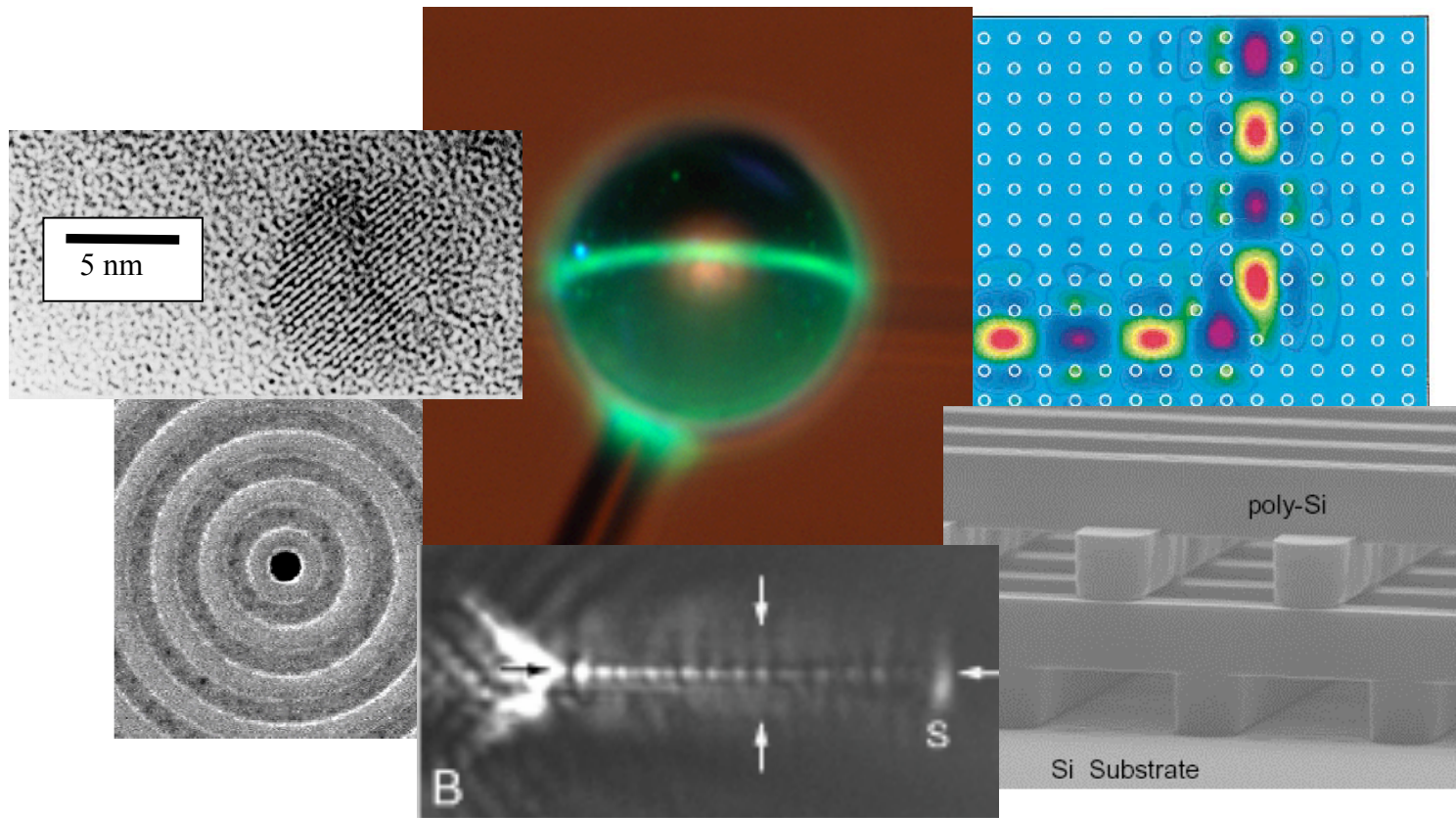


# Lecture 11: Guiding Light Along Nanoparticle Arrays



## What happened at the last Lecture

### Coupling light to surface plasmon-polaritons

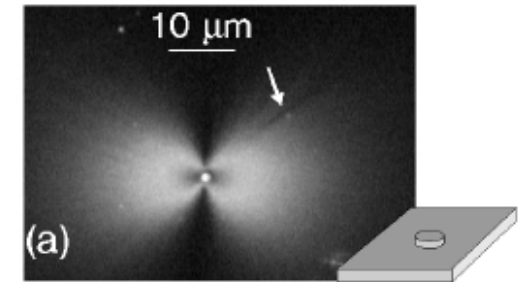
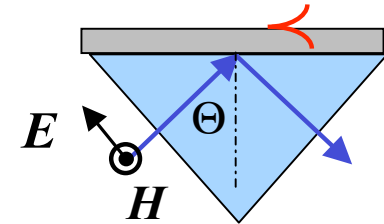
- Kretchman geometry

$$k_{//, \text{SiO}_2} = \sqrt{\epsilon_d} \frac{\omega}{c} \sin \theta = k_{sp}$$

- Grating coupling

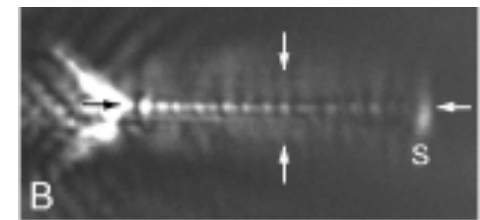
$$k_{//, \text{Air}} = k_{sp} \pm mG$$

- Coupling from a metal dot



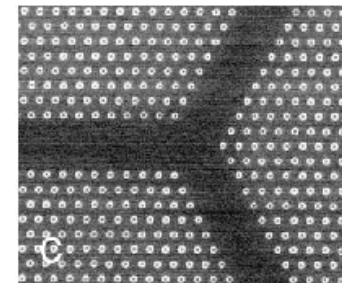
### Guiding geometries

- Stripes and wires



- Line defects in hexagonal arrays (2d photonic crystals)

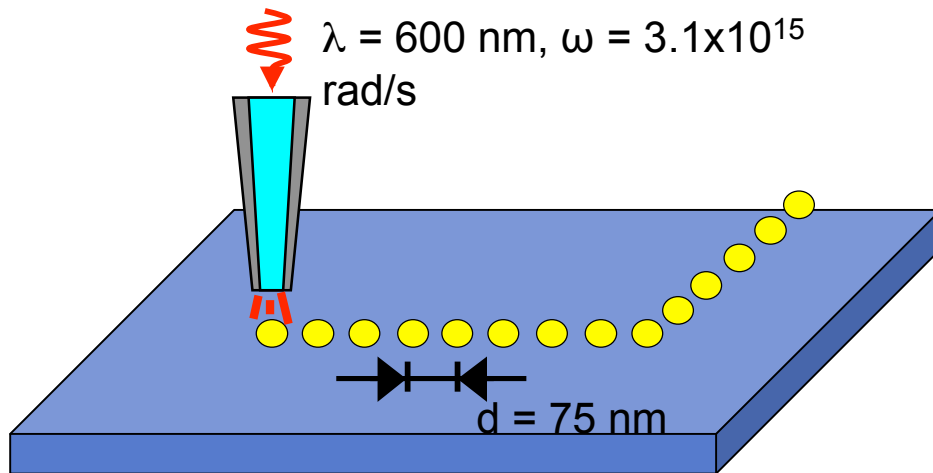
- Today: nanoparticle arrays



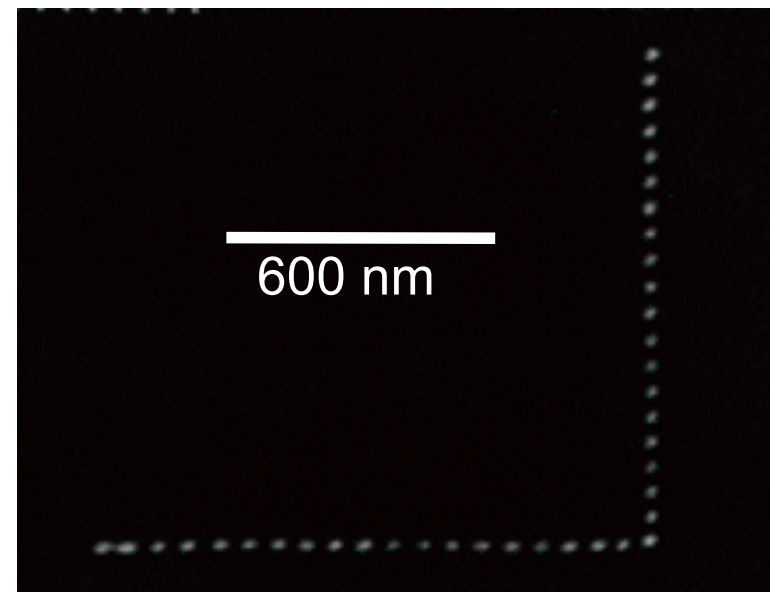
---

## Guiding of light along an array of Au nanoparticles ?

- Near field optical excitation



- SEM of array of 50 nm Au particles

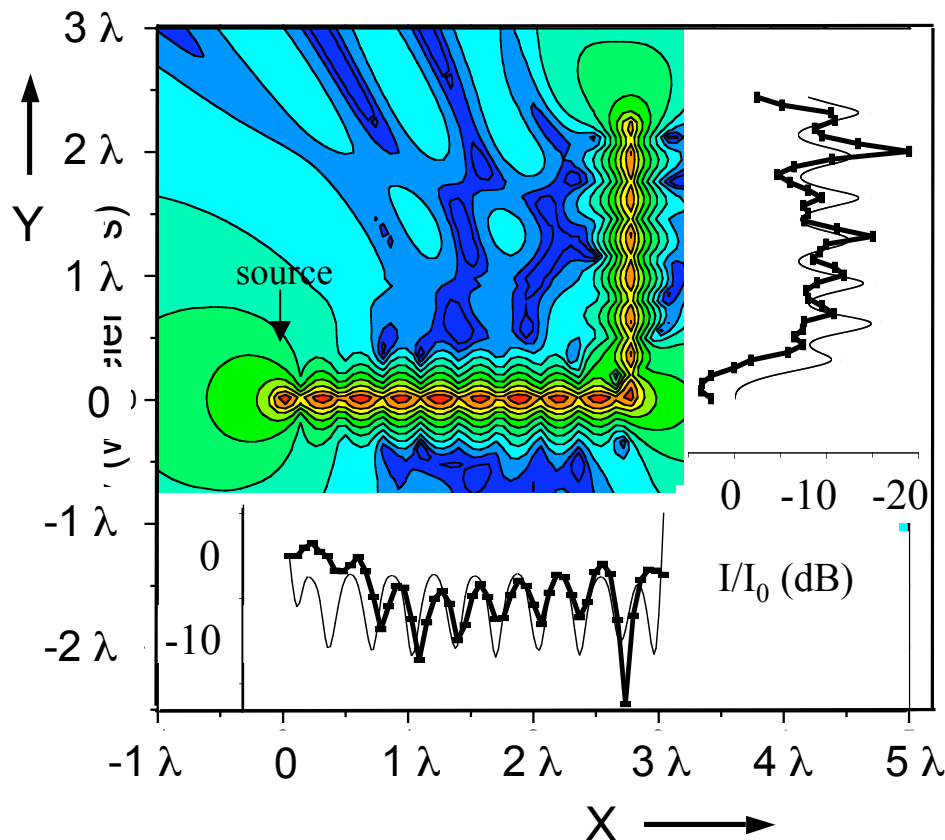


- Light and microwaves are electromagnetic waves described by Maxwell's equations

