNEL}}$ comparison, 2nm

Comparison for Si nMOSFET and pMOSFET  $R_{\text{CHANNEL}}$ :

	Si nMOSFET	Si pMOSFET
$I_{\text{ON}}$	1.89E3uA/um	1.13E3uA/um
$R_{\text{Channel}}$	6.26E-5 $\Omega$ m	2.1E-4 $\Omega$ m

$$R_{\text{CHANNELn}}/R_{\text{CHANNELp}} = .298$$

## 5c) n- vs. p-type comparisons, .5nm

Comparison for Si nMOSFET and pMOSFET at 0.5nm:

	Si nMOSFET	Si pMOSFET
$I_{ON}$	8.73E3uA/um	5.46E3uA/um
$R_{Channel}$	2.56E-5Ωm	3.56E-4Ωm

$$I_{ONn}/I_{ONp} = 1.6$$

$$I_{ONn}/I_{ONp} = n_{vn} m_{effn} \sqrt{m_{effp}} / (n_{vp} m_{effp} \sqrt{m_{effn}}) \quad \text{if } C_G \rightarrow C_Q$$

$$I_{ONn}/I_{ONp} = 1.2 \quad \text{if } C_G \rightarrow C_Q$$

$$R_{CHANNELn}/R_{CHANNELp} = .719$$

# Problem 6

---

*In FETToy, two-dimensional electrostatics is treated with a simple circuit model and two parameters, a gate control parameter and a drain control parameter.*

6) Simulate a ballistic silicon, n-MOSFET using an insulator thickness of 2 nm (SiO<sub>2</sub>) and  $V_{DD} = 1V$ , and assuming room temperature operation.

6a) Set the gate control parameter to 1.0 and the drain control parameter to 0.0 and run a simulation. Then examine the plot of charge,  $Q$ , vs.  $V_{GS}$  at high and low  $V_{DS}$ . Explain what determines the slope of the two plots and how you can calculate the slope by hand. Also examine the charge vs.  $V_{DS}$  plot and explain why it is not constant.

6b) Adjust the gate and drain control parameters to give a subthreshold swing of  $S = 100$  mV/decade and a DIBL of 100 mV/V. Repeat the simulation, compare the results to part a) and explain the differences.

6c) Repeat parts a) and b) but this time use an insulator thickness of 0.5 nm.

Acknowledgement: The problem is provided by Prof. Mark Lundstrom, Purdue University

# 6a) 1D Electrostatics: Charge vs. Voltage, 2nm

## Material Parameters and Settings:

Device | Models | Environment

Model: MOSFET

Single Gate/Double Gate: Single Gate

Transport Effective Mass: 0.19

Valley Degeneracy: 2

Floating Boundary Flag: no

Body Thickness: 10nm

Source Doping Density:  $1.0e20/cm^3$

Oxide Dielectric Constant

Electron Masses in Silicon

The diagram shows a cross-section of a MOSFET. The top layer is SiO<sub>2</sub> (gate insulator) with thickness  $T_{ox}$ . Below it is the silicon substrate with thickness  $T_s$ . The substrate is divided into Source, Channel, and Drain regions. The Channel region is highlighted in green. Labels include 'Oxide Dielectric Constant' and 'Electron Masses in Silicon'.

Device | Models | Environment

Gate Insulator Thickness: 2nm

Insulator Dielectric Constant: 3.9

Threshold Voltage: 0.32V

Gate Control Parameter: 1

Drain Control Parameter: 0

Series Resistance (ohm-um): 0

Device | Models | Environment

Ambient Temperature: 300K

Initial Gate Voltage: 0V

Final Gate Voltage: 2.0V

Number of Gate Voltage Bias Points: 30

Initial Drain Voltage: 0V

Final Drain Voltage: 2V

Number of Drain Voltage Bias Points: 30

# 6a) 1D Electrostatics: Charge vs. Voltage, 2nm

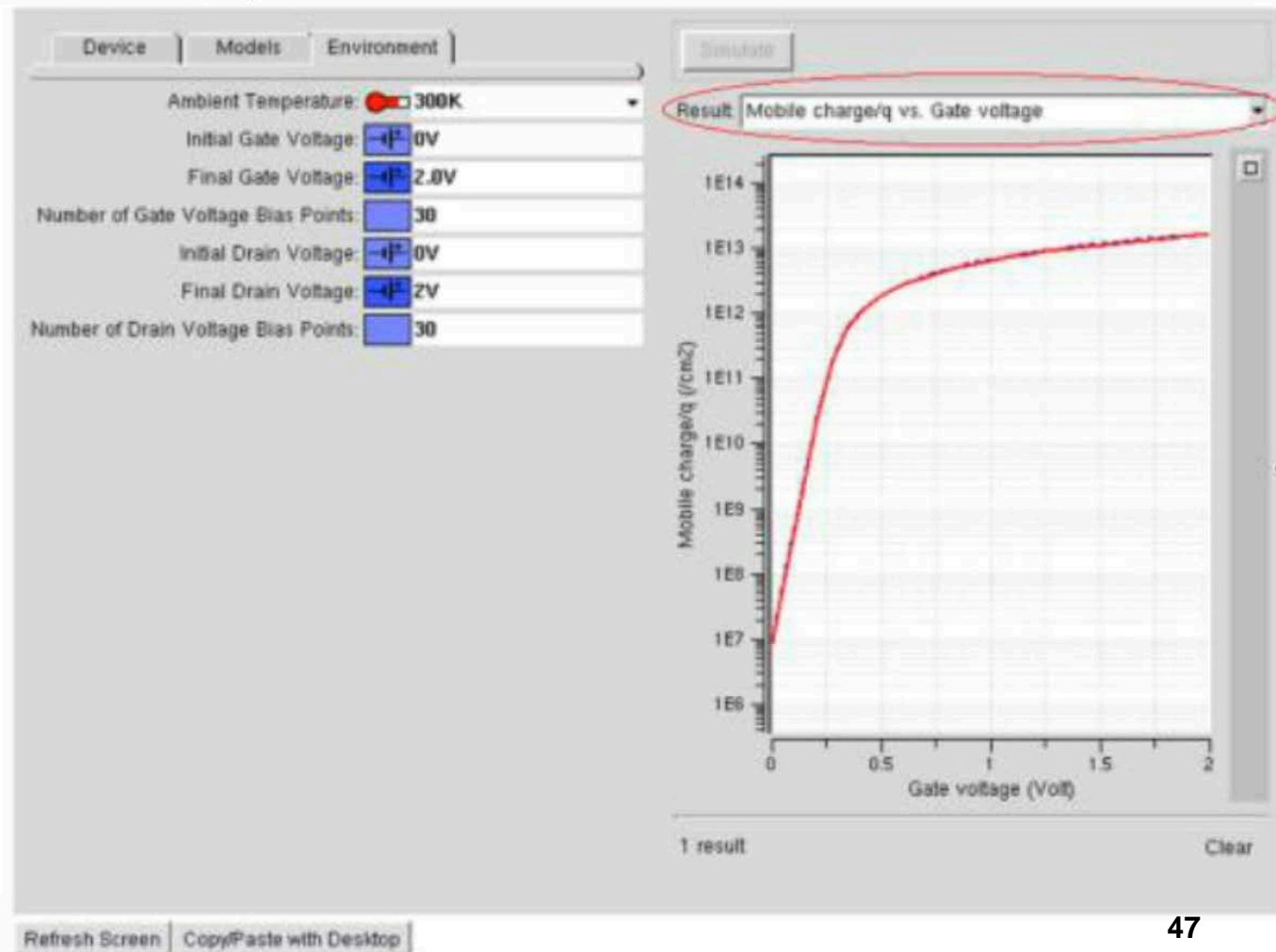
Simulation Result:

Slope for  $V_{DS} = 2V$ :

$\text{slope}_h = ??$

Slope for  $V_{DS} = 0.069V$ :

$\text{slope}_l = ??$



# 6a) 1D Electrostatics: Charge vs. Voltage, 2nm

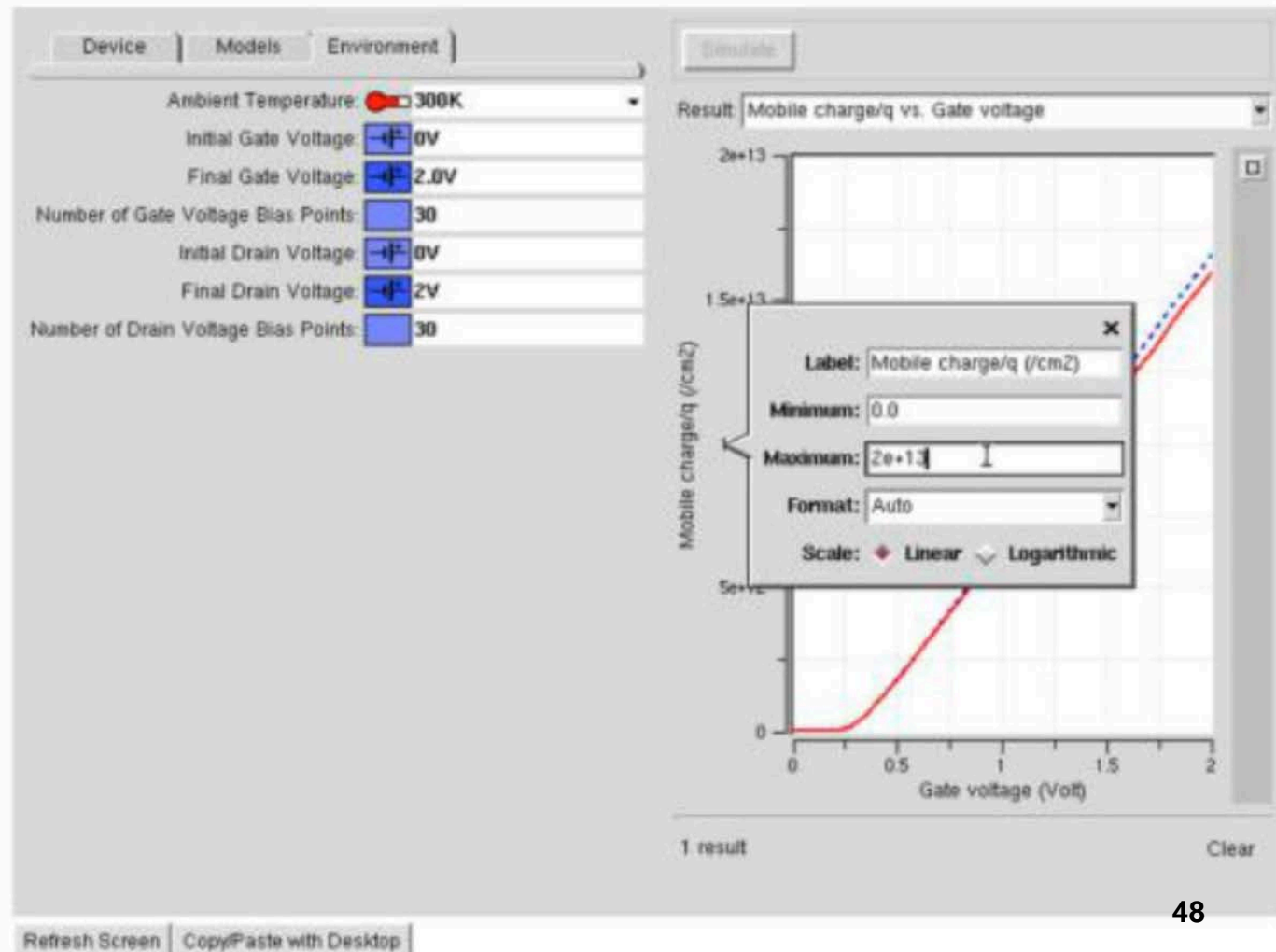
Simulation Result:

