

Thermoelectricity: From Atoms to Systems

Week 4: Thermoelectric Systems

Lecture 4.6: Overview of Week 4

By Ali Shakouri

Professor of Electrical and Computer Engineering

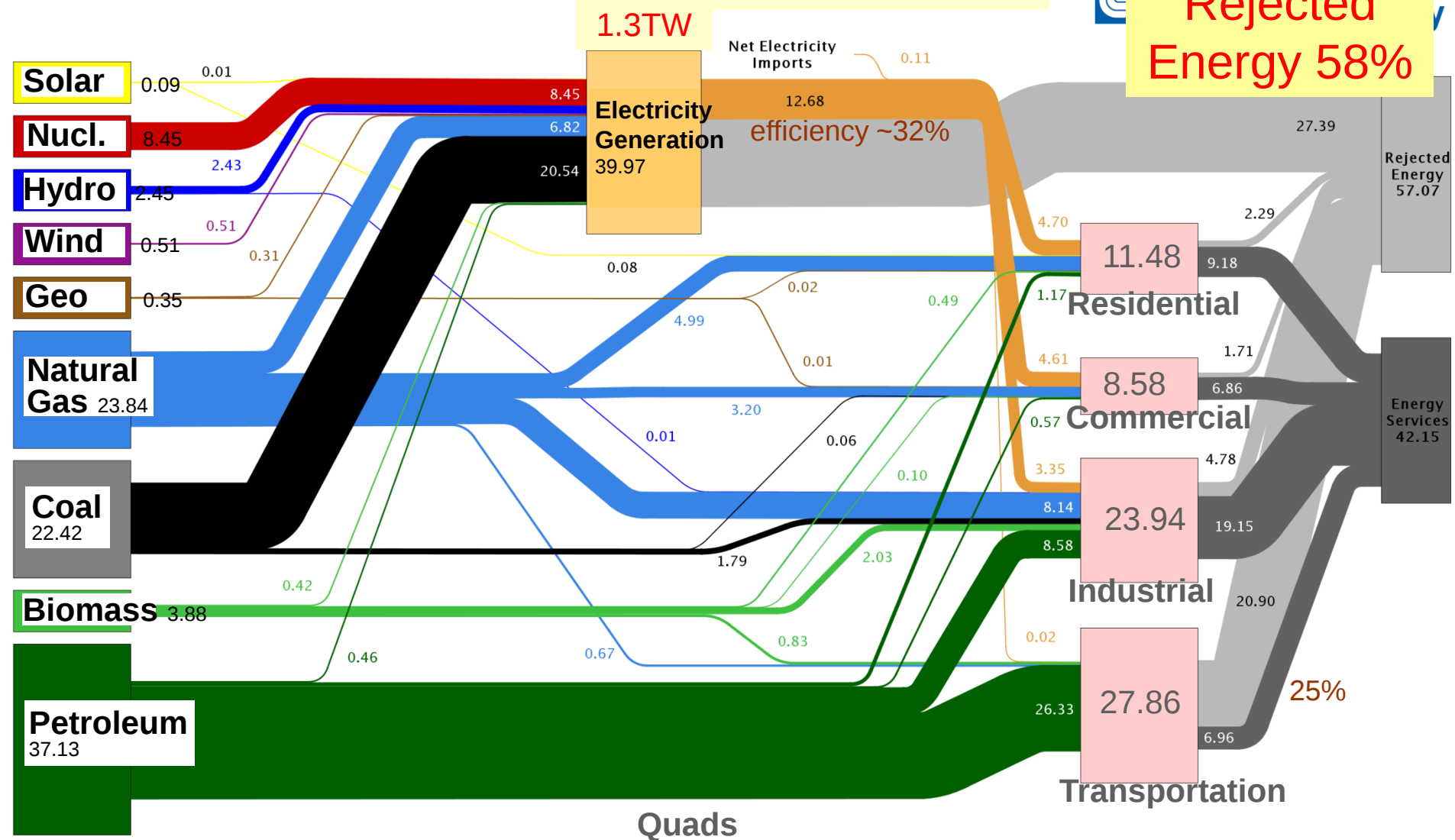
Birck Nanotechnology Center

Purdue University

US Energy Flow 2008