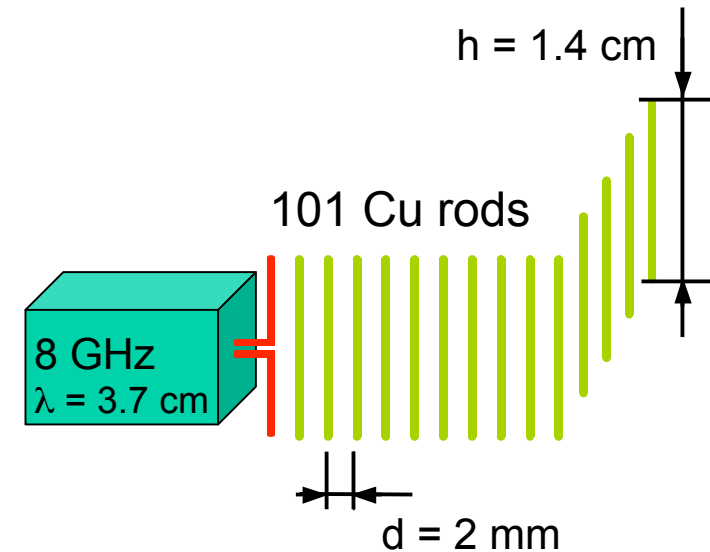
*S.A. Maier, M.L. Brongersma H.A. Atwater, Appl. Phys. Lett. 78, 16, 2001*

# A cm-scale Analogue to a Plasmonic Device

Plot of  $|E_z|$  on a logarithmic scale



Experimental setup

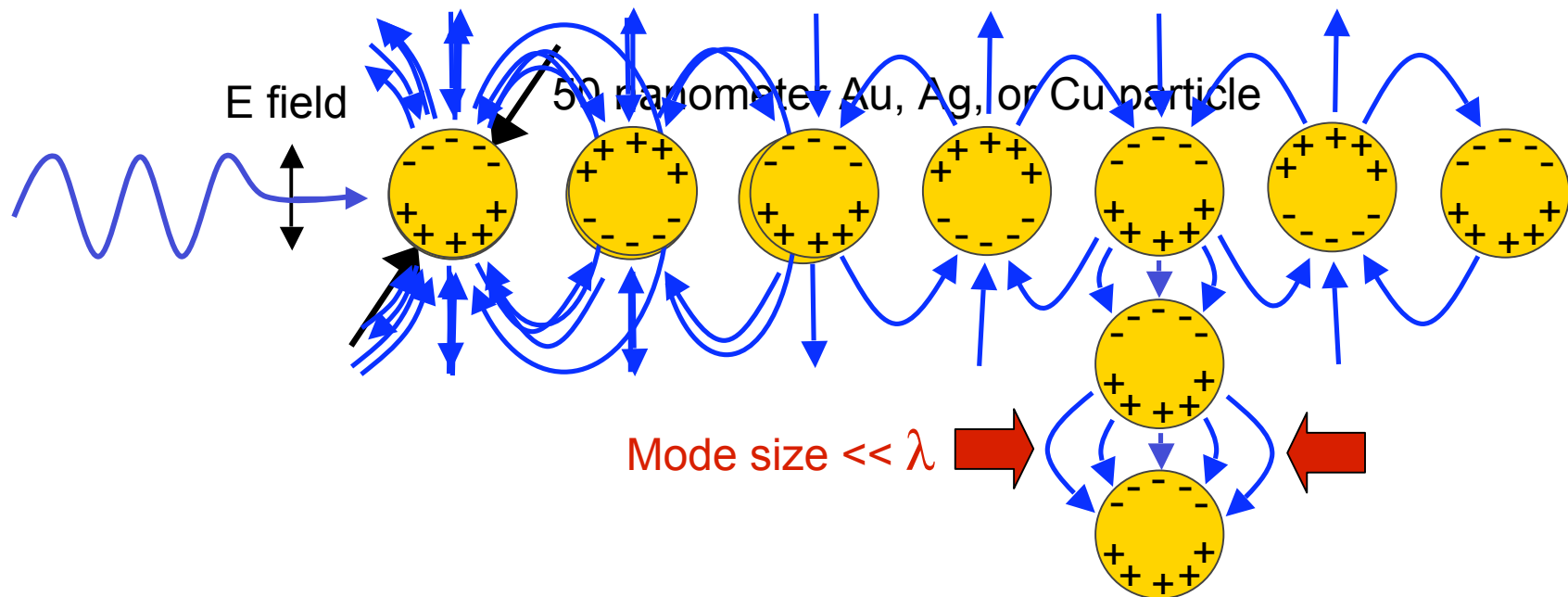


*Stefan A. Maier et al.,  
Appl. Phys. Lett. 78, 16, 2001*

- 90% of the energy is confined within a distance of  $0.05\lambda_F$
- 3-4 dB loss at a corner due far-field radiation

## EM Near-field Interaction between Nanoparticles

---



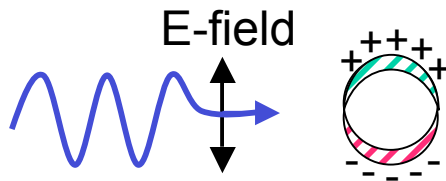
- Light can penetrate metallic nanoparticles and set the electrons in motion
- This collective electron motion is called a plasmon
- **Plasmonics**: Guiding “light” along metallic nanostructures
- Loss per unit length  $\approx 3 \text{ dB}/\mu\text{m}$  .... Loss per device may be manageable

# Excitation of a Single Metal Nanoparticle

## Particle

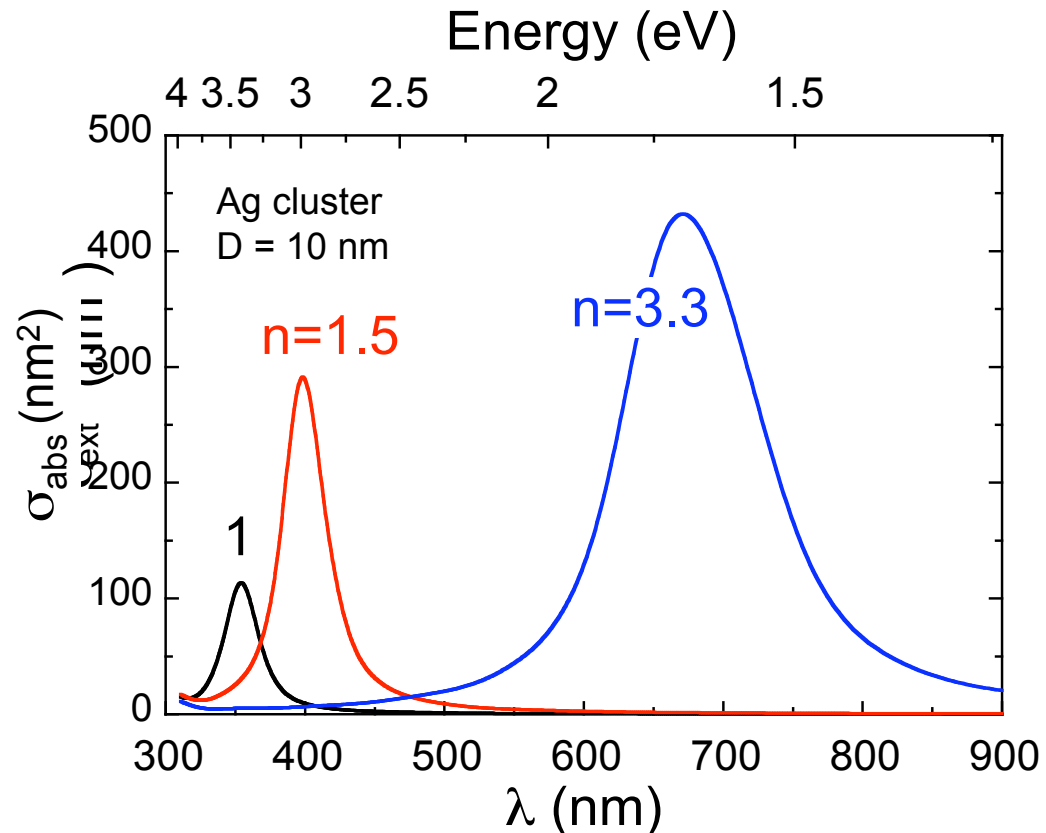
Volume =  $V_0$

$$\epsilon_M = \epsilon_{1,M} + i\epsilon_{2,M}$$



## Host matrix

$$\epsilon_H = \epsilon_{1,H} = \begin{bmatrix} \blacksquare & \\ & \blacksquare \end{bmatrix}$$



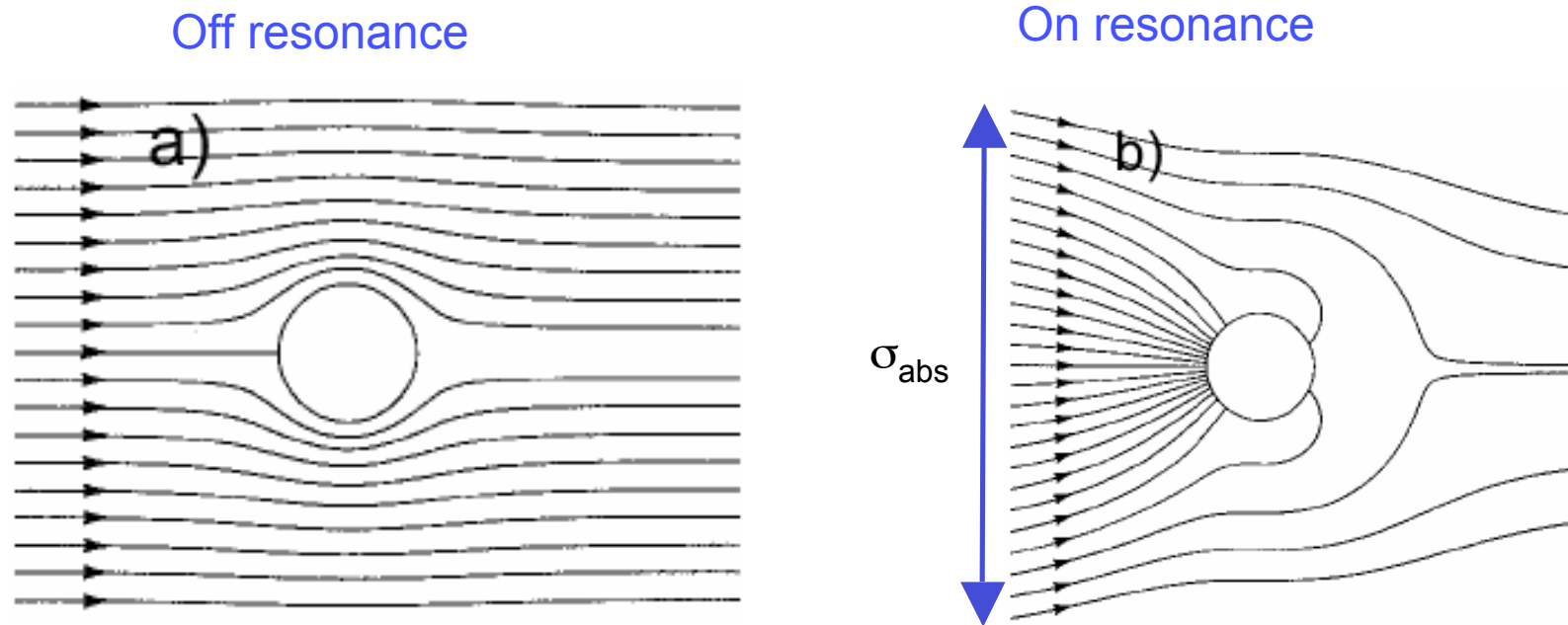
$$\sigma_{abs}(\omega) = 9 \frac{\omega}{c} \epsilon_H^{3/2} V_0 \frac{\epsilon_{1,M}(\omega)}{[\epsilon_{1,M}(\omega) + 2\epsilon_H]^2 + \epsilon_{2,M}(\omega)^2}$$