Slope for  $V_{DS} = 2V$ :

$\text{slope}_h = ??$

Slope for  $V_{DS} = 0.069V$ :

$\text{slope}_l = ??$





# 6a) 1D Electrostatics: Charge vs. Voltage, 2nm

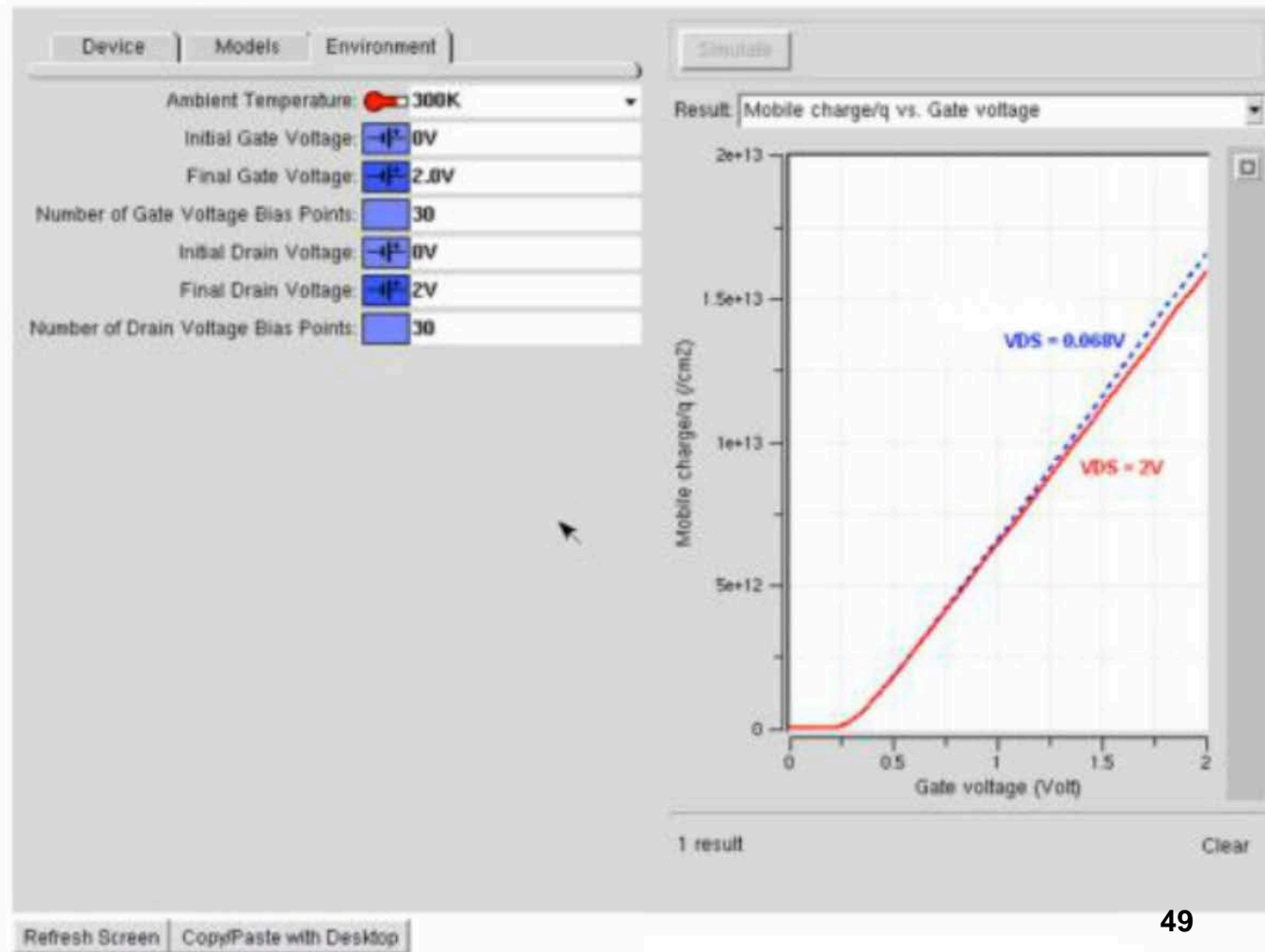
Simulation Result:

Slope for  $V_{DS} = 2V$ :

Slope for  $V_{DS} = 0.069V$ :

$\text{slope}_h = 1.54E-6 \text{ F/cm}^2$

$\text{slope}_l = 1.58E-6 \text{ F/cm}^2$



## 6a) 1D Electrostatics: Charge vs. Voltage, 2nm

---

Determining the Slope of Charge vs. Gate Voltage by Hand:

$$1\text{D Electrostatics} \rightarrow C_D = C_S = 0$$

$$\text{Since } V_G = Q/C_G$$

$$Q = C_G * V_G$$

Slope is determined by  $C_G$ ,  $C_G \rightarrow C_{OX}$  if  $C_Q \gg C_{OX}$

$$C_{OX} = 3.9\epsilon_0/T_{OX} = 1.73\text{E-}6\text{F/cm}^2$$

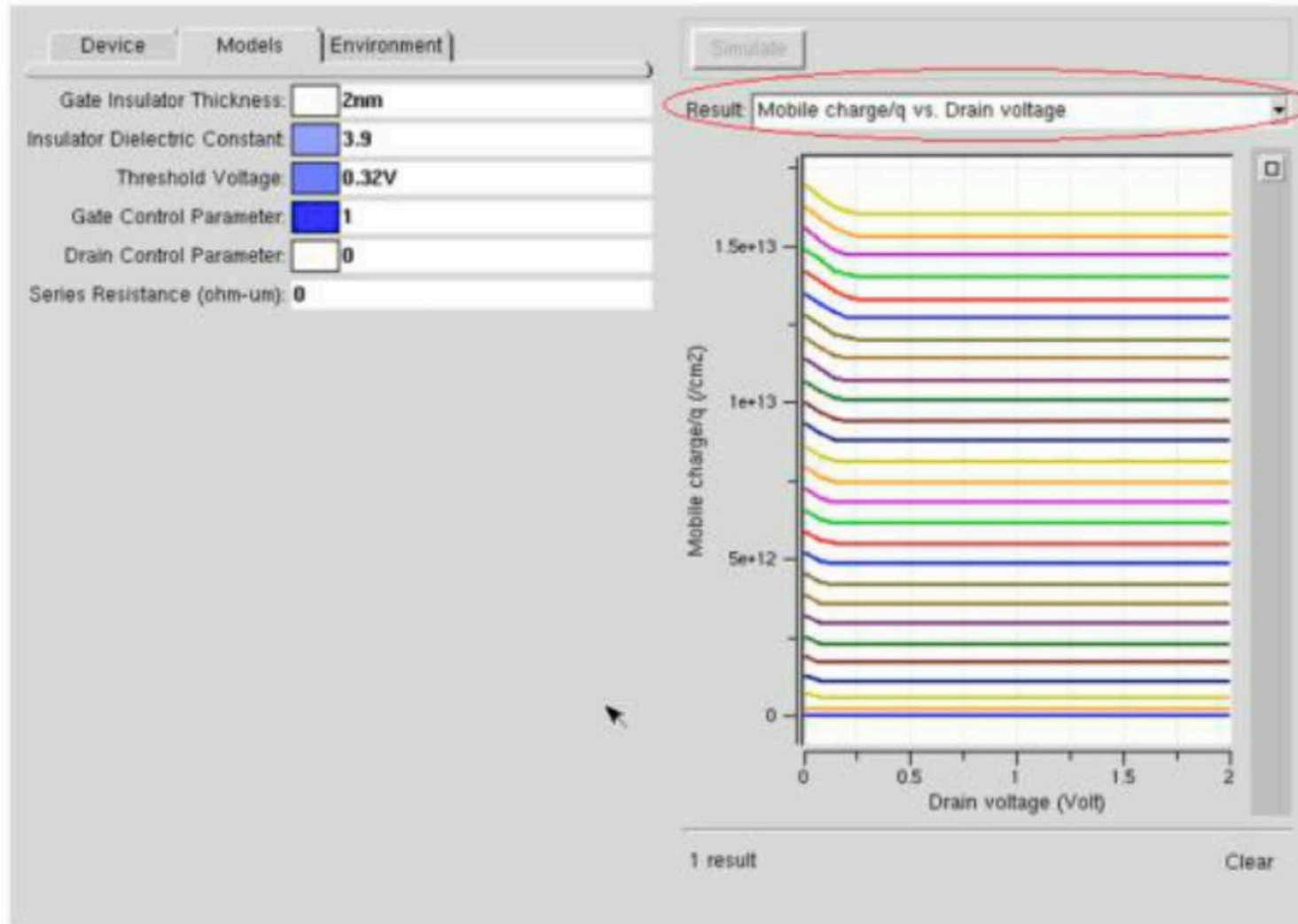
$$\text{slope}_h = 1.54\text{E-}6\text{F/cm}^2 \qquad \text{slope}_l = 1.58\text{E-}6\text{F/cm}^2$$

$$C_Q = 2 * q^2 * m_{\text{eff}} / (\pi * h_{\text{bar}}^2) = 2.54\text{E-}5\text{F/cm}^2$$

$$C_G = C_{OX} C_Q / (C_{OX} + C_Q) = 1.45\text{E-}6\text{F/cm}^2$$

# 6a) 1D Electrostatics: Charge vs. Voltage, 2nm

## Simulation Result:



# 6a) 1D Electrostatics: Charge vs. Voltage, 2nm

---

Explanation for Q not constant as  $V_{DS}$  increases for 1D electrostatic case:

$$N = N_{2D}WL/2[F_0(\eta_{F1}) + F_0(\eta_{F2})]$$

$$\psi_S = C_{OX}/C_{\Sigma} * V_G - q(N-N_0)/C_{\Sigma}$$

independent of  $V_D$

$$\eta_{F1} = (E_{F1} - E_C^{FB} + q\psi_S)/(k_b T)$$

independent of  $V_D$

$$\eta_{F2} = \eta_{F1} - qV_D/(k_b T)$$

dependent on  $V_D$

$$F_j(\eta) \rightarrow e^{\eta} \quad \text{as} \quad \eta \rightarrow -\infty$$

$$F_0(\eta_{F2}) \rightarrow 0 \quad \text{as} \quad \eta_{F2} \rightarrow -\infty$$

$$\eta_{F2} \rightarrow -\infty \quad \text{as} \quad V_D \rightarrow \infty$$

$$N = N_{2D}WL/2[F_0(\eta_{F1})] \quad \text{for } V_D \text{ large} \quad \text{independent of } V_D$$