Energy Use = 99.2 Quad = 105 EJ → Power ~3.3 TW

Rejected Energy 58%



TEs for Telecom Cooling

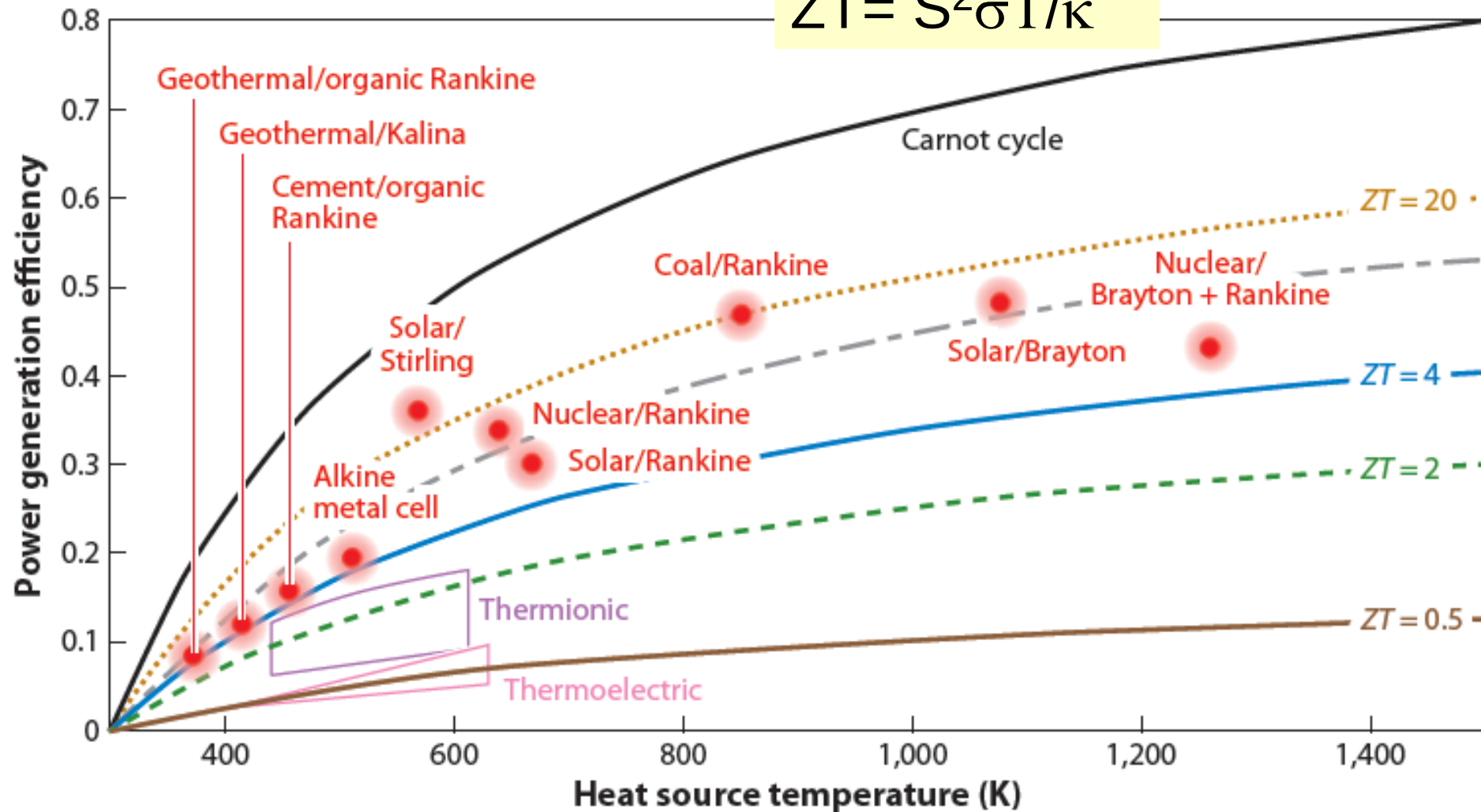
- TE manufacturers provide coolers specifically designed for Telecom laser-cooling and low noise detector/sensor applications