*G. Mie Ann. Phys. 25, 377 (1908)*

# Origin Enhanced Absorption Cross-section

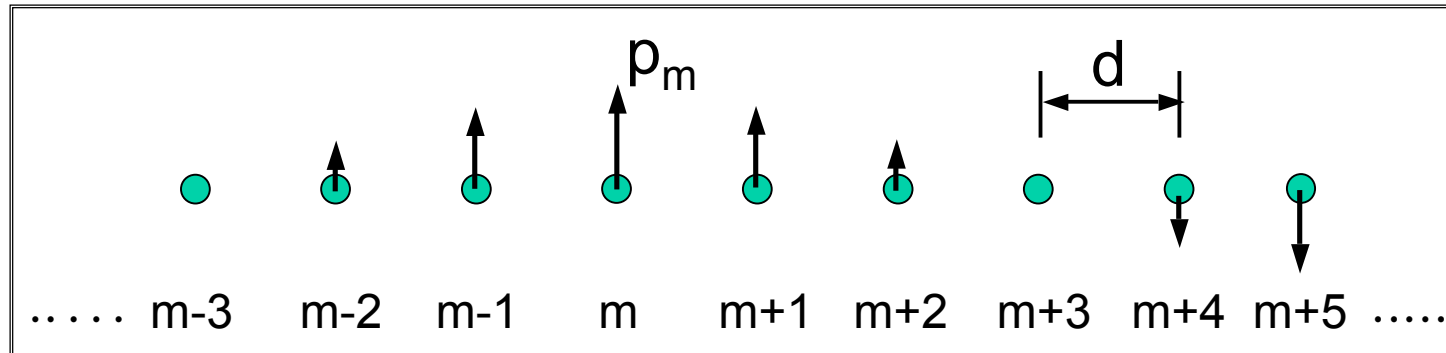
## Poynting vector

Energy flux (Poynting vector) for a plane wave incident on a metallic nanoparticle



# Properties of a Chain of Metal Nanoparticles

---



- Near-field interaction sets up dipole (plasmon) waves
- Two types: Transverse (T) & Longitudinal (L) modes
- Interaction strength related to dipole field  $E_p$

$$E_p = E_F + E_M + E_R \quad \text{Where} \quad \begin{array}{ll} E_F \propto R^{-3} & \text{Förster field} \\ E_M \propto R^{-2} & \\ E_R \propto R^{-1} & \text{Radiation field} \end{array}$$

When  $d \ll \lambda$  Förster field dominant  $\Rightarrow$  n.n. interaction dominates



## Dispersion Relation for Plasmon Modes

---

Equation of motion of dipole at m:

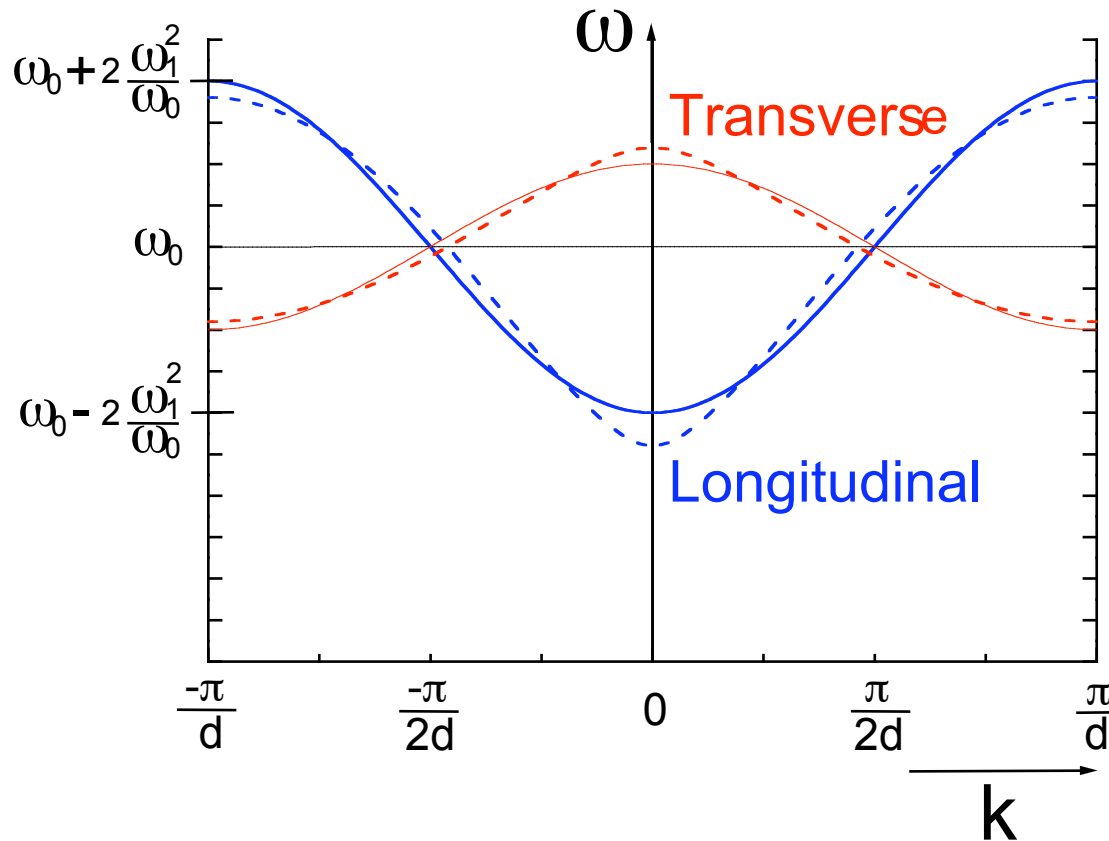
$$\ddot{p}_{i,m}(t) = -\omega_0^2 p_{i,m}(t) - \gamma_i \omega_1^2 [p_{i,m-1}(t) + p_{i,m+1}(t)]$$

$$\text{Where } \omega_1^2 = \frac{\rho V e^2}{4\pi\epsilon_0 m_e n^2 d^3}$$

$$\gamma \equiv \text{a polarization dependent constant} \begin{cases} \gamma_T = 1: & \begin{array}{cc} \uparrow p_{T,m} & \uparrow p_{T,m+1} \end{array} \\ \gamma_L = -2: & \begin{array}{cc} \overrightarrow{p_{L,m}} & \overrightarrow{p_{L,m+1}} \end{array} \end{cases}$$

Propagating wave solution:  $p_{i,m}(t) = P_i \exp i(\omega t \pm k m d)$

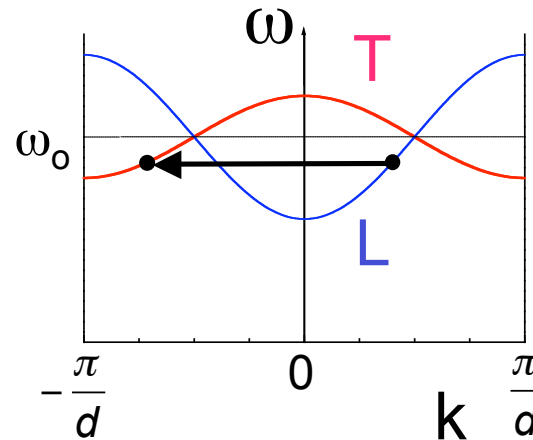
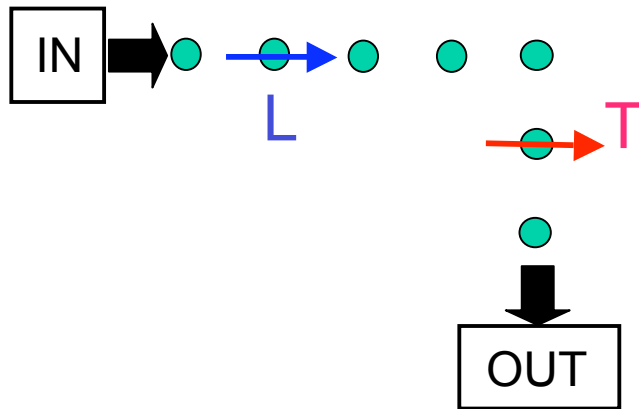
# Dispersion Relation for Plasmon Modes



$$\text{Where } \omega_1^2 = \frac{\rho V e}{4\pi\epsilon_0 m_e n^2 d^3}$$

**Example:** Ag particles,  $R = 10 \text{ nm}$   
 $d = 40 \text{ nm}; \quad n = 1.5$   $\Rightarrow \begin{cases} v_{g,T} = 3.4 \times 10^6 \text{ m/s} \\ \Delta\omega_T = 1.8 \times 10^{14} \text{ s}^{-1} (E = 115 \text{ meV}) \end{cases}$

# Propagation Through Corners

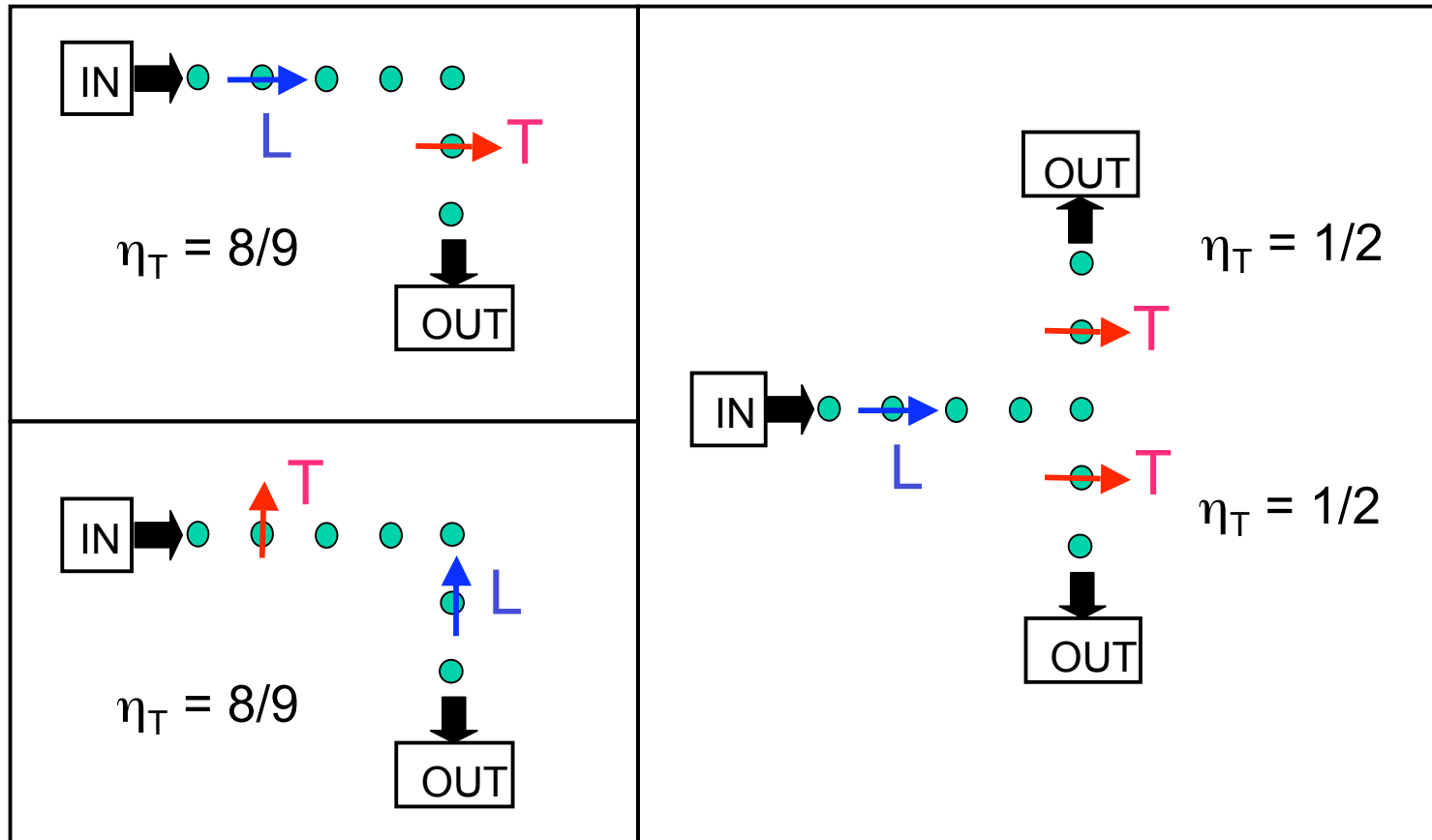


Calculation of power transmission coefficient,  $\eta_T(\omega, \text{pol})$ :

- Continuity amplitude of plasmon wave
- Continuity energy flux in plasmon wave

Maximum  $\eta_T$  at  $\omega_0$

## Power Transmission Coefficients, $\eta_T$



- $\eta_T > 64\%$  for all possible corner and T structures
- Calculations easily extended to 3D structures

## Fabrication of Arrays by AFM Manipulation

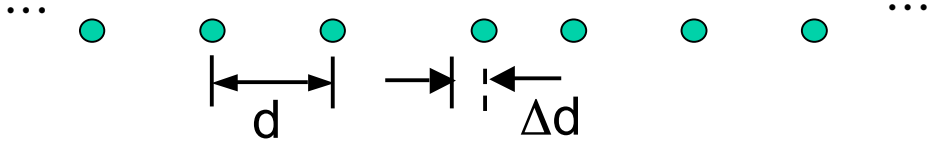
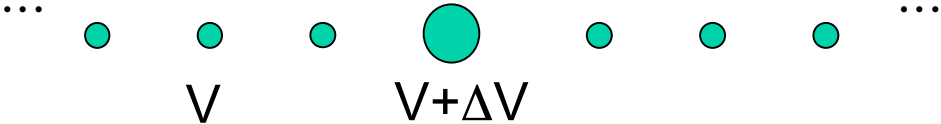
---



- AFM manipulation of 30 nm Au particles on APTS coated  $\text{SiO}_2$   
(APTS = *AminoPropylTrimethoxySilane*)
- Advantages: Au particles and chemicals commercially available.  
Flexibility to image and modify structures.