## 6b) 2D Electrostatics: Charge vs. Voltage, 2nm

---

Gate Control Parameter:

$$S = 100\text{mV/decade}$$

$$\alpha_G = (2.3k_B T/q)/S$$

$$\underline{\alpha_G = 0.595}$$

Drain Control Parameter:

$$\text{DIBL} = 100\text{mV/V}$$

$$\alpha_D = (2.3k_B T * \text{DIBL}) / (q * S)$$

$$\underline{\alpha_D = 0.059}$$

# 6b) 2D Electrostatics: Charge vs. Voltage, 2nm

## Simulation Result:

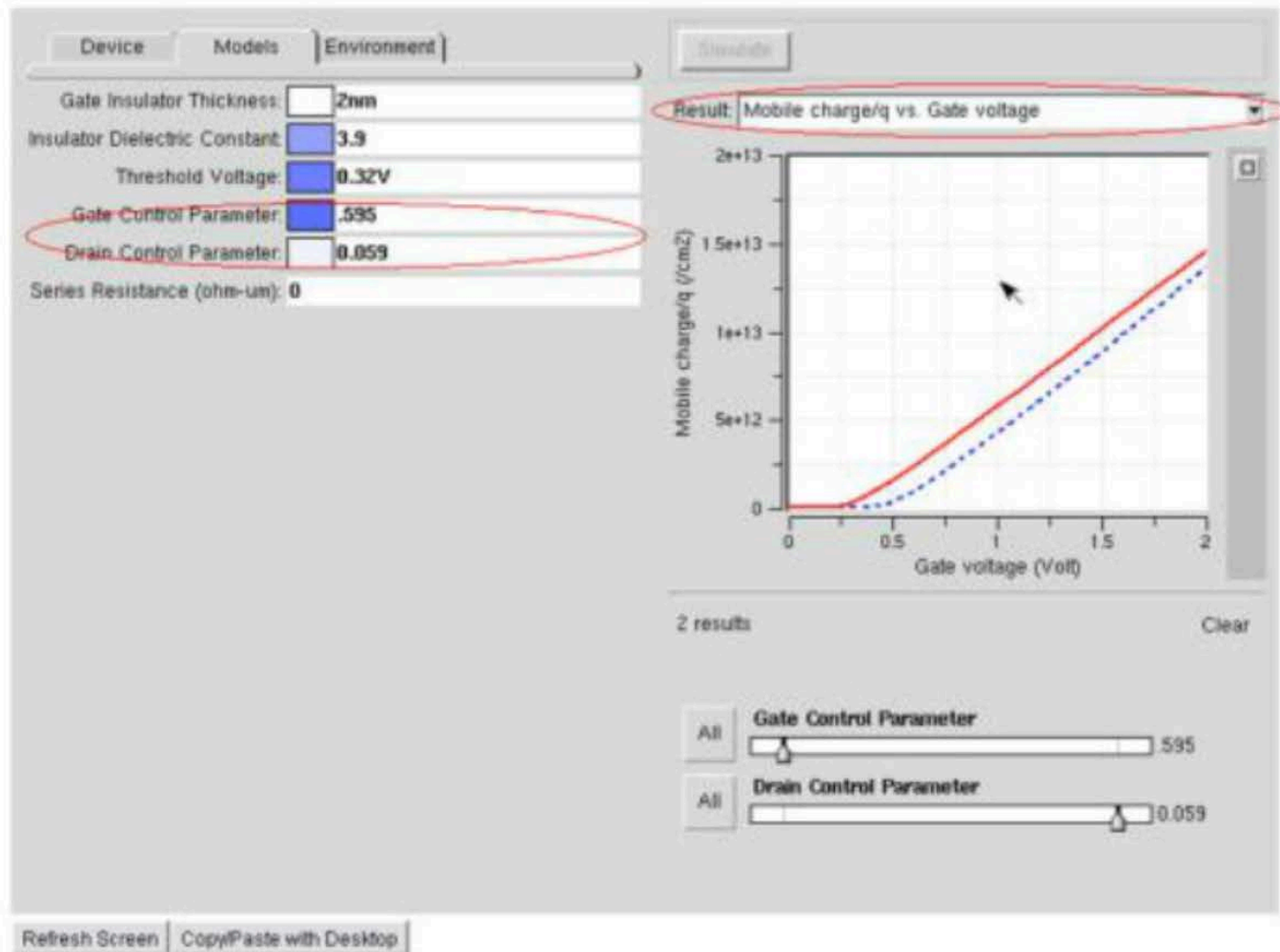
Slope for  $V_{DS} = 2V$ :

$$\text{slope}_h = 1.40E-6F/cm^2$$

$$C_{OX} = 1.73E-6F/cm^2$$

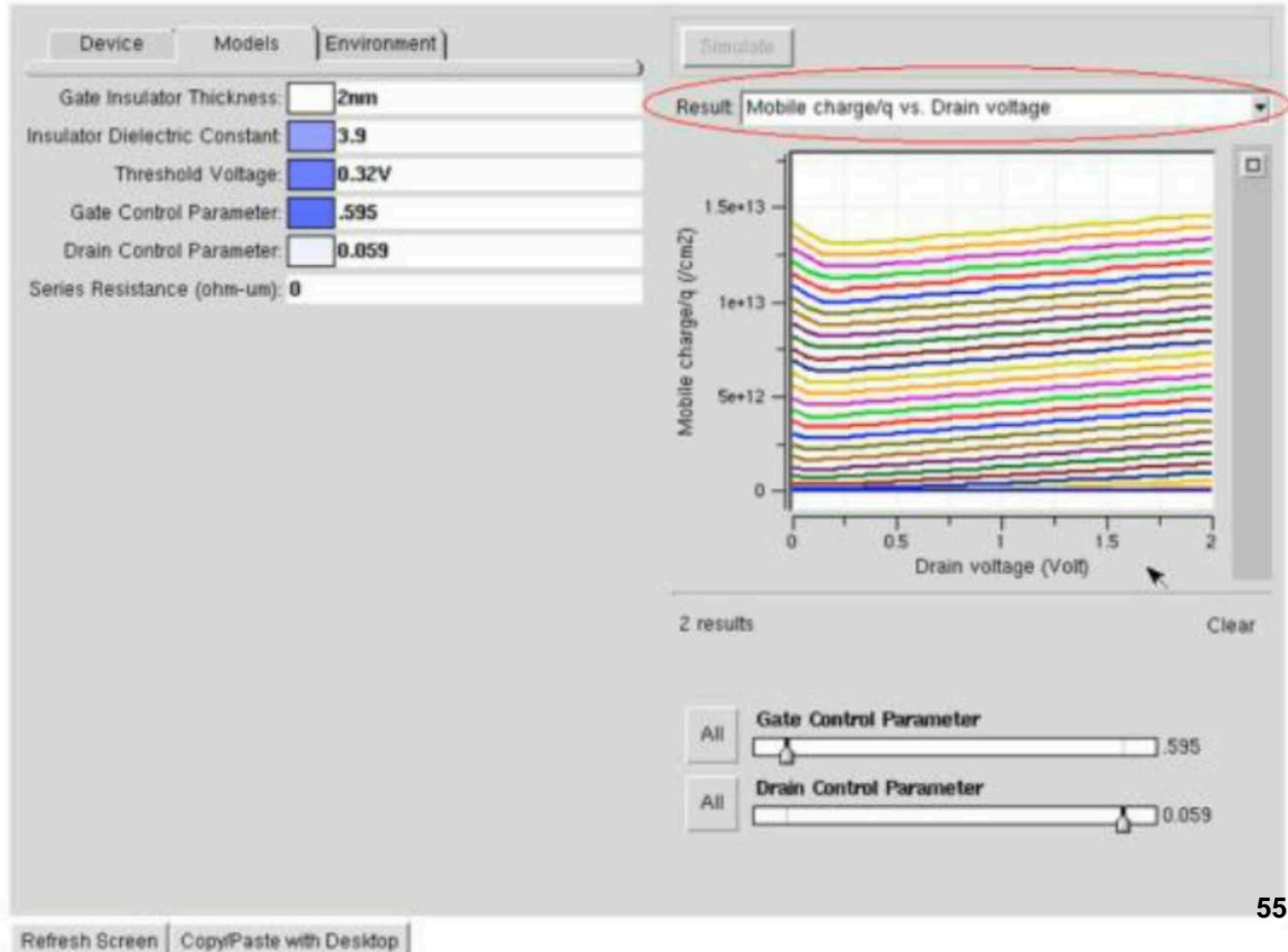
Slope for  $V_{DS} = 0.069V$ :

$$\text{slope}_l = 1.49E-6F/cm^2$$



# 6b) 2D Electrostatics: Charge vs. Voltage, 2nm

## Simulation Result:



# 6c) 1D/2D Electrostatics: Charge vs. Voltage, 0.5nm

## Material Parameters and Settings:

Device | Models | Environment

Model: MOSFET

Single Gate/Double Gate: Single Gate

Transport Effective Mass: 0.19

Valley Degeneracy: 2

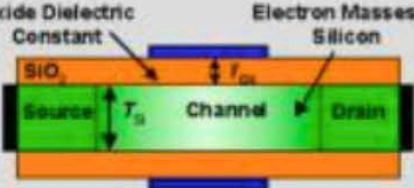
Floating Boundary Flag: no

Body Thickness: 10nm

Source Doping Density:  $1.0e20/cm^3$

Oxide Dielectric Constant

Electron Masses in Silicon



Source Channel Drain

Device | Models | Environment

Gate Insulator Thickness: 4.5nm

Insulator Dielectric Constant: 3.9

Threshold Voltage: 0.32V

Gate Control Parameter: 1

Drain Control Parameter: 0

Series Resistance (ohm-us): 0

Device | Models | Environment

Ambient Temperature: 300K

Initial Gate Voltage: 0V

Final Gate Voltage: 2.0V

Number of Gate Voltage Bias Points: 30

Initial Drain Voltage: 0V

Final Drain Voltage: 2V

Number of Drain Voltage Bias Points: 30



## 6c) 1D/2D Electrostatics: Charge vs. Voltage, .5nm

Simulation Result, 1D Electrostatics:

Slope for  $V_{DS} = 2V$ :

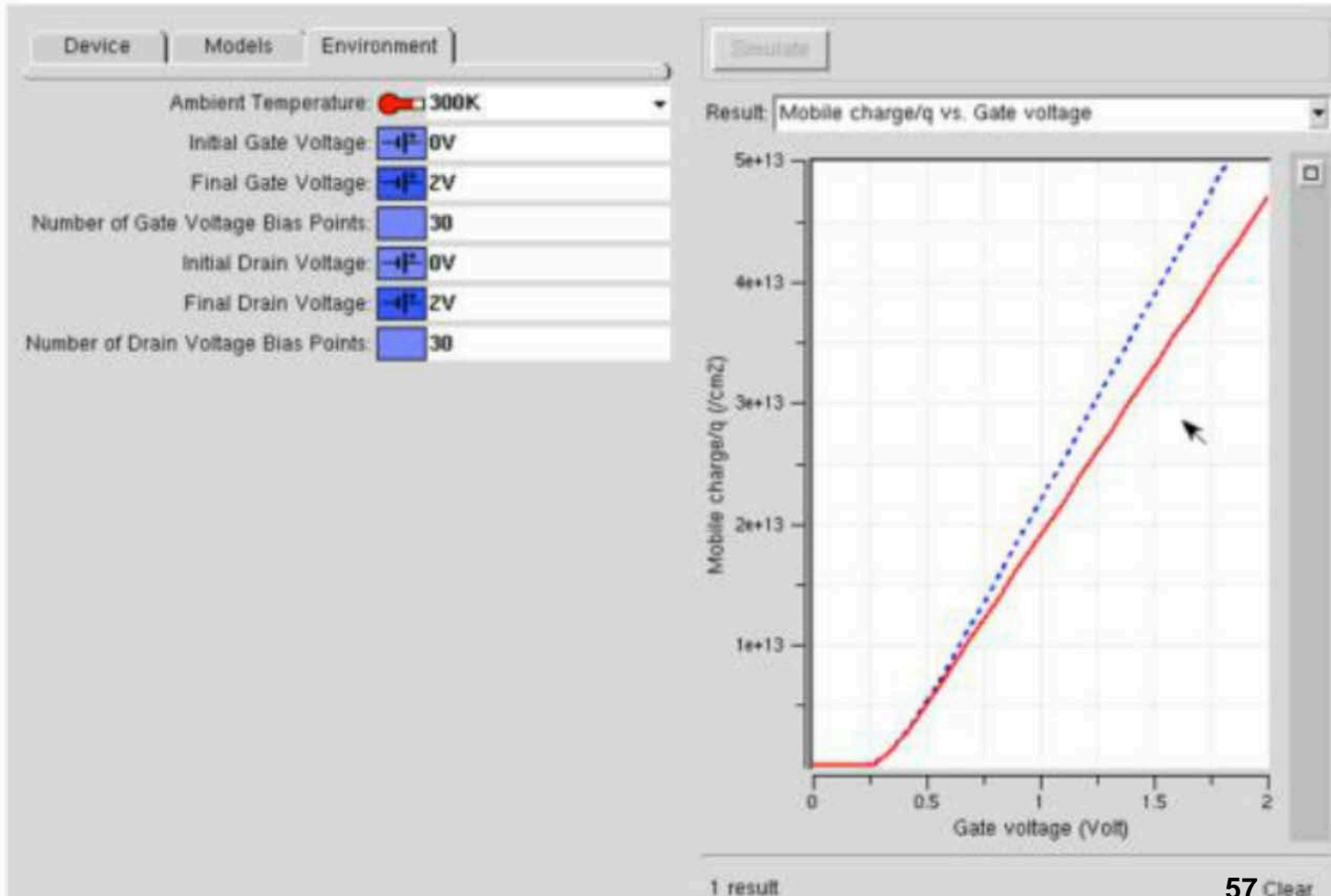
$\text{slope}_h = 4.50E-6F/cm^2$

$C_{OX} = 6.91E-6F/cm^2$

Slope for  $V_{DS} = 0.069V$ :

