

**Introduction to Semiconductor Devices**  
**(Purdue University EE 305/606)**  
**Supplemental Homework Exercises**

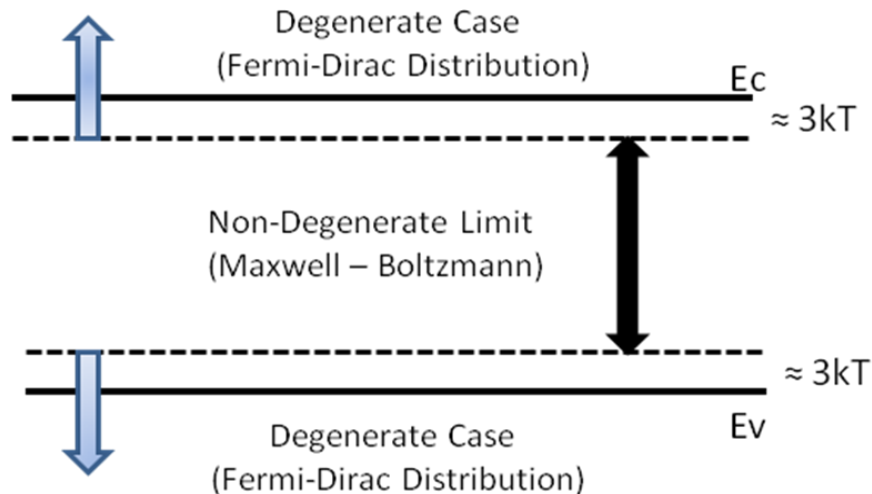
Tutorial questions based on *Carrier Statistics Lab v1.0* available online at <https://www.nanohub.org/resources/3798/>

Reference book: *Semiconductor Device Fundamentals* by Robert E. Pierret (Chapter 2)  
*FD: Fermi-Dirac MB: Maxwell-Boltzmann Ef: Fermi level above Ev*

Q1. Find the occupation probability (value) for Fermi-Dirac distribution function for the following temperatures (i) 4 K (liquid helium temperature) (ii) 77 K (liquid nitrogen temperature) and (iii) 300K (room temperature) and at following energy values. (Select Material = Si,  $E_f = 0.56\text{eV}$  (mid-gap))

- (a)  $E_f$
- (b)  $E_f - 3kT$
- (c)  $E_f + 3kT$
- (d) Compare the results with Maxwell-Boltzmann distribution.

Q2. As shown in fig.1, for degenerate semiconductors properties are defined by FD statistics and not by MB, as MB overestimates the electron/hole densities when Fermi level is  $> E_c - 3kT$  or  $< E_v + 3kT$ . Now, comment on the following,



**Figure1. Validity of Fermi-Dirac and Maxwell-Boltzmann distribution functions with fermi level.**

- (a) Compute electron and hole concentrations using FD and MB statistics for the following, (Material = Si)
  - (i) at  $T=100\text{ K}$  and  $E_f = E_g/2$  ;  $E_f = E_c$  ;  $E_c + 5kT$  ;  $E_f = E_v$  ;  $E_v - 5kT$
  - (ii) at  $T=200\text{ K}$  and  $E_f = E_g/2$  ;  $E_f = E_c$  ;  $E_c + 5kT$  ;  $E_f = E_v$  ;  $E_v - 5kT$
  - (iii) at  $T=300\text{ K}$  and  $E_f = E_g/2$  ;  $E_f = E_c$  ;  $E_c + 5kT$  ;  $E_f = E_v$  ;  $E_v - 5kT$
- (b) Tabulate the above and show when MB statistics overestimate FD statistics.

(c) What is the physical insight related to your observation?

Q3. Obtain the following for Silicon using Fermi-Dirac statistics at  $T=300\text{K}$ . Vary  $E_f$  from  $E_v+5kT$  to  $E_c-5kT$ .

(a) Plot  $N$  vs  $E_f$ ,  $P$  vs  $E_f$ , and  $N_i$  vs  $E_f$ . (Use minimum 10 data points), where  $N$ ,  $P$  and  $N_i$  represent the mobile electron density, hole density and intrinsic density respectively.

(b) How does the carrier distribution curves change with variation in Fermi-level ( $E_f$ ) and why?

(c) At what energy the peaks occur in (b) ?

Q4. Simulate for intrinsic Silicon using Fermi-Dirac statistics. Vary Temperature from  $T=200\text{K}$  to  $700\text{K}$ . (Hint: Assume intrinsic Fermi level is at  $E_g/2$ )

(a) Plot  $N$  vs  $T$ ,  $P$  vs  $T$  and  $N_i$  vs  $T$ .

(b) Do the same for intrinsic Ge and intrinsic GaAs. (Adjust energy range from  $-0.4\text{eV}$  to  $E_g+0.4\text{eV}$ )

Q.5 Simulate an n-type doped ( $N_d=1\text{e}15/\text{cm}^3$ ) (i) Si (ii) Ge and (iii) GaAs. (take  $N_a=10/\text{cm}^3$ )

(Hint: You can simulate different temperature ranges)

(a) Find the freeze out temperature. ( $T_{\text{freeze-out}}: N/N_d=0.99$ ).

(b) Find the temperature at which extrinsic behaviour ceases to exist. Suppose extrinsic behavior is valid till  $N/N_d \leq 1.01$ .

(c) The difference of (a) and (b) is the working range for that material. Which material has highest working range and why?

(d) Plot Fermi level for the temperature range  $300\text{K}-700\text{K}$ . What do you see and why? Find the slope in  $\text{eV/K}$ .