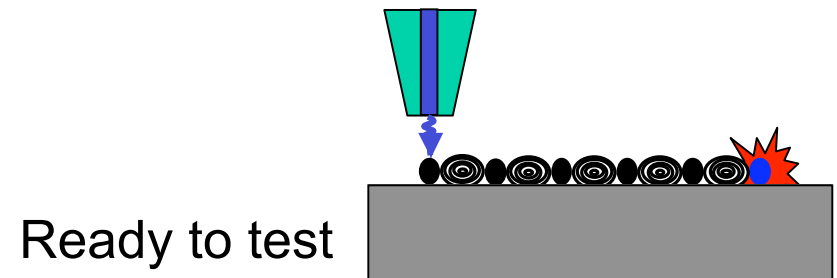
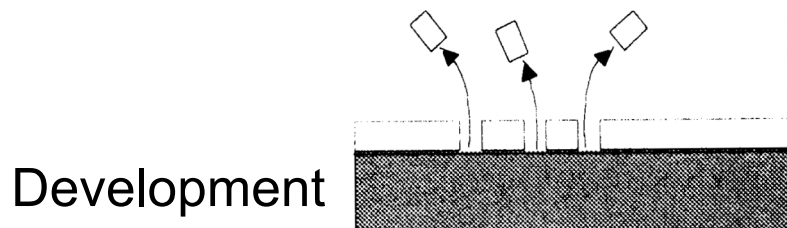
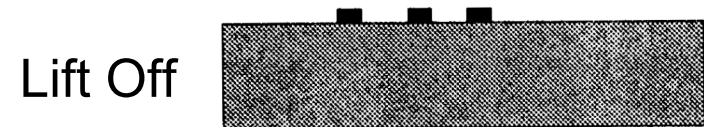
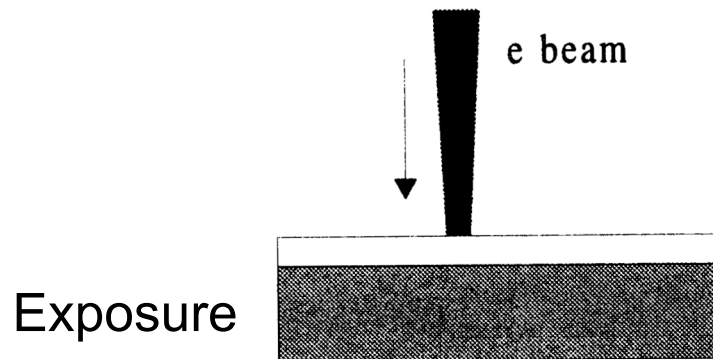
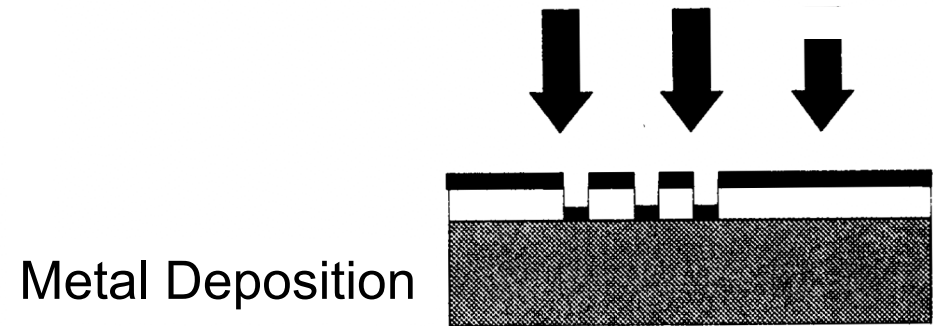
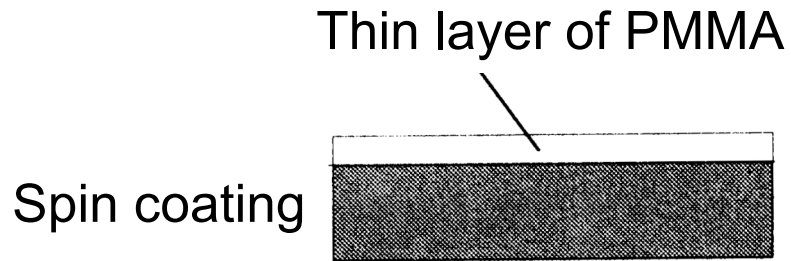
*Sheffer Meltzer, Aristides A.G.  
Requicha, and Bruce E. Koel, USC*

## The Role of Defects and Disorder → Reflections

Periodicity	 <p>Dipole approximation: <math>\eta_T = 1 - 9(\Delta d/d)^2</math>          Example: <math>\Delta d/d = 5\%</math> (5nm/75nm) ➡ <math>\eta_T = 96\%</math></p>
Size fluctuations	 <p>Dipole approximation: <math>\eta_T = \frac{1}{[1 + \Delta V/2V]^2}</math>          Example: <math>\Delta V/V = 9\%</math> (1nm/25nm) ➡ <math>\eta_T = 91\%</math></p>
Intrinsic loss:	<p>5% per interparticle spacing ➡ <math>\eta_T = 95\%</math>          (Calculated for 25 nm Ag particles spaced by 75 nm)</p>

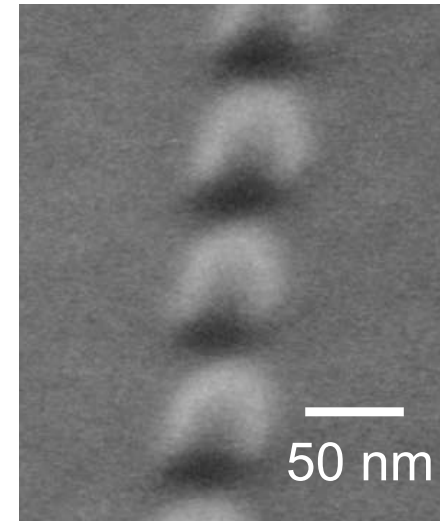
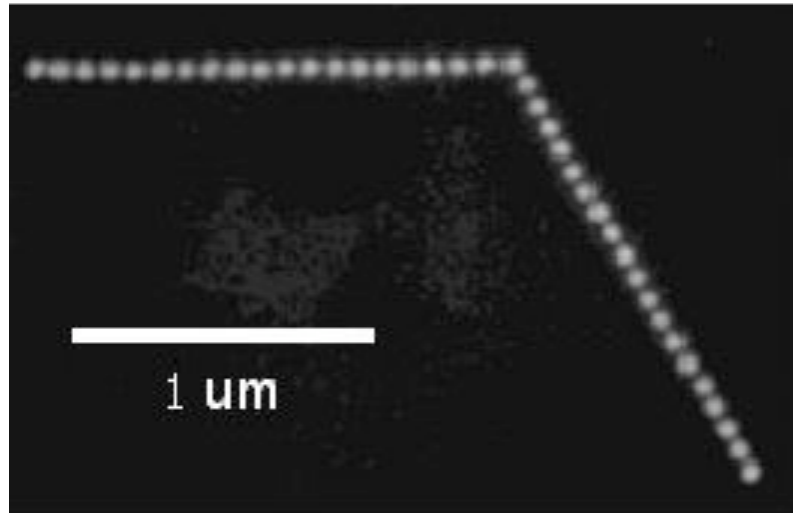
# Generation of Arrays by e-beam Lithography

---



## SEM Images of Nanoparticle Arrays

---

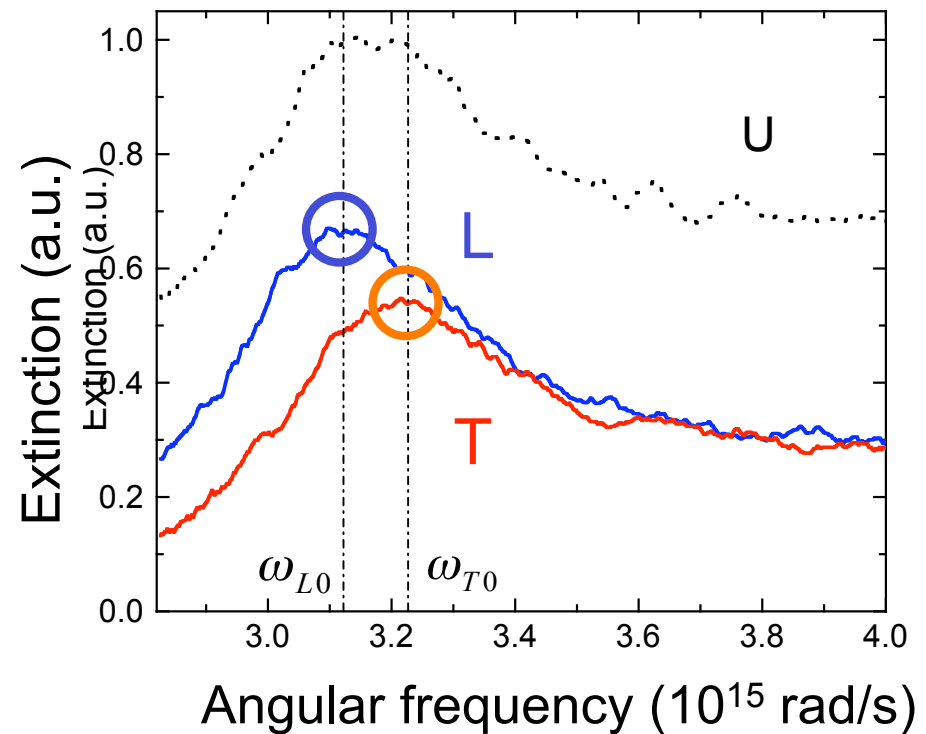
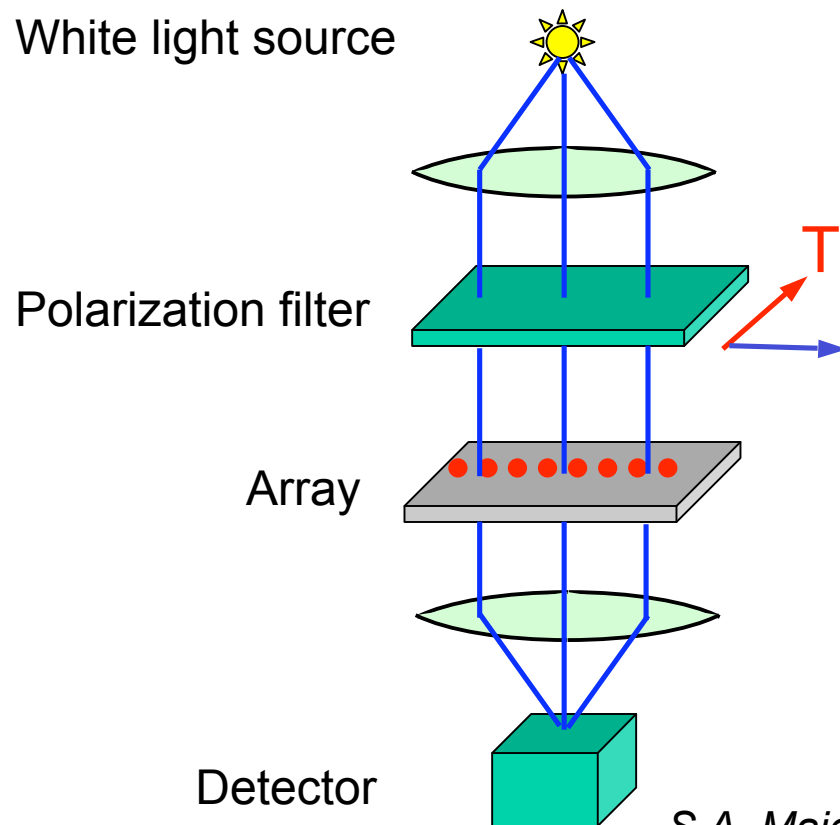