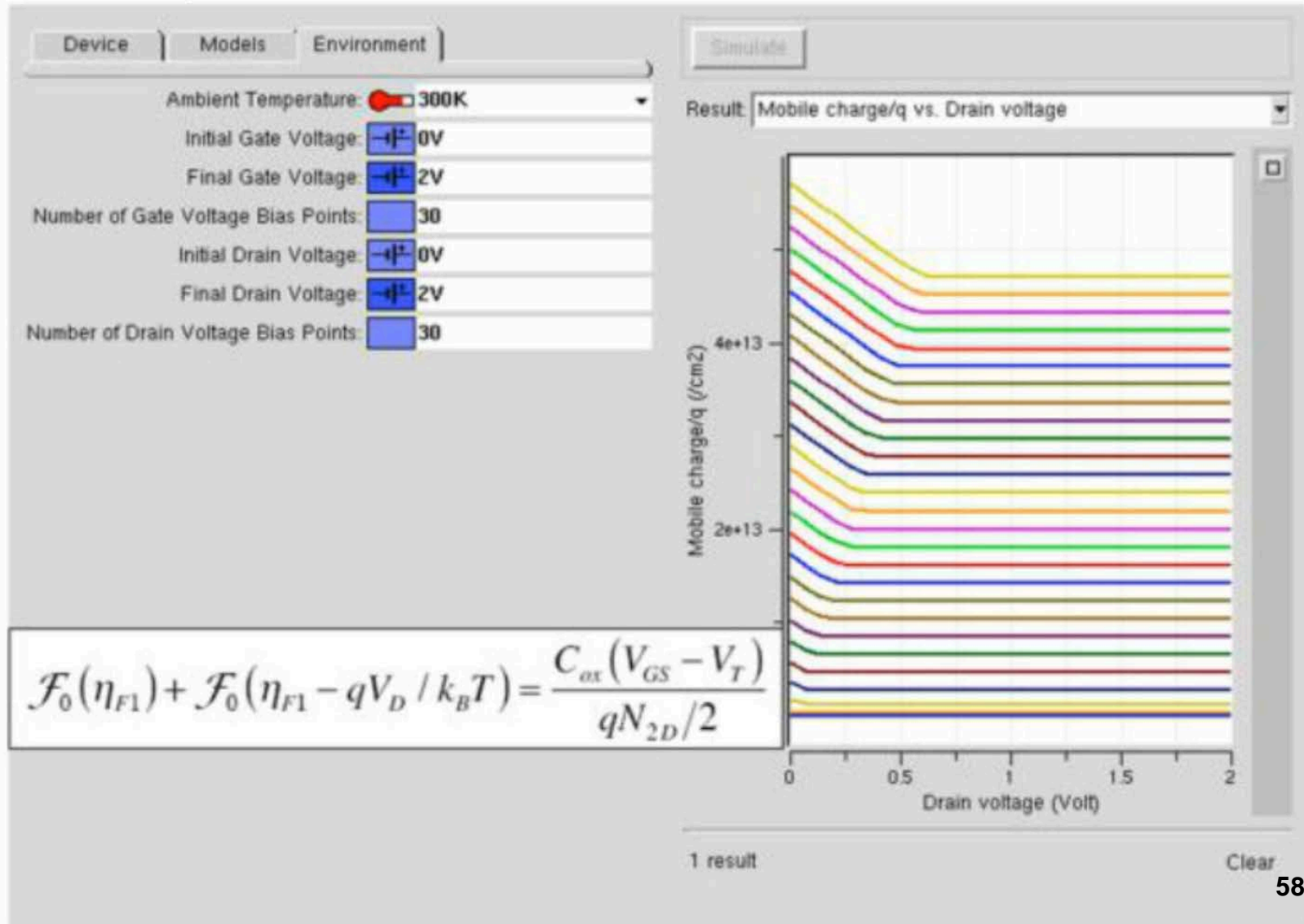
$\text{slope}_l = 5.46E-6F/cm^2$

$C_G = 5.43E-6F/cm^2$



# 6c) 1D/2D Electrostatics: Charge vs. Voltage, .5nm

## Simulation Result, 1D Electrostatics:



# 6c) 1D/2D Electrostatics: Charge vs. Voltage, .5nm

Simulation Result, 2D Electrostatics:

Slope for  $V_{DS} = 2V$ :

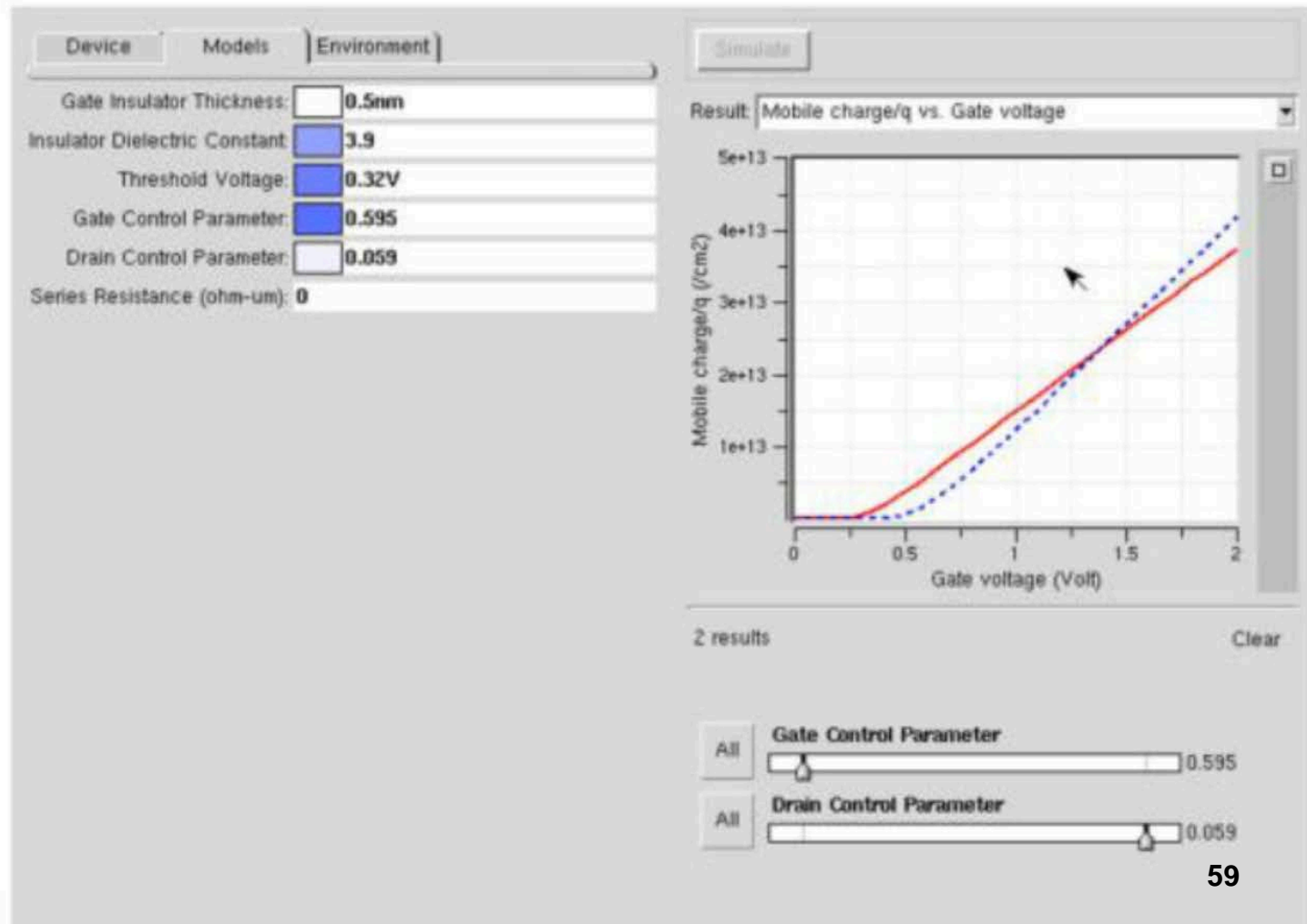
$$\text{slope}_h = 3.62E-6F/cm^2$$

$$C_{OX} = 6.91E-6F/cm^2$$

Slope for  $V_{DS} = 0.069V$ :