- Array of 50 nm diameter Au dots spaced by 75 nm
- Good control over particle size, shape, interparticle spacing



# Far-field Spectroscopy on a Au Nanoparticle Array

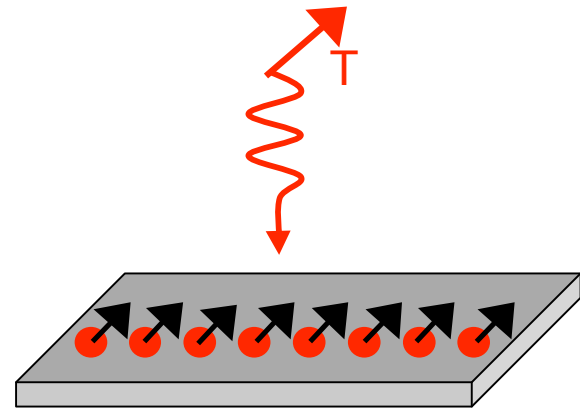
## Extinction measurement



*S.A. Maier et. al, Phys. Rev. B 65, 193408-193411 (2002).*

- EM coupling between particles breaks the rotational symmetry of a single particle

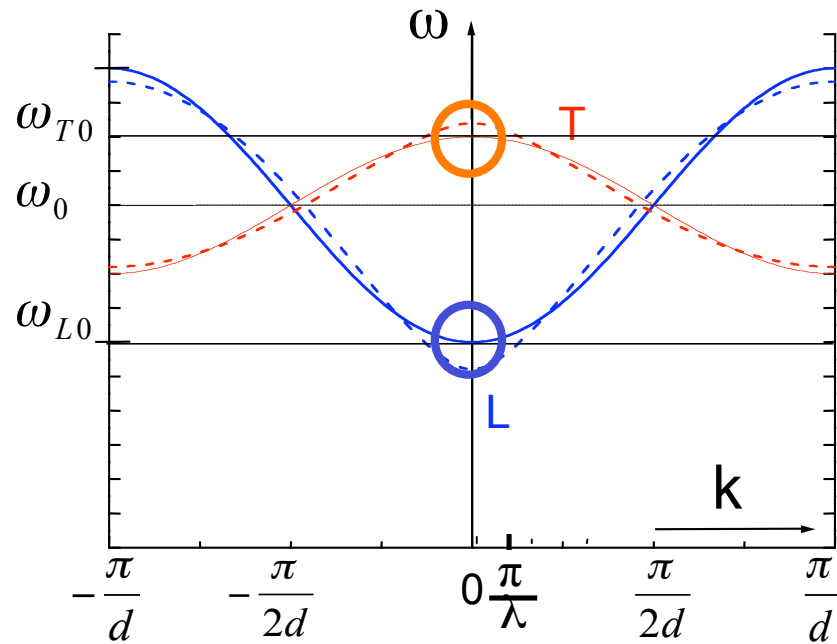
# Observation of Near-field Coupling in Particle Arrays



Transverse polarization

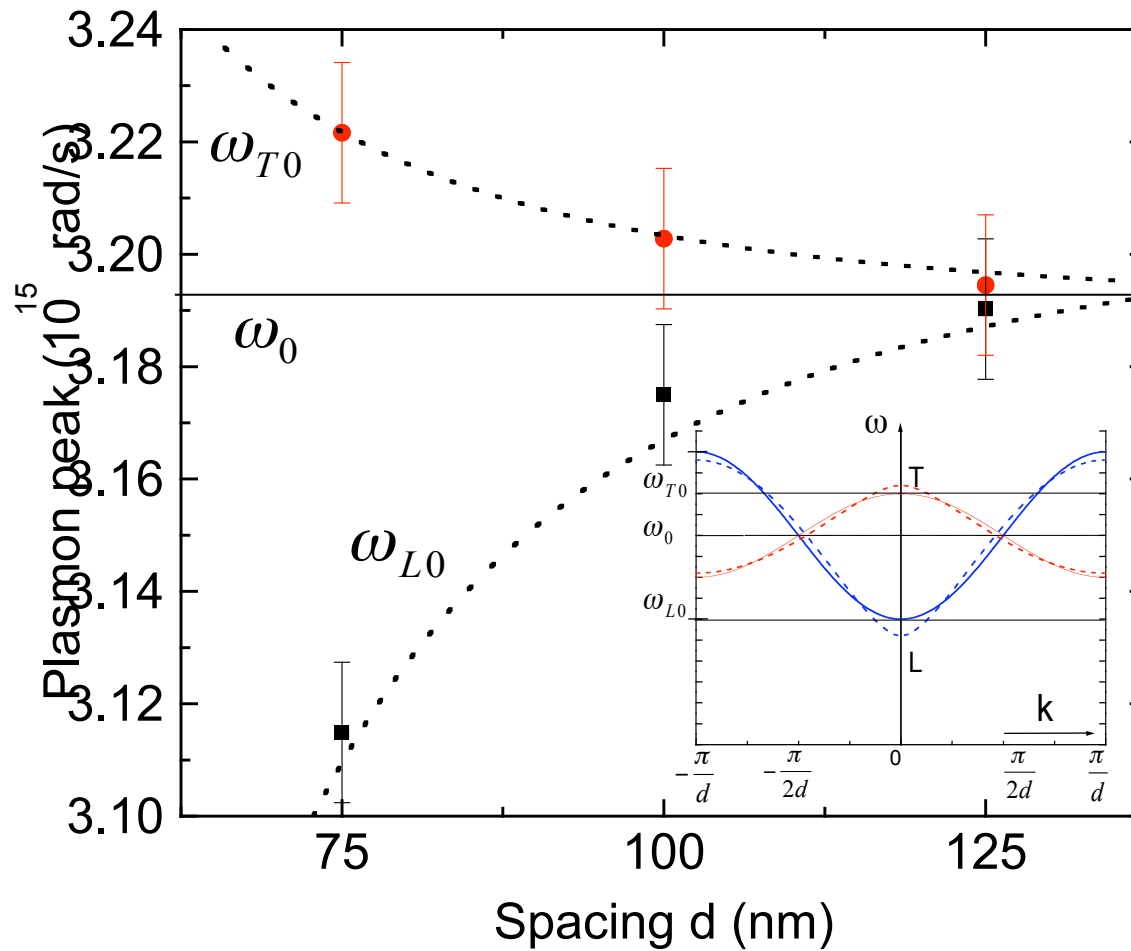


Longitudinal polarization



- Probes dispersion relation at  $k=0$   
(Because  $\lambda \gg d$  = interparticle spacing)

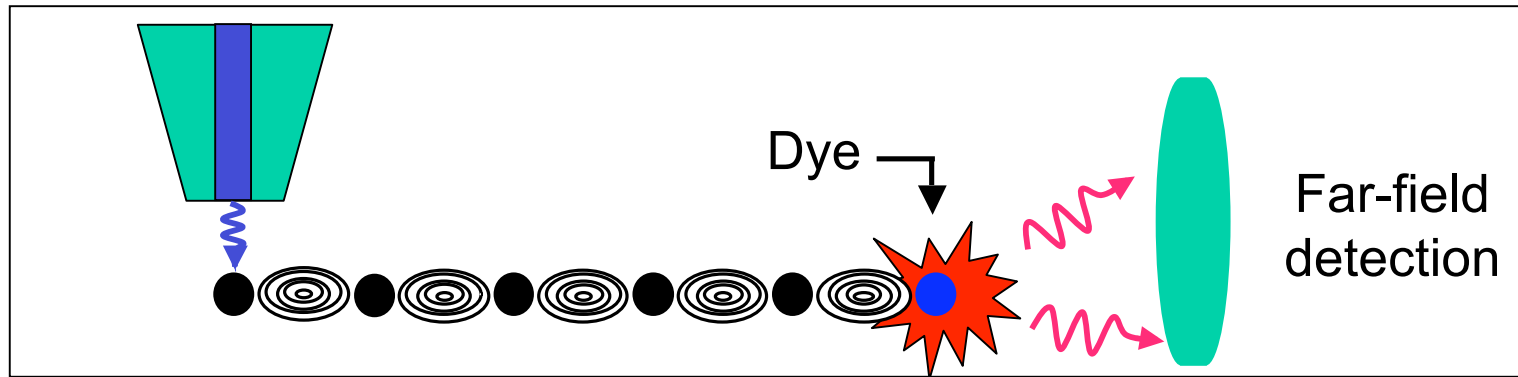
## Dependence of Mode Splitting on Interparticle Spacing



- Peak splitting vanishes with increasing interparticle spacing  $d$  as  $d^{-3}$

# Experiments on AFM Assembled Arrays

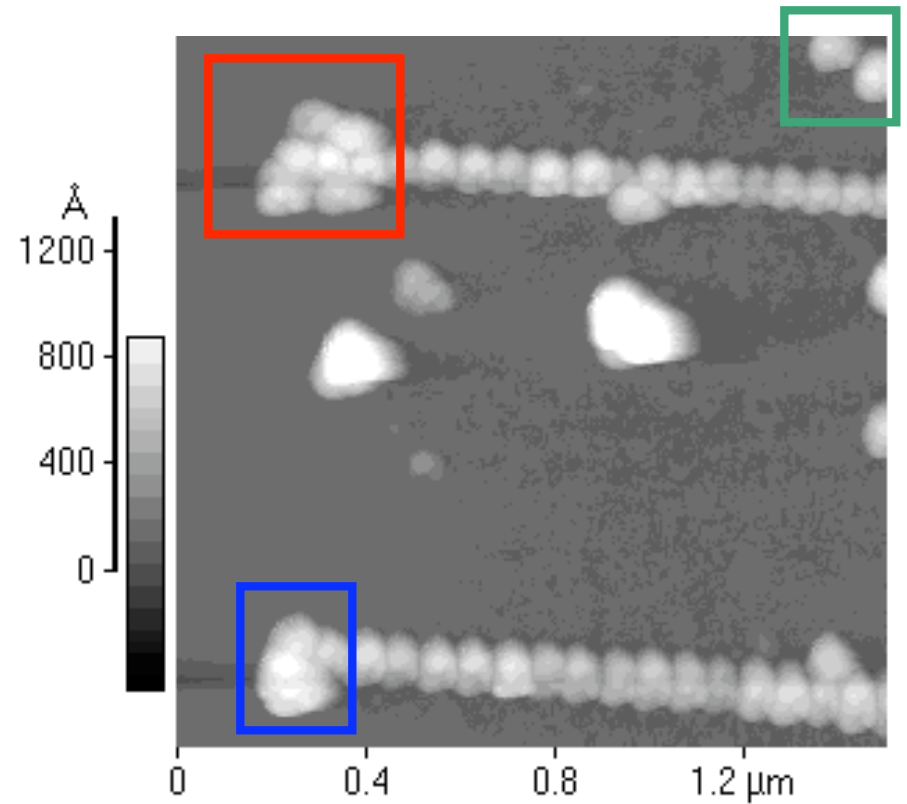
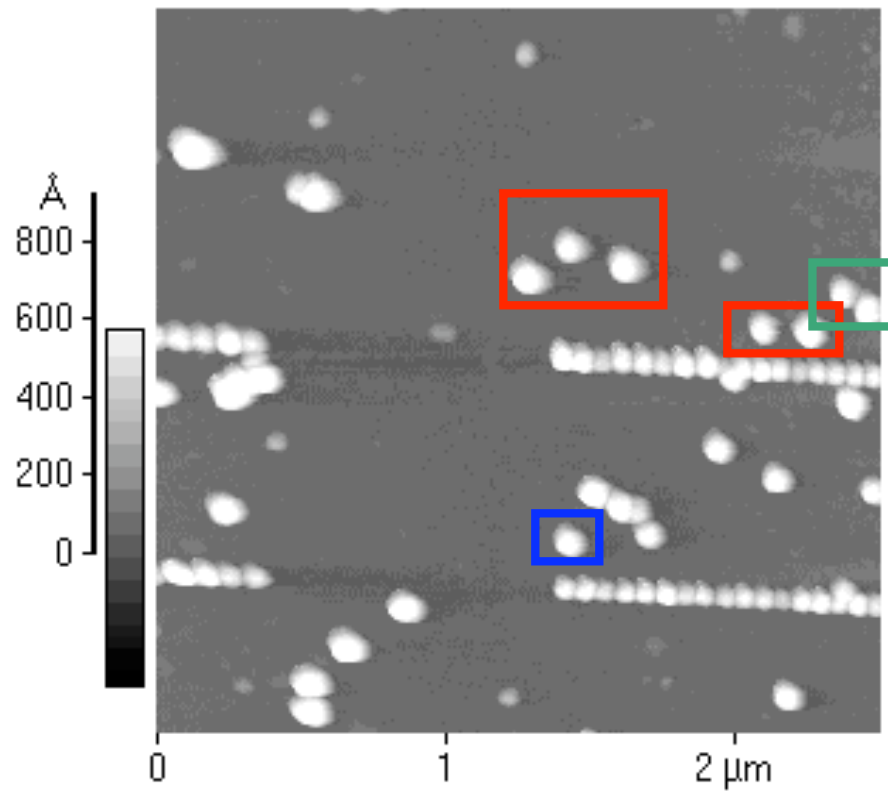
---



- **Excitation** using a scanning near-field optical microscope
- **Transport** along metal nanoparticle array
- **Detection** of dye luminescence in far-field

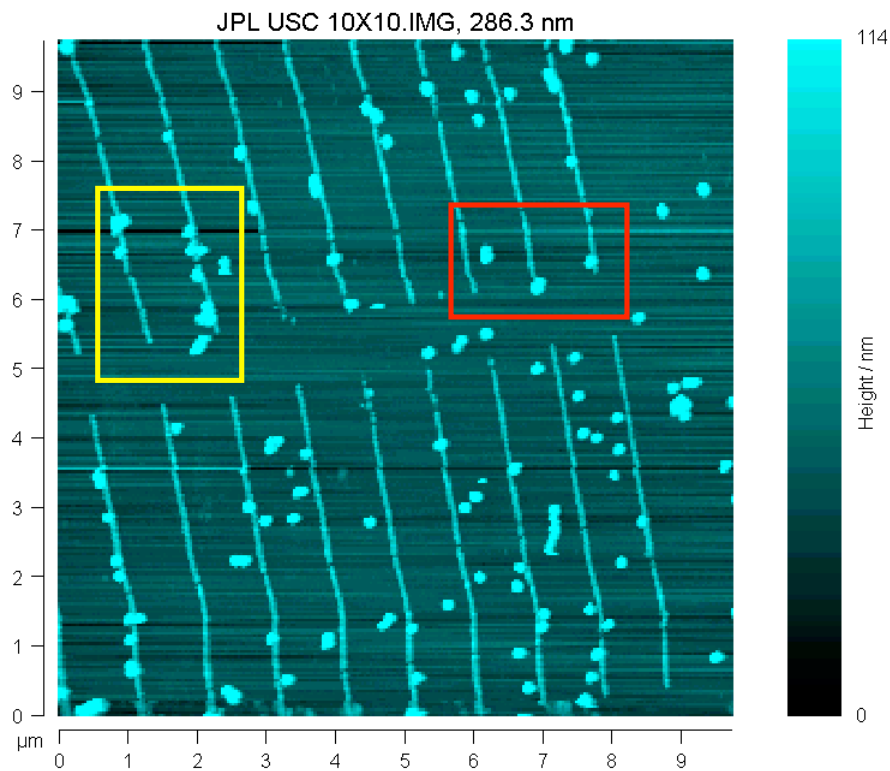
## AFM Manipulation of Latex Beads with Dyes

---

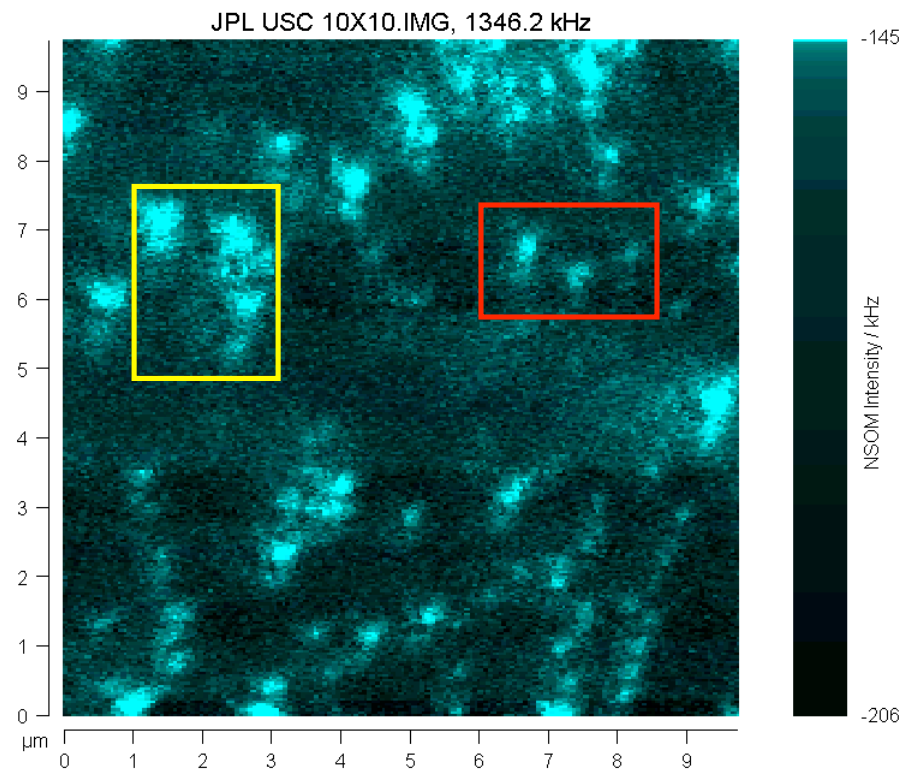


# Luminescence from Single Latex Spheres

## Topography

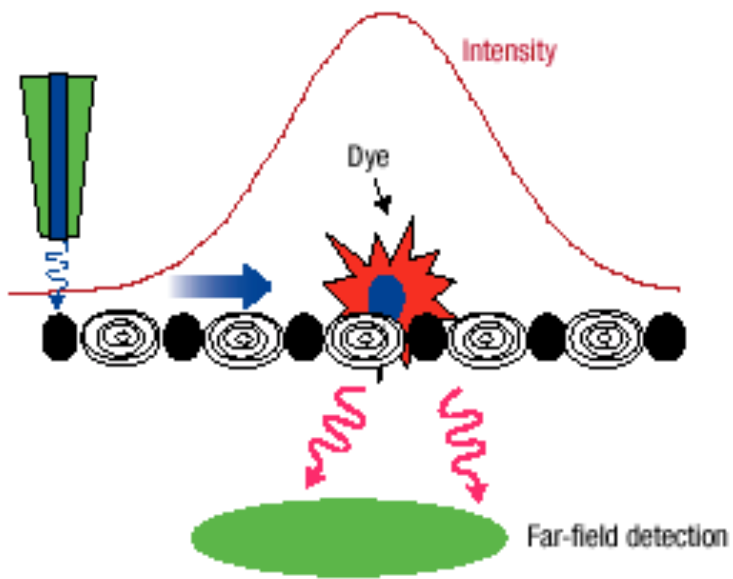


## Fluorescence (inverted log)

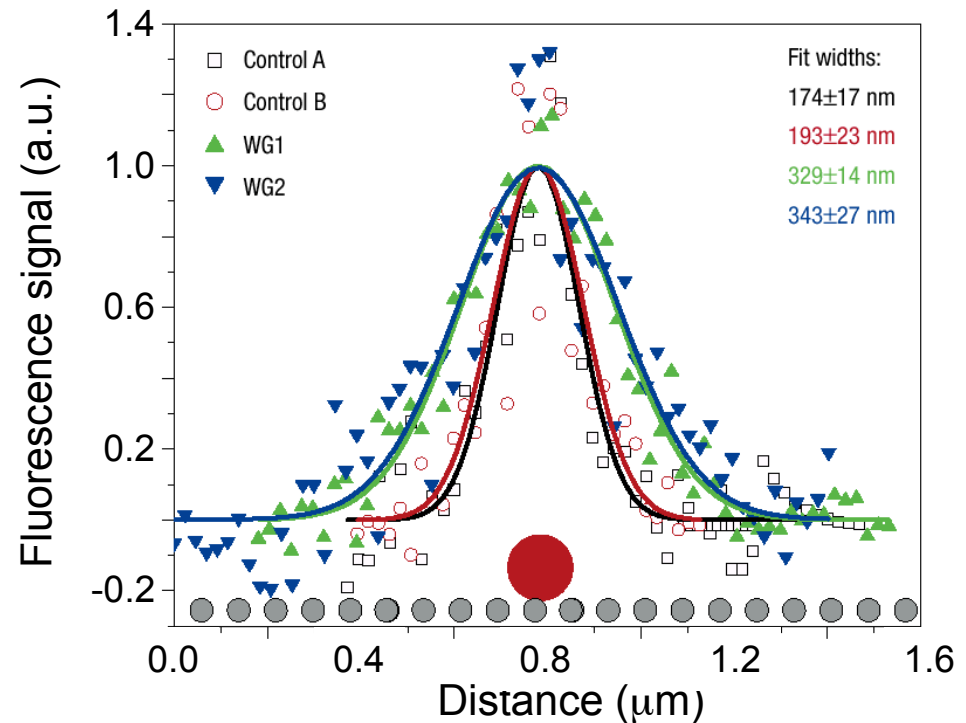


# Transport experiment

## Idea



## Experiment



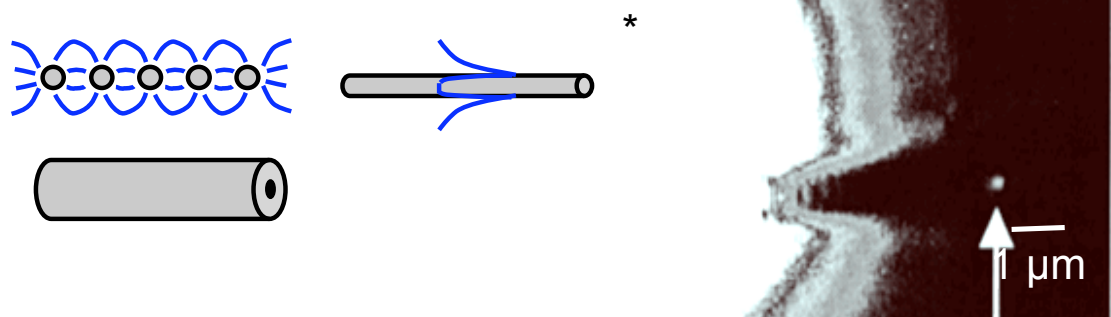
If no transport occurs, fluorescence will only be collected when the tip is directly on top of the dye

Green/blue curves luminescent particle on a wire  
Red/black curves luminescent particles next to a wire