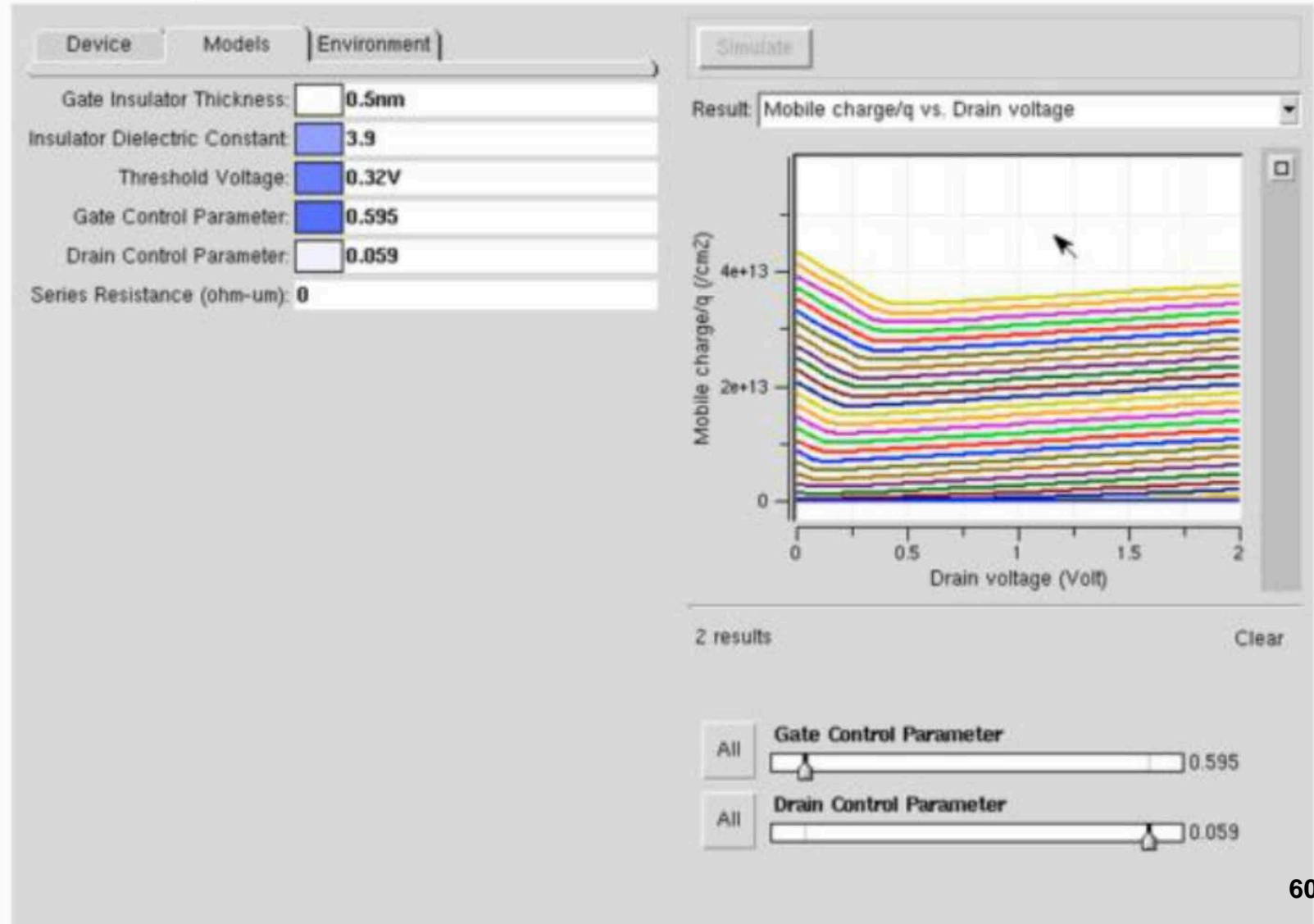
$$\text{slope}_l = 4.70E-6F/cm^2$$

$$C_G = 5.43E-6F/cm^2$$



# 6c) 1D/2D Electrostatics: Charge vs. Voltage, .5nm

## Simulation Result, 2D Electrostatics:



# Problem 7

---

*Nanowire transistors are getting a lot of attention these days. They seem to operate more nearly as SB FETs than as MOSFETs, but it's interesting so see what might happen if Nanowire MOSFETs can be realized. The exercise below will get you calibrated on silicon Nanowire MOSFETs.*

7) Examine the  $I$ - $V$  characteristics of a hypothetical silicon nanowire MOSFET. Assume  $D = 1\text{nm}$  and that the insulator is  $2\text{ nm}$  of  $\text{SiO}_2$  and that  $V_{DD} = 0.5\text{V}$ . Use an approximate threshold voltage of  $V_T = 0.2\text{V}$  and assume room temperature operation.

- a) Compute  $I_D$  vs.  $V_{DS}$  at  $T = 300\text{K}$  and compare the low- $V_{DS}$  drain conductance,  $G_D$  with the quantum conductance,  $4e^2/h$ .
- b) Repeat problem i) but at  $T = 77\text{K}$ . The channel conductance vs.  $V_{GS}$  is strikingly different than a conventional MOSFET. Explain how.
- c) The on-current can be written as  $I_D = CG\langle v(0)\rangle(V_{GS} - V_T)$ . Deduce  $CG$ ,  $\langle v(0)\rangle$ , and  $V_T$ .

Acknowledgement: The problem is provided by Prof. Mark Lundstrom, Purdue University

# 7a) Silicon Nanowire FET at 300K

## Material Parameters and Settings:

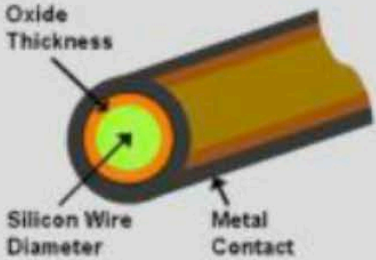
Device | Models | Environment

Model: Silicon Nanowire FET

NW Diameter: 1.0nm

Transport Effective Mass: 0.19

Valley Degeneracy: 2



Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Gate Insulator Thickness: 2nm