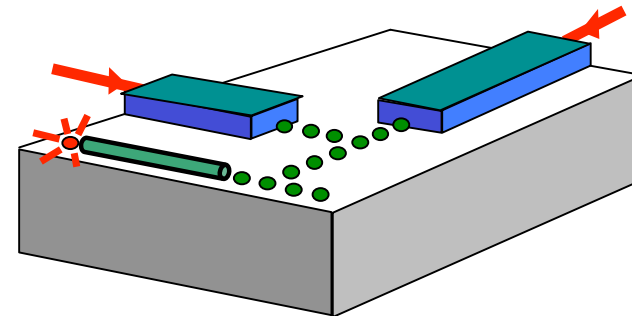
# The Future of Metal Optics

## Photonics

- Basic building blocks



- More complex architectures

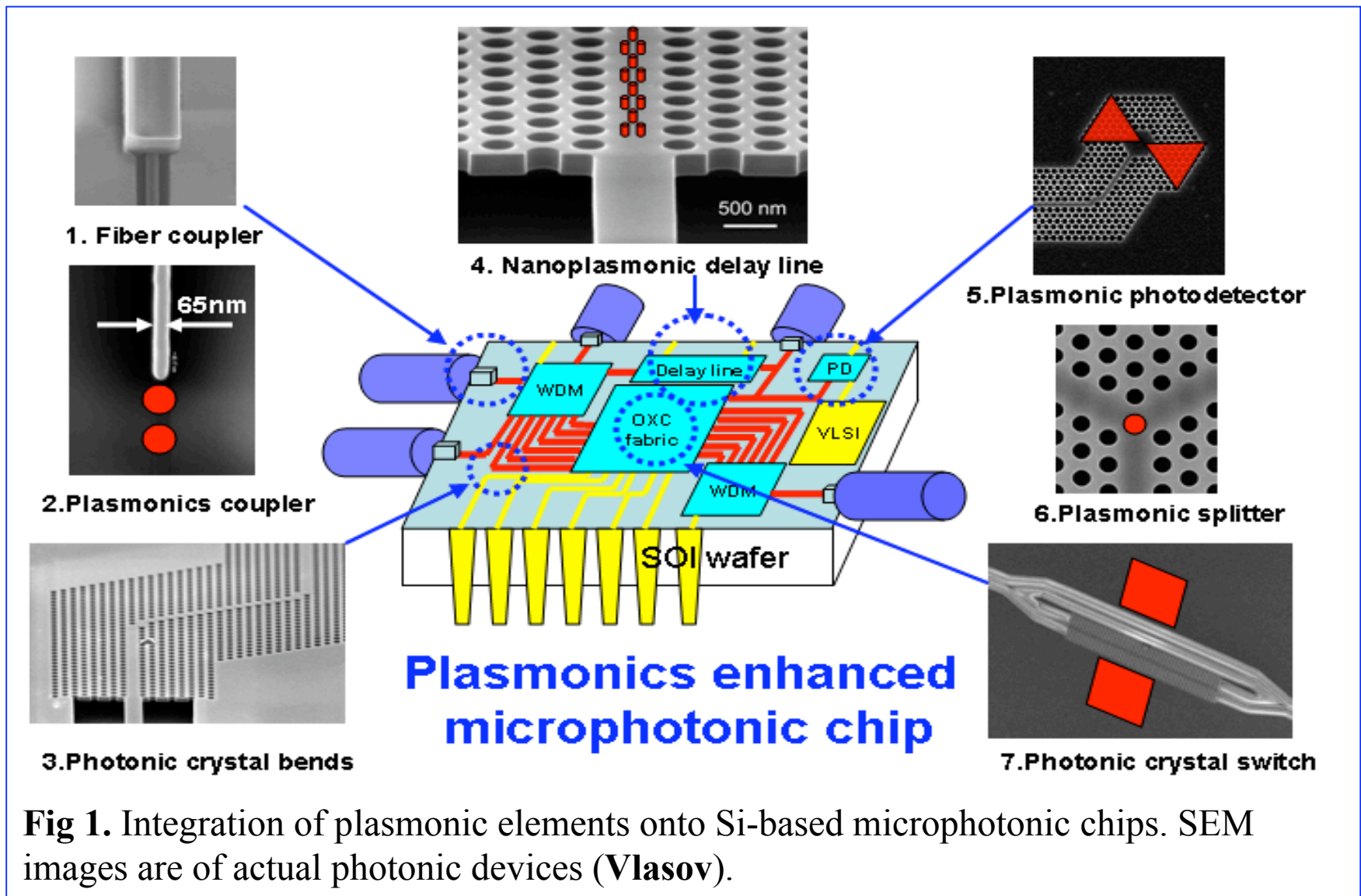


- Applications in biology for “Optical microscopy” ?
- Applications in high-density optical data storage ?
- Fundamental studies of light-matter interaction

\* *R.M. Dickson et al., J. Phys. Chem. B* **104**, 6095-6098 (2000)



# The Future of Metal Optics

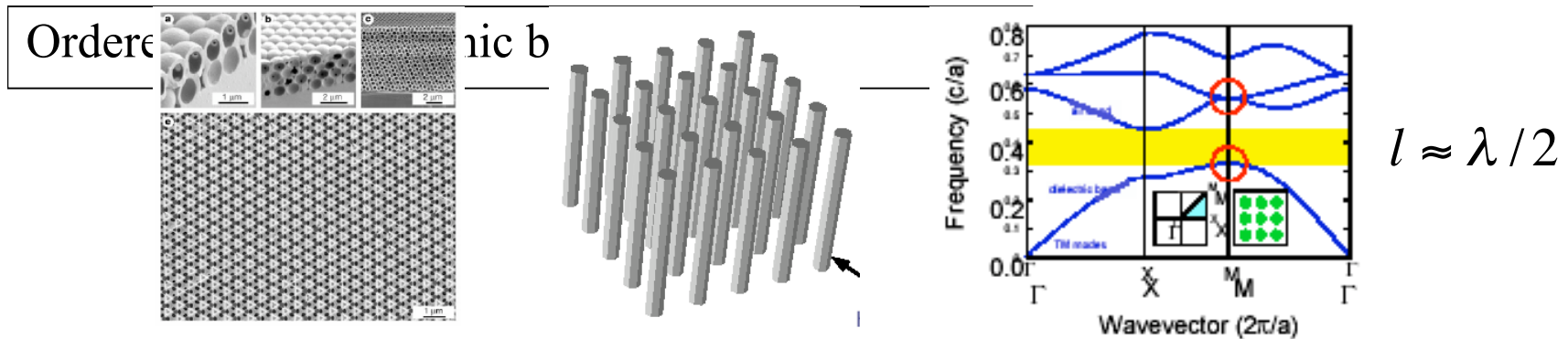


**Fig 1.** Integration of plasmonic elements onto Si-based microphotonic chips. SEM images are of actual photonic devices (Vlasov).

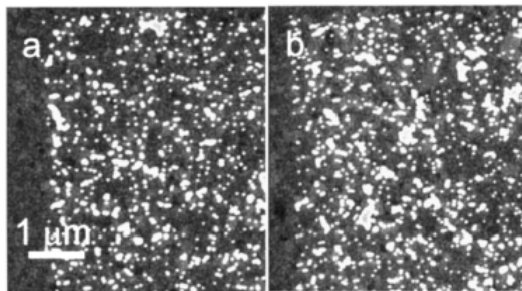
---

# **Addition to Lecture #11: Localization and Guiding of Surface Plasmon Polaritons in Random Nanostructures**

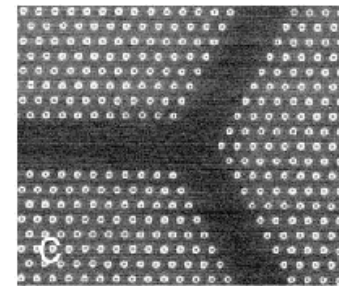
*Bozhevolnyi et al., Physics Review Letter  
89, p186801-1 (2002)*



Disordered media: localization (multiple scattering)



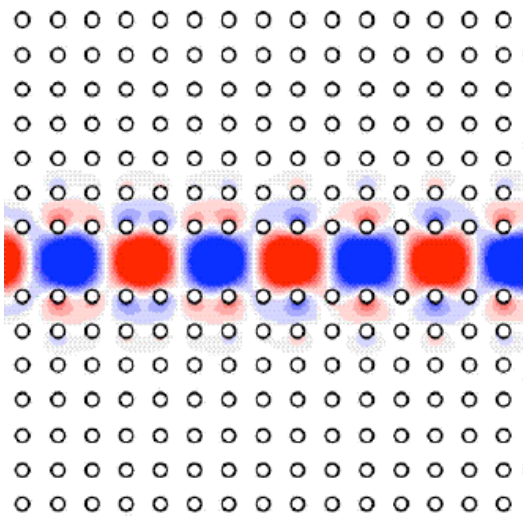
$$l < \lambda/2\pi$$



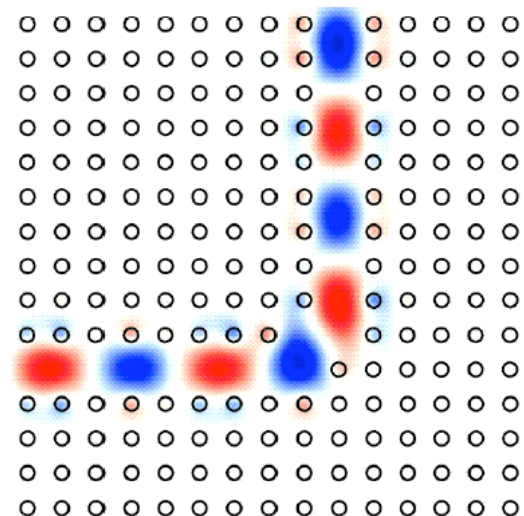
- Both inhibit light propagation
- Both in a limited range of frequencies
- Both require a large refractive index contrast

---

Photonic crystals confine the  
light inside the defect



Can guide light  
through bends!

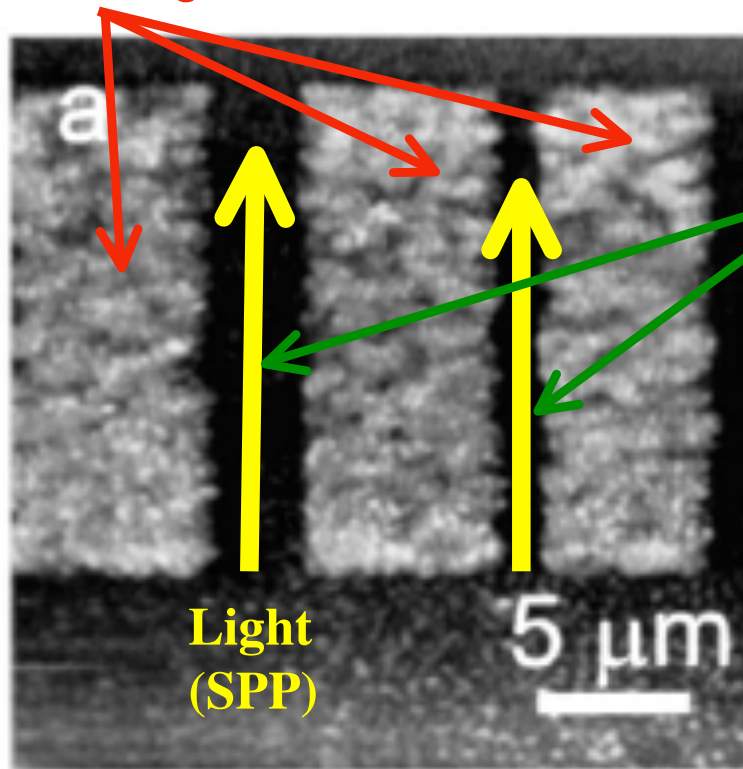


**Can the same thing can be done in random  
media?**

---

This paper: First observations of confinement due to random corrugations created by surface features.