Insulator Dielectric Constant: 3.9

Threshold Voltage: 0.2V

Gate Control Parameter: 1

Drain Control Parameter: 0

Series Resistance (ohm-um): 0

Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Ambient Temperature: 300K

Initial Gate Voltage: -0.6V

Final Gate Voltage: -0.5V

Number of Gate Voltage Bias Points: 2

Initial Drain Voltage: -0.6V

Final Drain Voltage: -0.5V

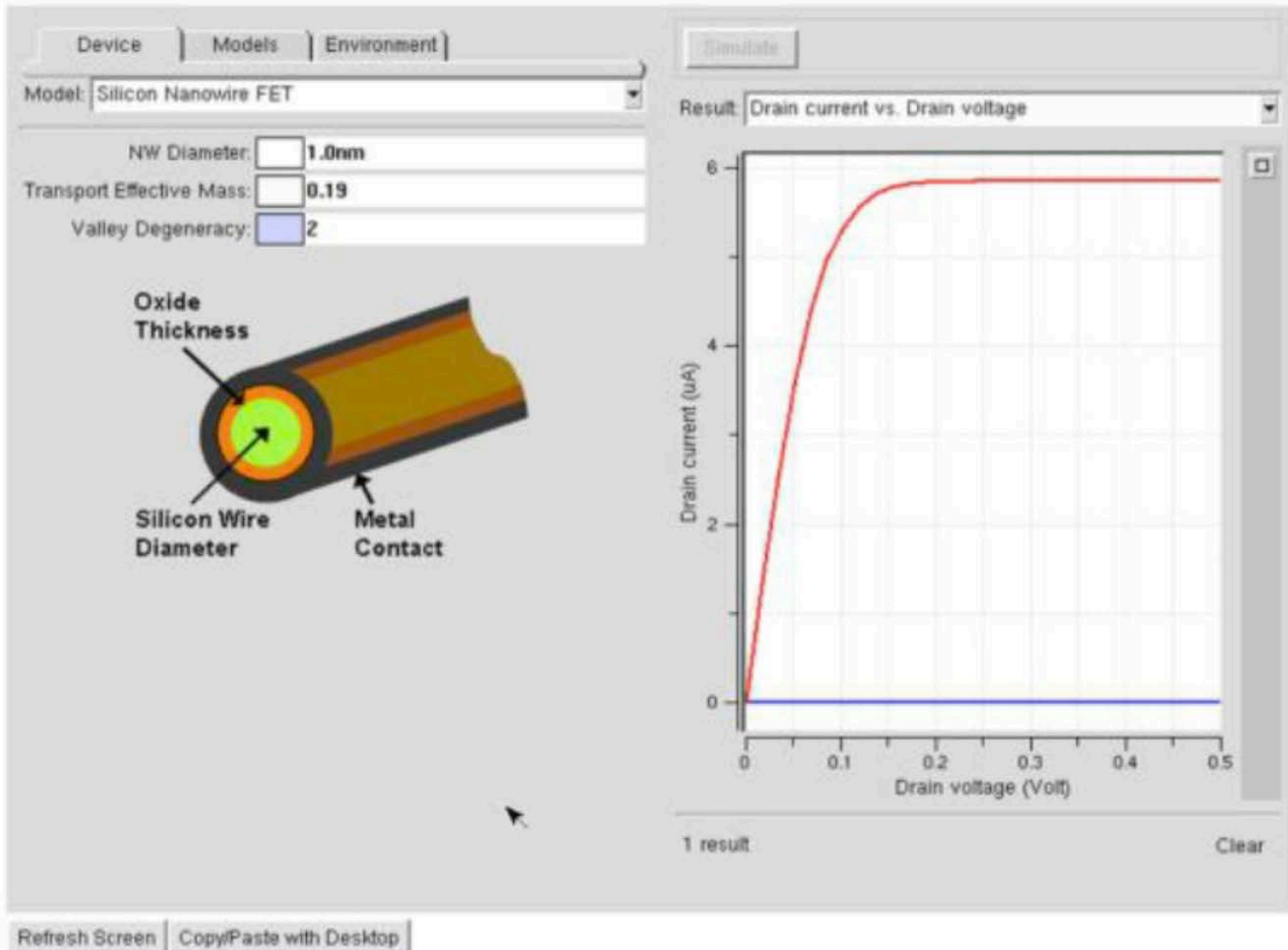
Number of Drain Voltage Bias Points: 30

Refresh Screen | Copy/Paste with Desktop



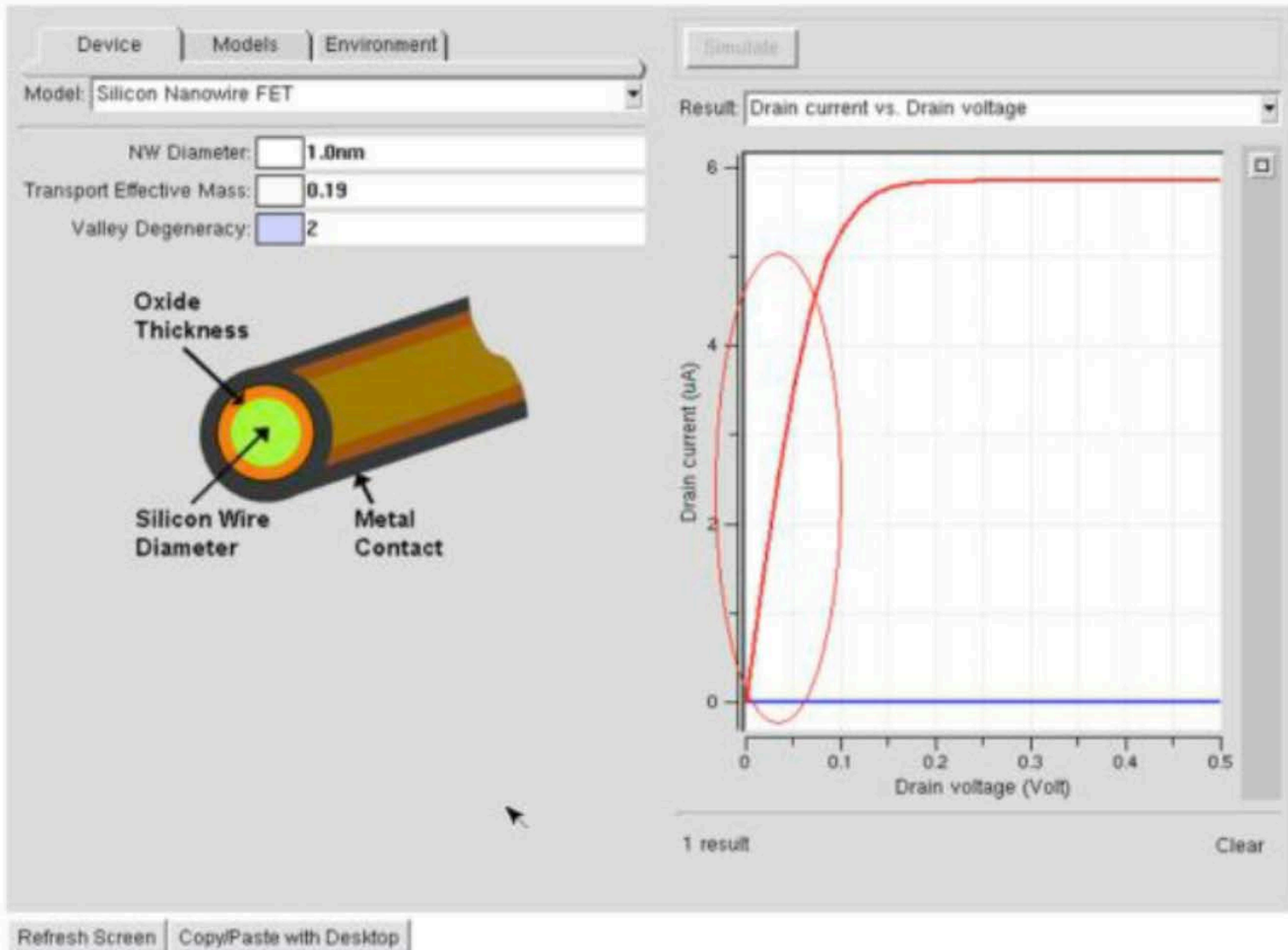
# 7a) Silicon Nanowire FET at 300K

## Simulation Result:



# 7a) Silicon Nanowire FET at 300K

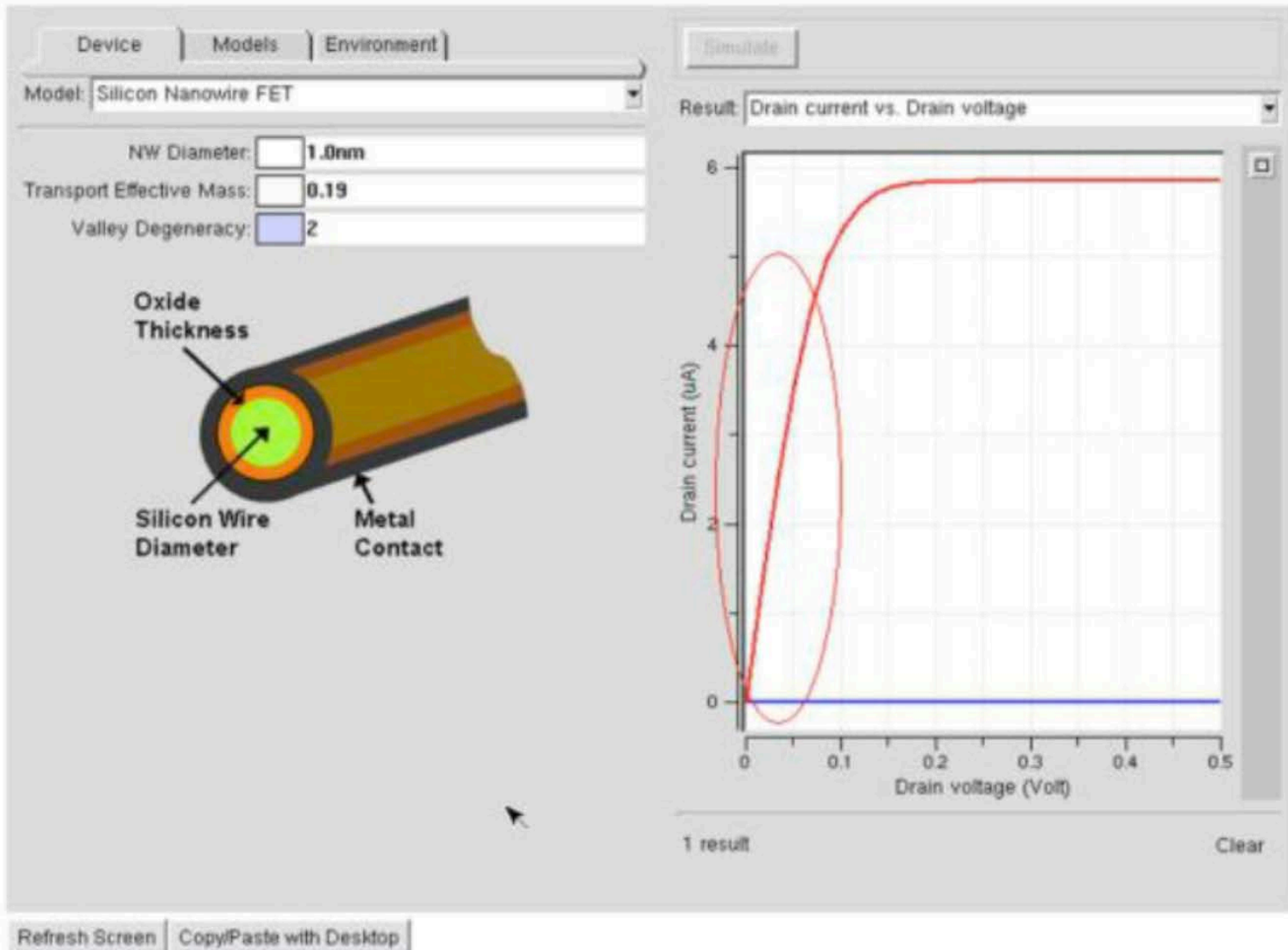
Simulation Result:  $G_D = 5.89E-5$ siemens for  $V_G = 0.5V$





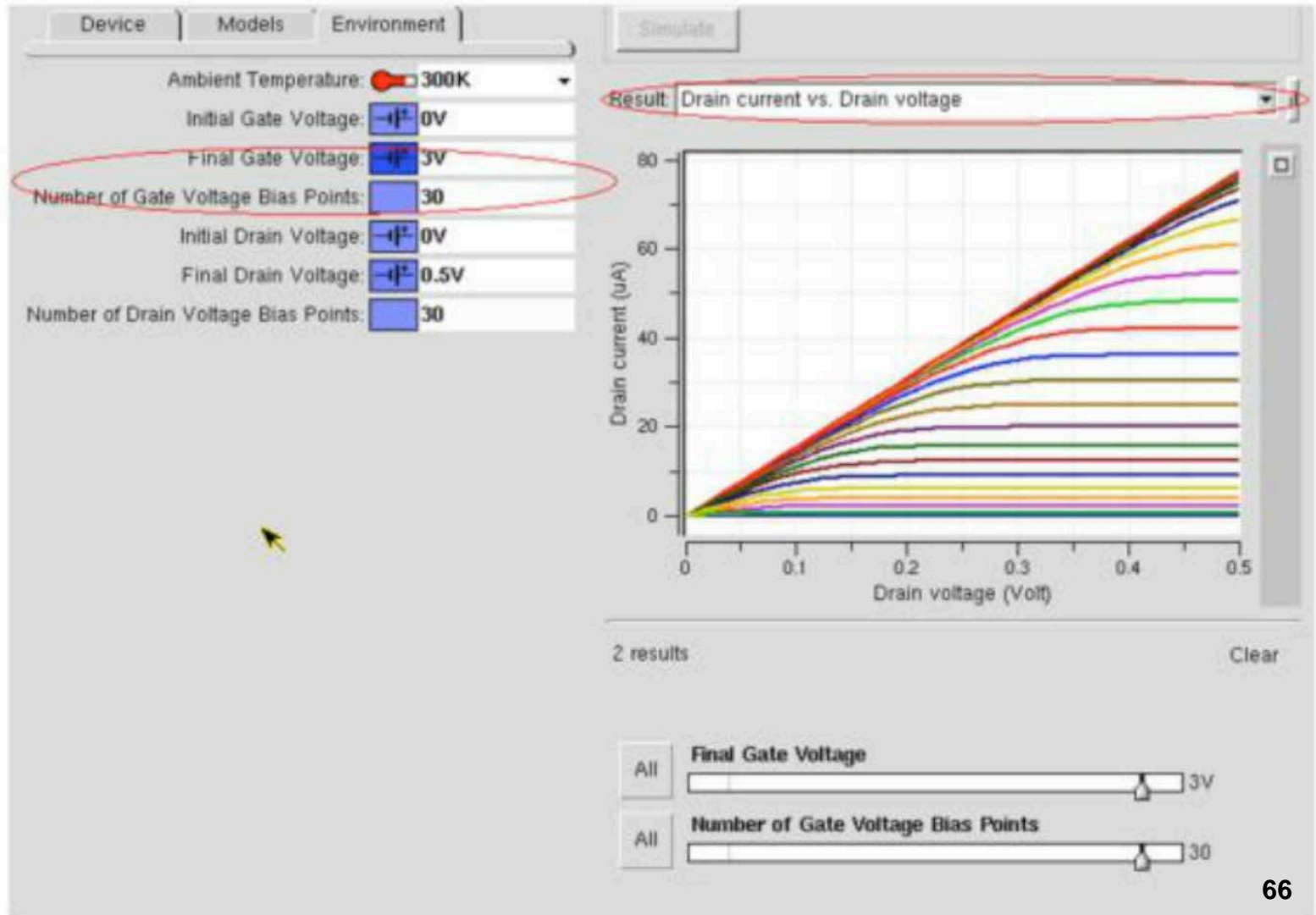
# 7a) Silicon Nanowire FET at 300K

Simulation Result:  $G_D = 5.89E-5$ siemens for  $V_G = 0.5V$   $G_Q = 1.55E-4$ siemens



# 7a) Silicon Nanowire FET at 300K

Simulation Results:  $G_D = 1.55E-4$ siemens at  $V_G > 1.5V$   $G_Q = 1.55E-4$ siemens



# 7b) Silicon Nanowire FET at 77K

## Material Parameters and Settings:

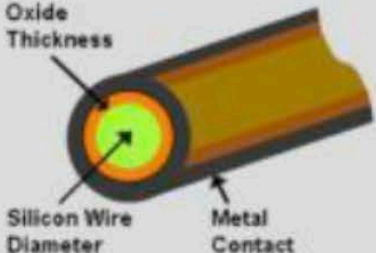
Device | Models | Environment

Model: Silicon Nanowire FET

NW Diameter: 1.0nm

Transport Effective Mass: 0.19

Valley Degeneracy: 2



Oxide Thickness

Silicon Wire Diameter

Metal Contact

Refresh Screen CopyPaste with Desktop

Device | Models | Environment

Gate Insulator Thickness: 2nm

Insulator Dielectric Constant: 3.9

Threshold Voltage: 0.2V

Gate Control Parameter: 1

Drain Control Parameter: 0

Series Resistance (ohm-um): 0

Refresh Screen CopyPaste with Desktop

Device | Models | Environment

Ambient Temperature: 77K

Initial Gate Voltage: -0.6V

Final Gate Voltage: -0.5V

Number of Gate Voltage Bias Points: 2

Initial Drain Voltage: -0.6V

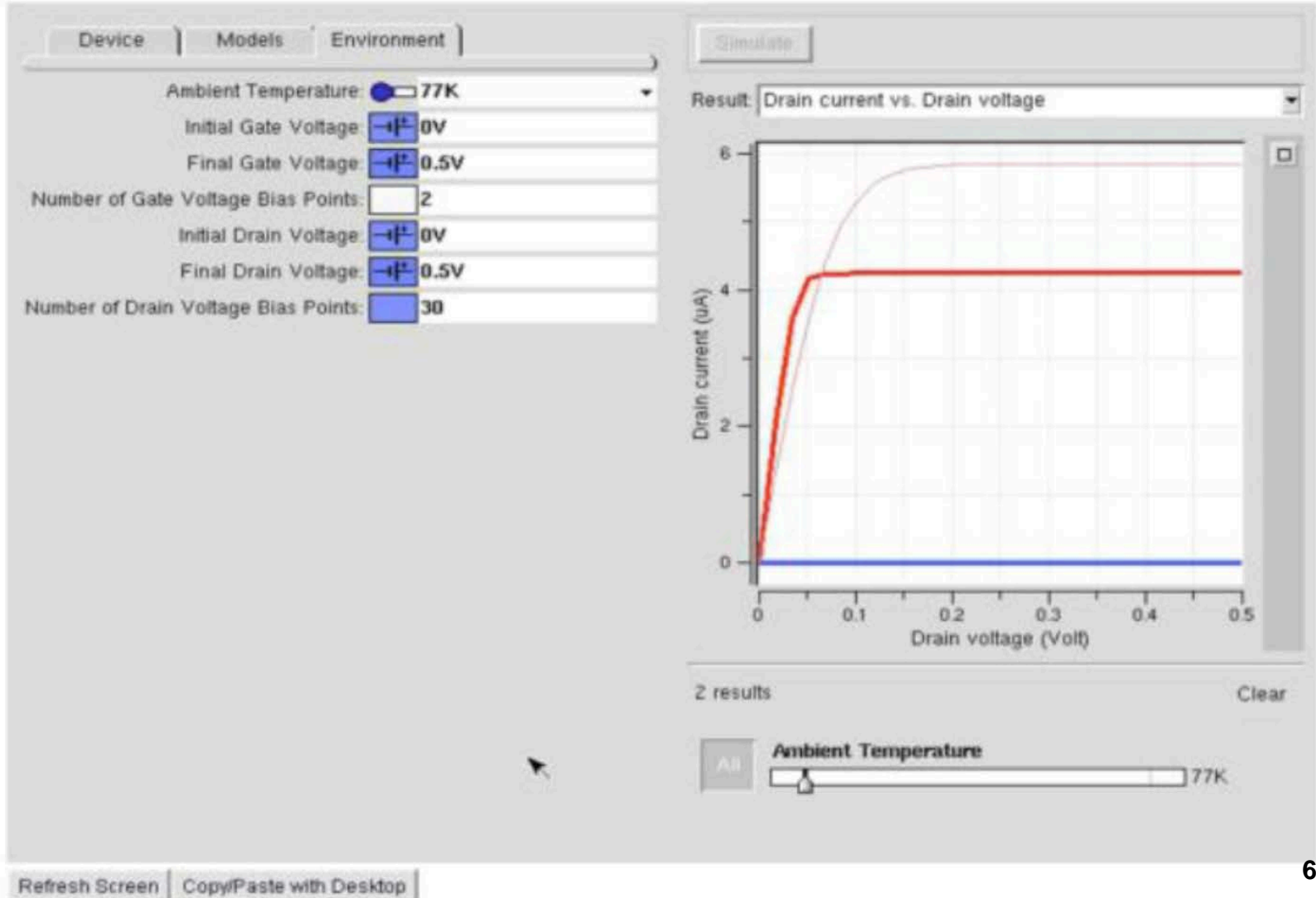
Final Drain Voltage: -0.5V

Number of Drain Voltage Bias Points: 30

Refresh Screen CopyPaste with Desktop

# 7b) Silicon Nanowire FET at 77K

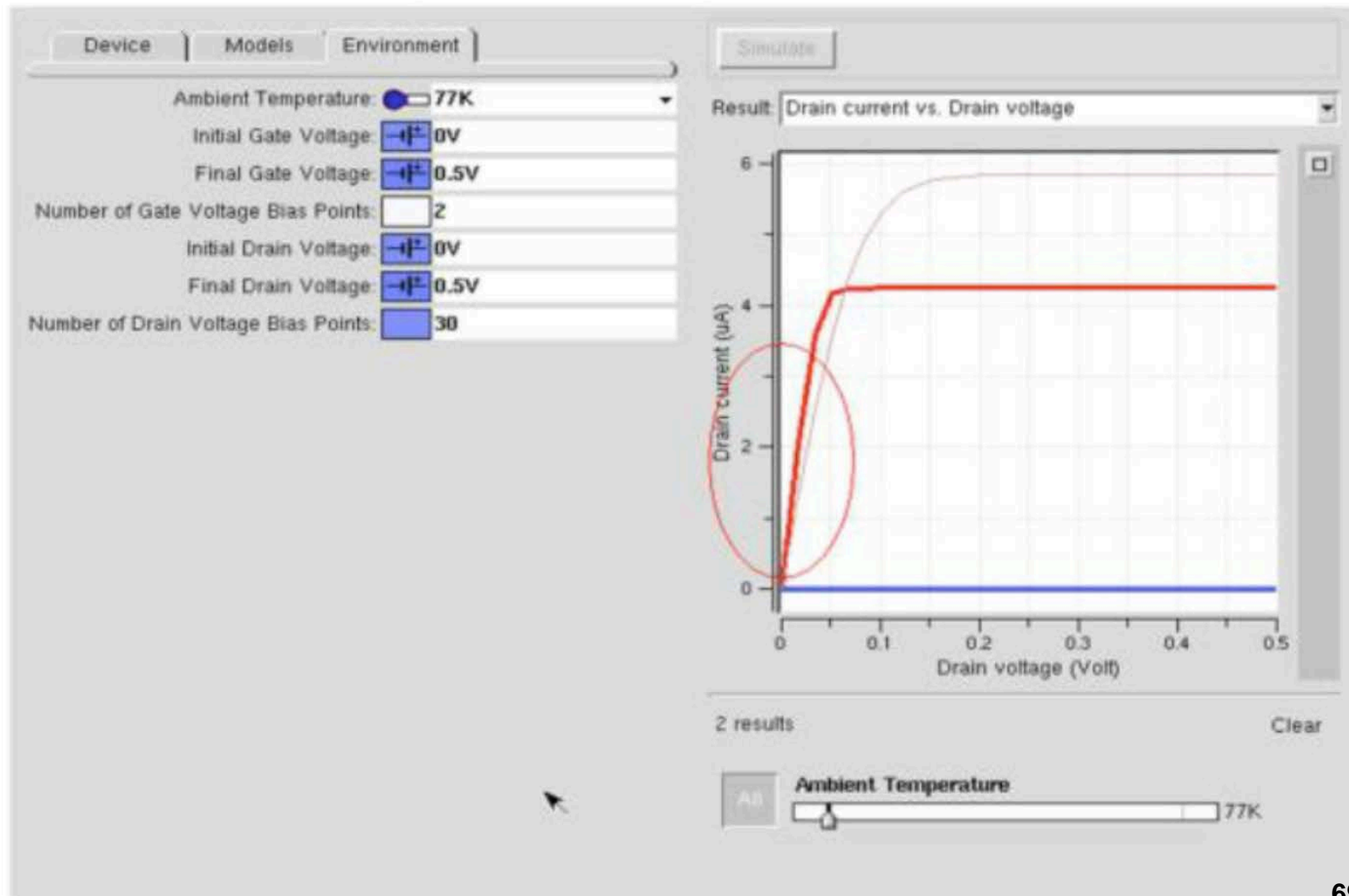
## Simulation Result:



# 7b) Silicon Nanowire FET at 77K

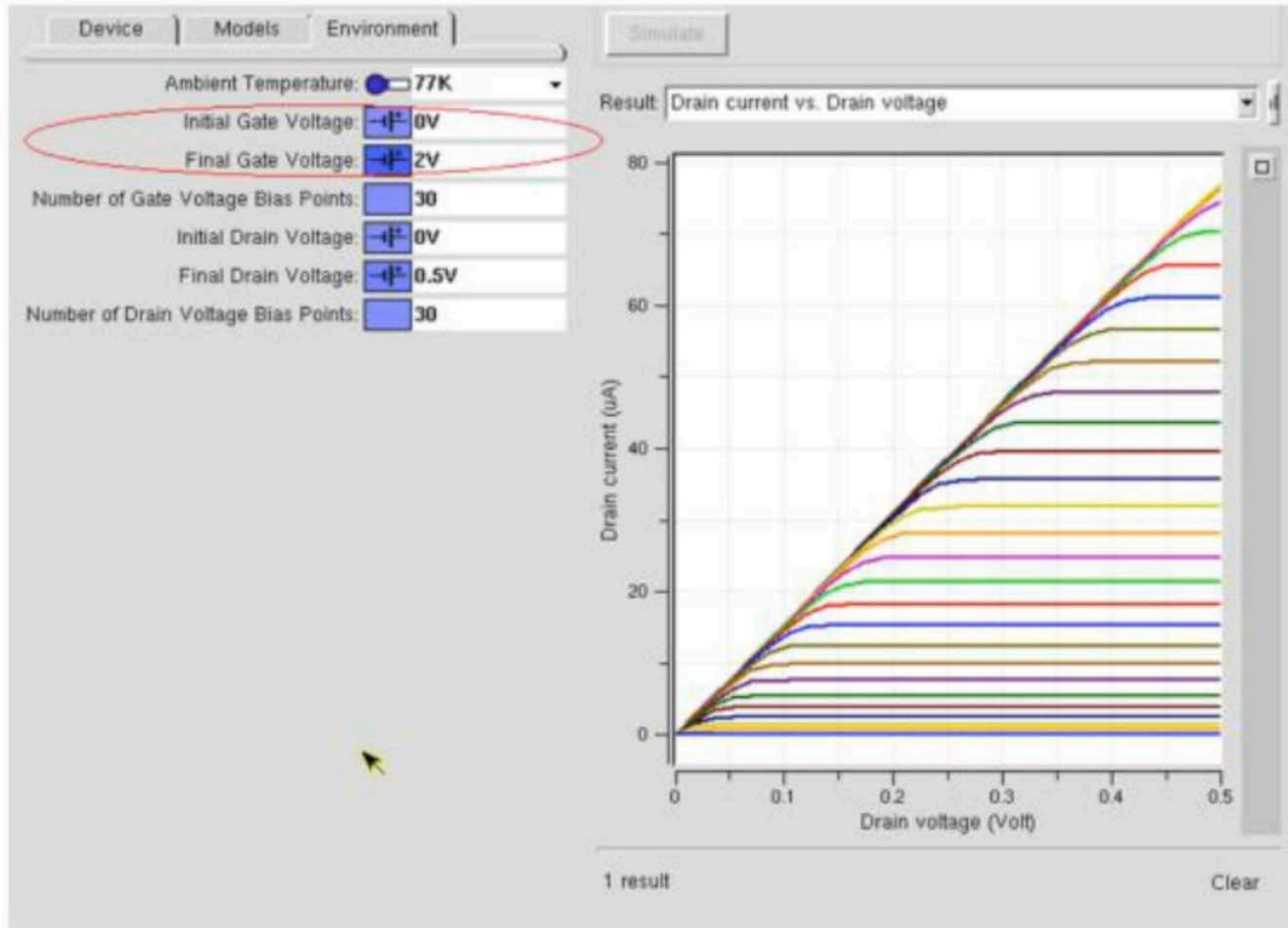
Simulation Result:  $G_D = 8.84E-5$ siemens at  $V_G = 0.5V$

$G_Q = 1.55E-4$ siemens



# 7b) Silicon Nanowire FET at 77K

Simulation Results:  $G_D = 1.55E-4$ siemens at  $V_G > .1V$   $G_Q = 1.55E-4$ siemens



## 7b) Silicon Nanowire FET at 77K

---

Comparison of conventional MOSFET to Nanowire: Conductance vs. VGS

**MOSFET:**

As VG increases GC increases linearly:

$$G_C = M \cdot \frac{2 \cdot q^2}{h}$$

**Nanowire FET:**

As VG increases GC increases in quantized steps

# 7c) Deducing Components of $I_{ON}$

## Material Parameters and Settings:

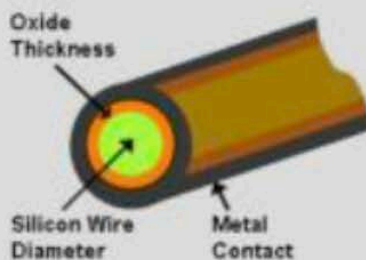
Device | Models | Environment

Model: Silicon Nanowire FET

NW Diameter: 1.0nm

Transport Effective Mass: 0.19

Valley Degeneracy: 2



Oxide Thickness

Silicon Wire Diameter

Metal Contact

Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Gate Insulator Thickness: 2nm