Surface corrugation

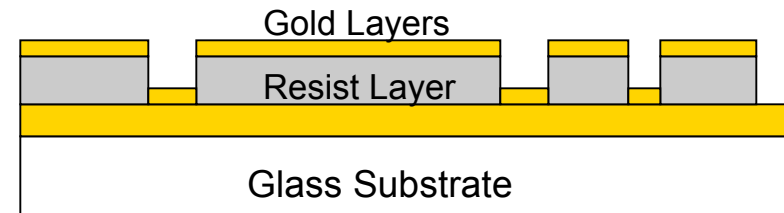


Propagation of SPPs: Surface Plasmon Polariton

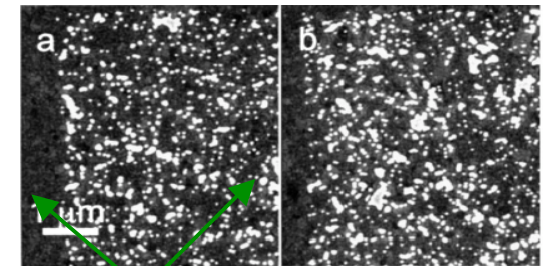
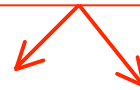
Confining mechanism: **localization**, i.e. multiple scattering and interference that prevents the light from propagating.

## Randomly positioned Au nanoscatterers lead to strong SPP localization

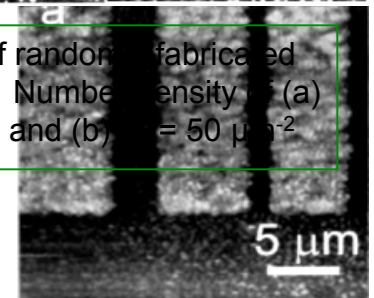
- 45 nm thick Au layer thermally evaporated onto glass substrate
- Resist is deposited on Au layer and  $6 \times 18 \mu\text{m}^2$  rectangular areas patterned
- Random coordinates within each rectangle exposed using an electron beam
- Exposed region removed and 2<sup>nd</sup> Au layer evaporated
- Remaining resist is etched away leaving disordered arrays of ~45 nm high gold bumps



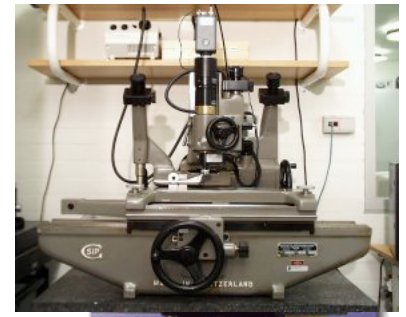
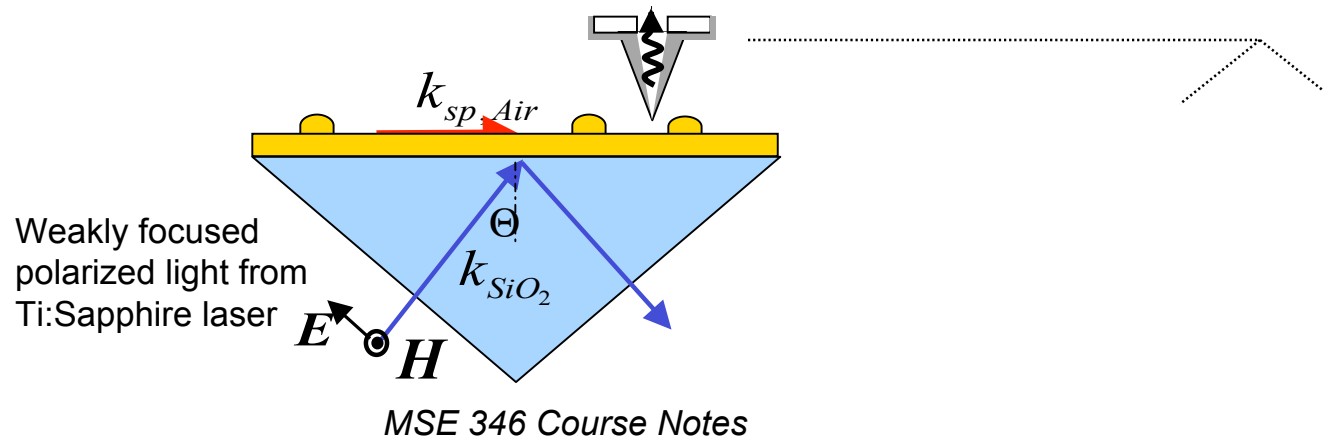
A 2- and 4- $\mu\text{m}$  wide channel were left free of scatterers for SPP guiding



Two regions of randomly fabricated nanoparticles. Number density is (a)  $n_1 = 37.5 \mu\text{m}^{-2}$  and (b)  $n_2 = 50 \mu\text{m}^{-2}$



## Kretschmann-based configuration used to excite SPP's



<http://www.elicht.com/DualScop.htm>

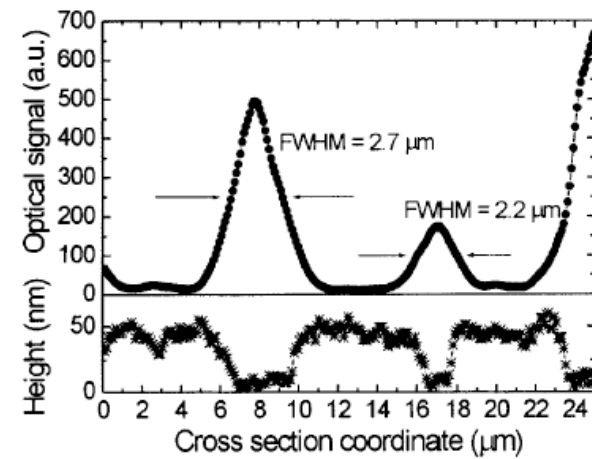
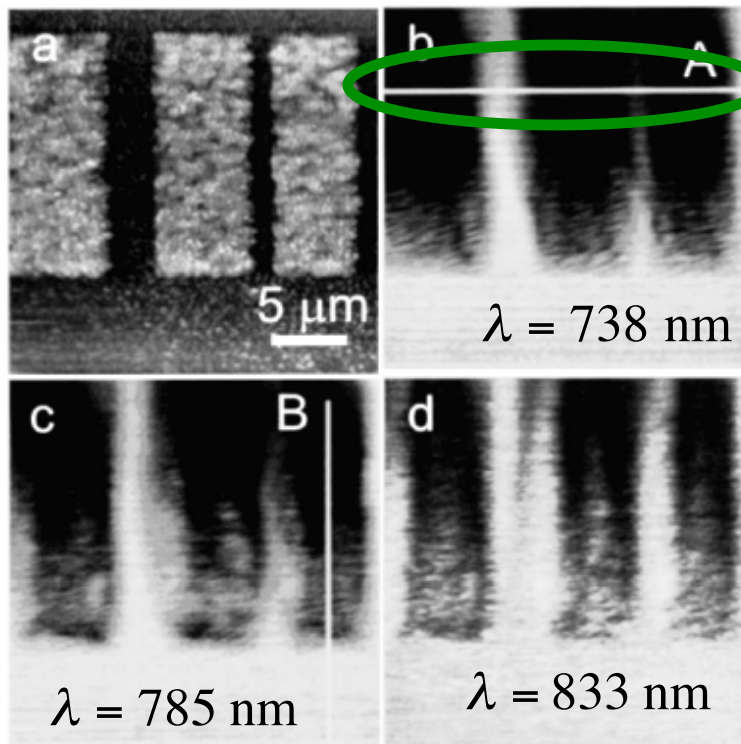
- Ti:Sapphire laser ( $\lambda = 725 - 850$  nm,  $P \sim 100$  mW) excitation source focused to a  $300 \mu\text{m}$  spot size

- Near-field radiation scattered by sharp fiber tip into fiber modes. Imaged by DME-DualScope NSOM

- SPP excitation recognized through a minimum in the angular dependence of reflected light



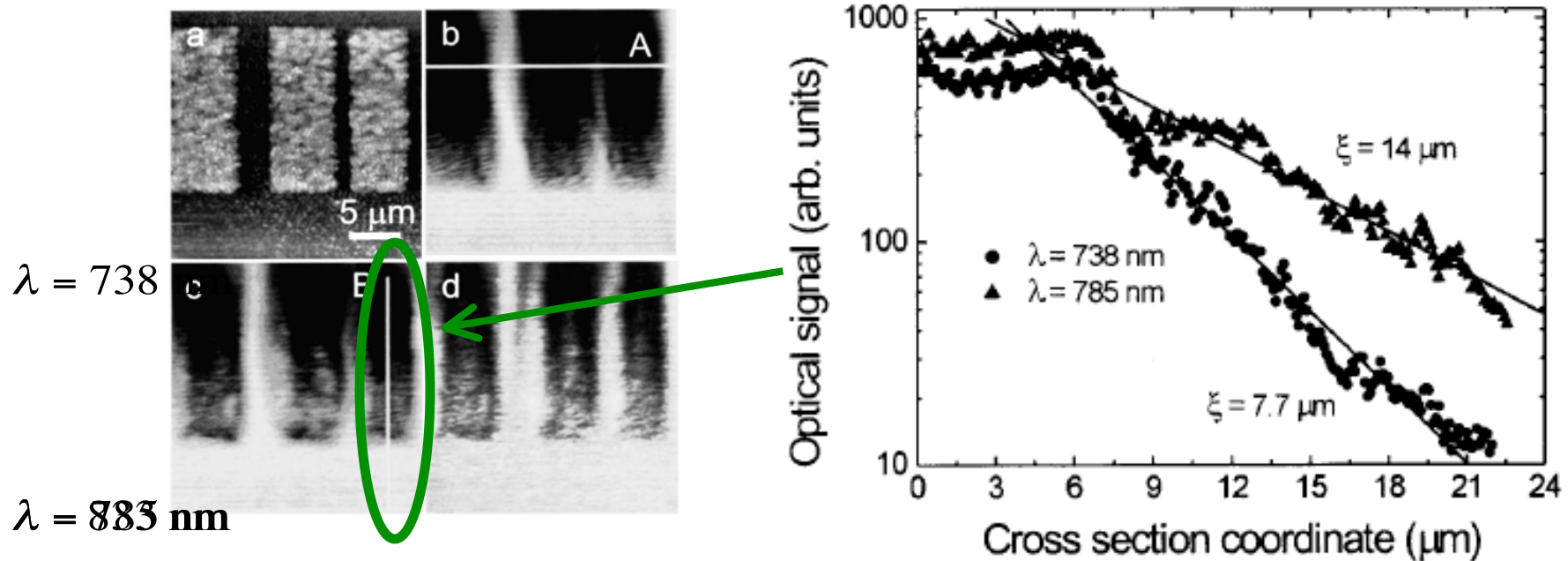
## Experimental demonstration of waveguiding



- Waveguide length: 18  $\mu\text{m}$
- Waveguiding range:  
725 - 765 nm  
(40 nm bandwidth!)

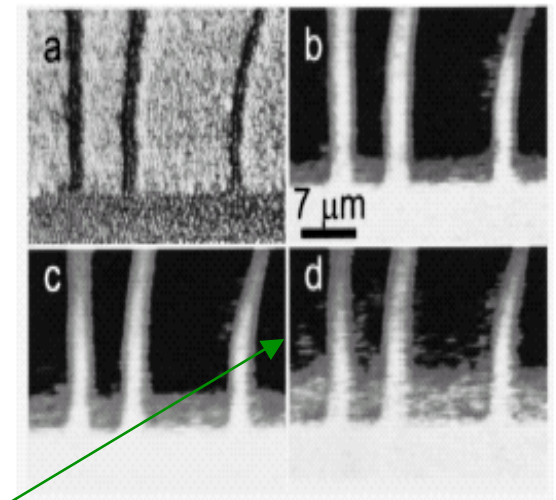


Random media stops the propagation of the light



The penetration depth (or localization length) depends on the scattering cross-section, the scattering mean free path, and the wavelength

- 
- Increase particle number density  
(75 per  $\mu\text{m}^2$  has been tried and works better)
  - Increase the particle size  
(for a larger scattering cross-section)
  - Bends and other waveguide geometries



2- $\mu\text{m}$  straight and bent channels show strong SPP attenuation. Low levels of additional bend loss ( $<1\text{dB}$ ) in the wavelength range of 735-795 nm

- 
- Successful demonstration of waveguiding of surface plasmon-polaritons
  - Demonstration of confinement in disordered media
  - Random media could perhaps complement photonic crystals in future work...