Insulator Dielectric Constant: 3.9

Threshold Voltage: 0.2V

Gate Control Parameter: 1

Drain Control Parameter: 0

Series Resistance (ohm-um): 0

Refresh Screen | Copy/Paste with Desktop

Device | Models | Environment

Ambient Temperature: 300K

Initial Gate Voltage: 0V

Final Gate Voltage: 0.5V

Number of Gate Voltage Bias Points: 30

Initial Drain Voltage: 0V

Final Drain Voltage: 0.5V

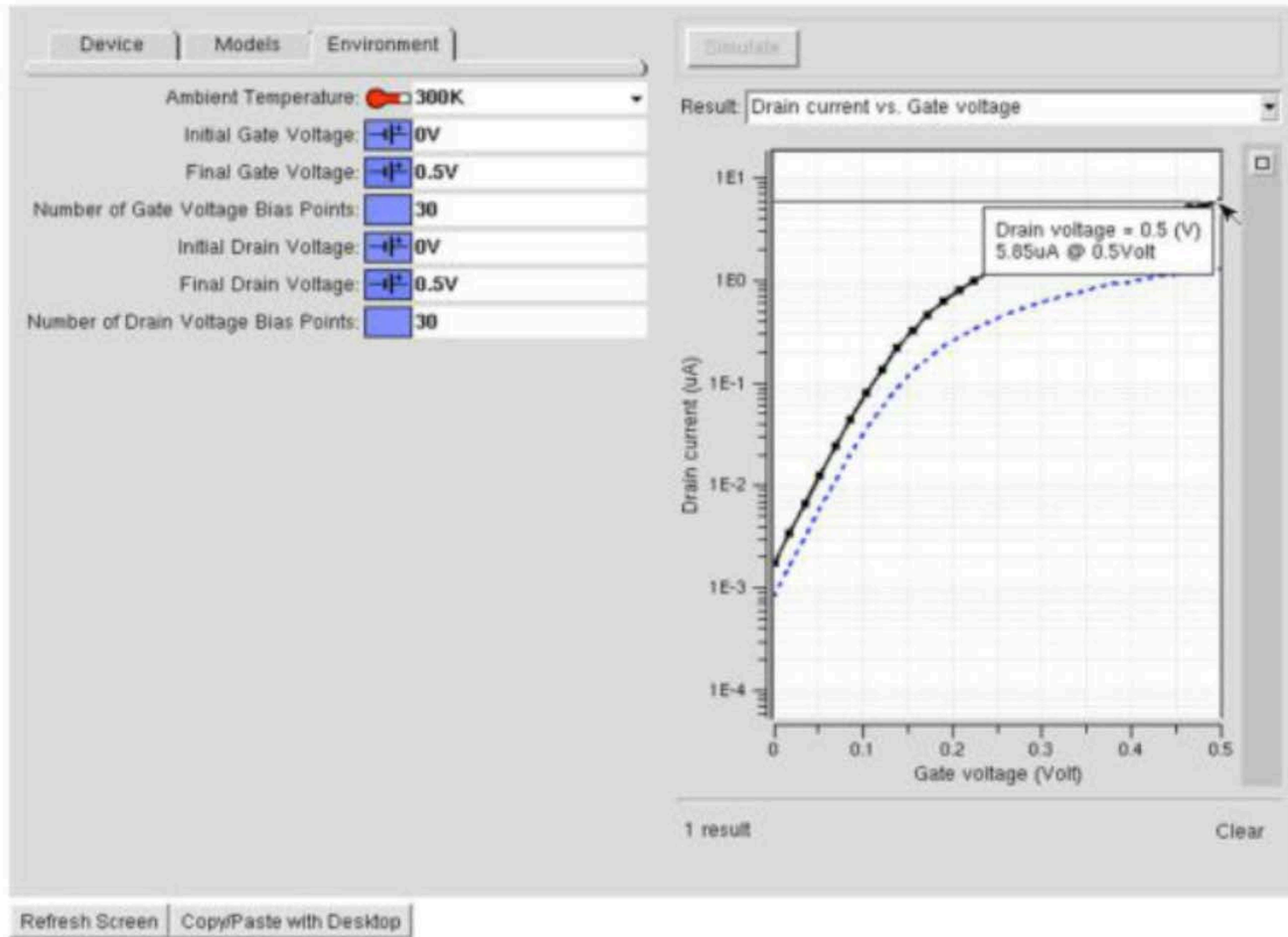
Number of Drain Voltage Bias Points: 30

Refresh Screen | Copy/Paste with Desktop



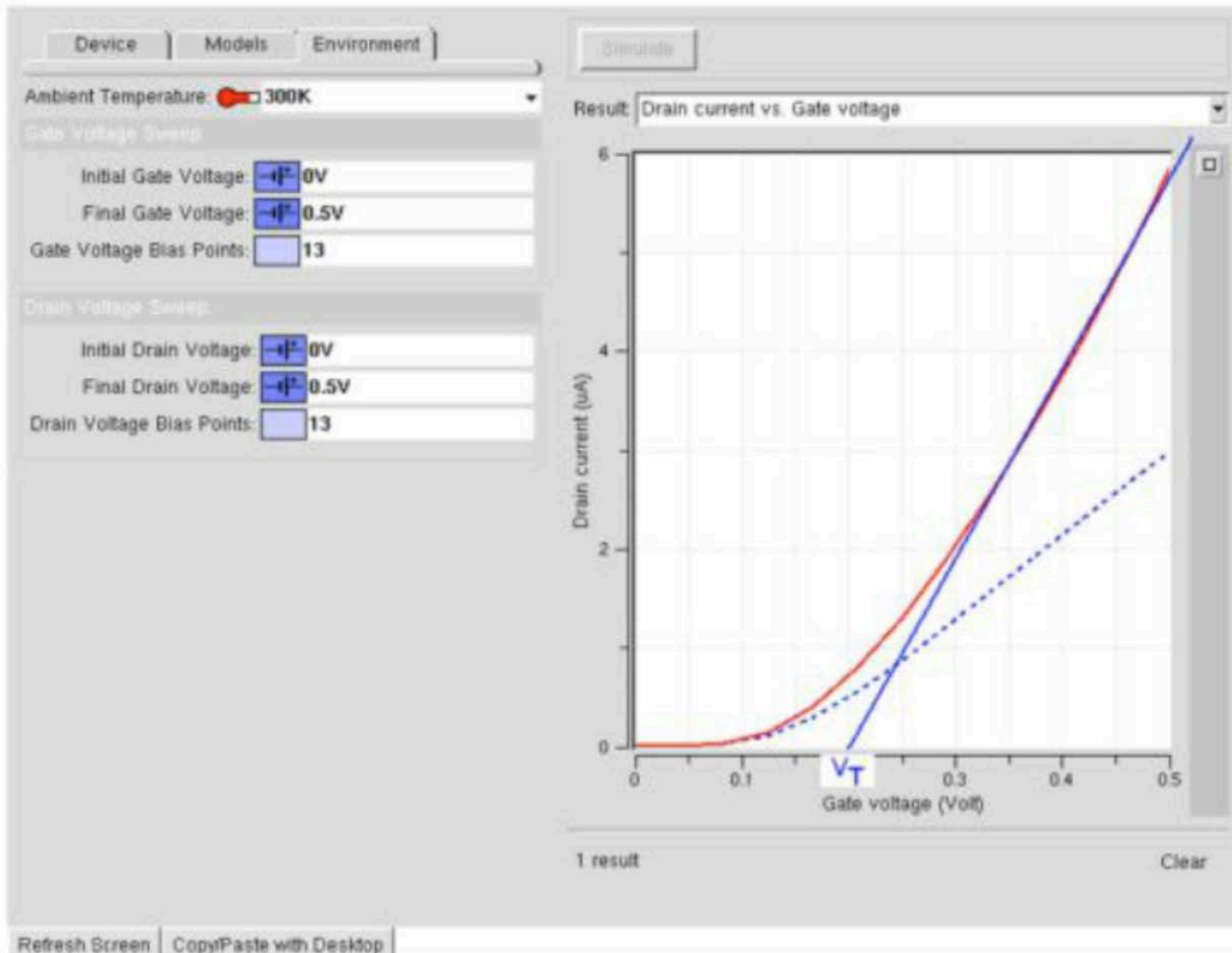
# 7c) Deducing Components of $I_{ON}$

Simulation Result:  $I_{ON} = 5.85\mu A$



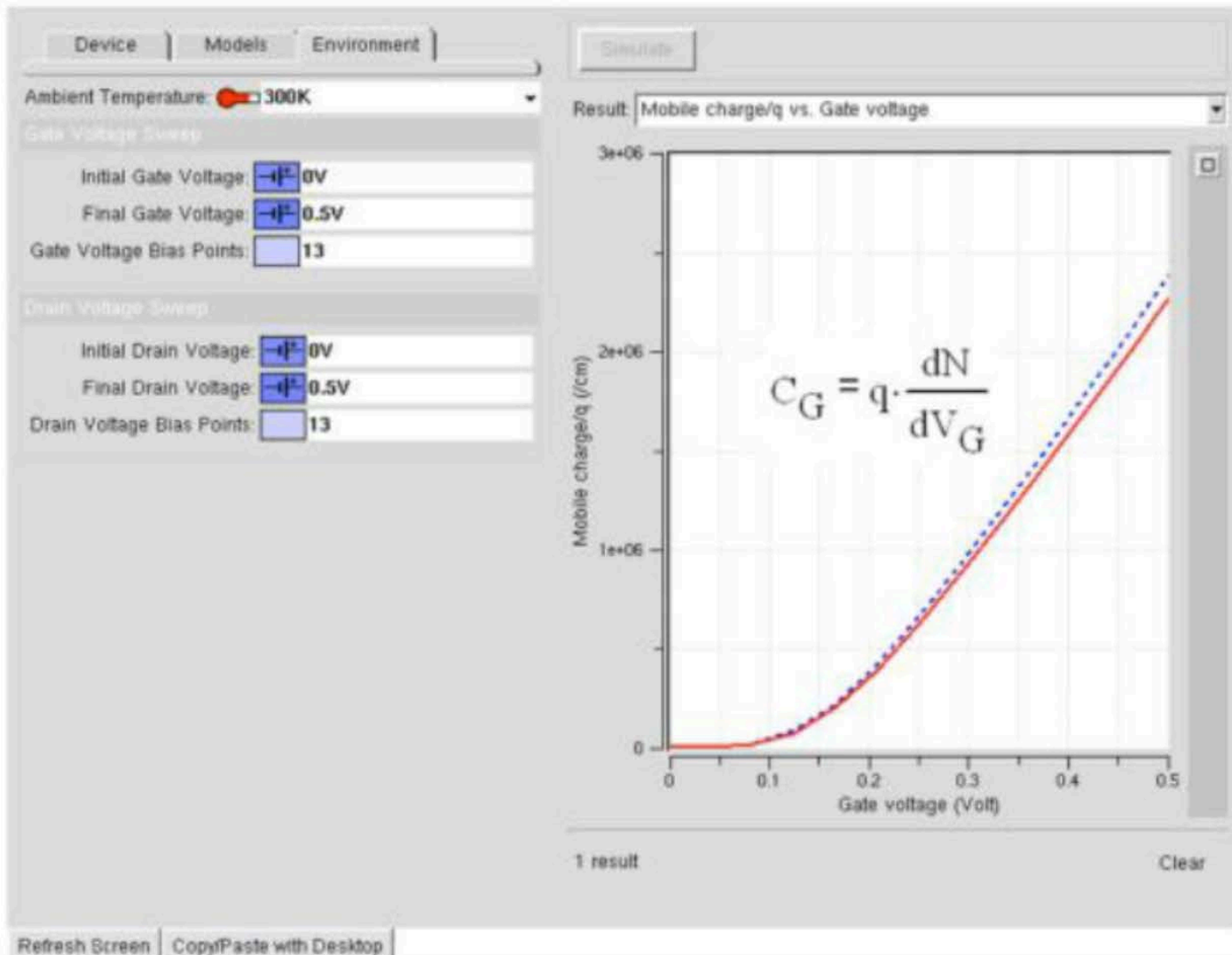
# 7c) Deducing Components of $I_{ON}$

Simulation Result:  $V_T = 0.2V$



# 7c) Deducing Components of $I_{ON}$

Simulation Result:  $C_G = 1.09E-12F/cm$



## 7c) Deducing Components of $I_{ON}$

---

$$\langle v(0) \rangle = \frac{I_{ON}}{C_G(V_G - V_T)}$$

$$\langle v(0) \rangle = 6.71E6 \frac{\text{cm}}{\text{s}}$$