Cronin Vining, ZT Services

Power Generation Efficiencies

$$ZT = S^2 \sigma T / \kappa$$



Adapted from Cronin Vining, Nature Materials 2009

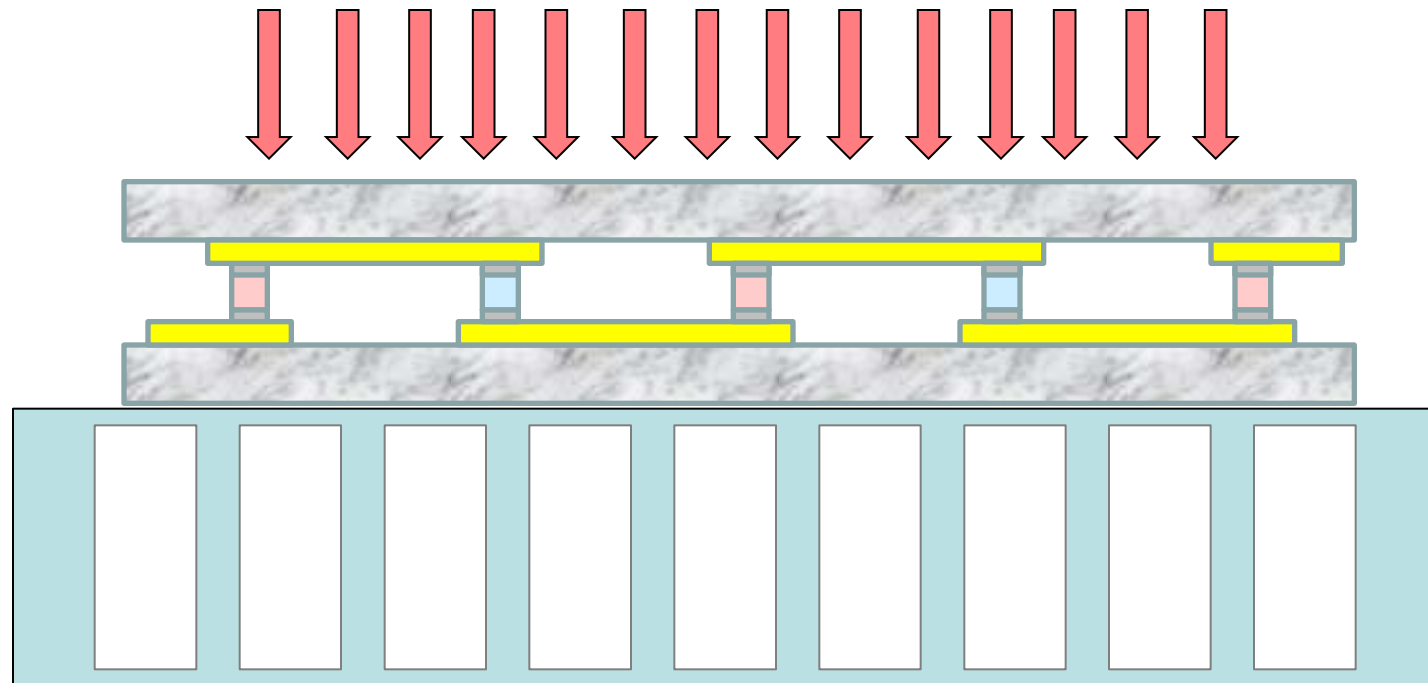
Use of heat spreading inside TE module (thermal concentration)

F = Fractional area coverage
= Area of TE legs divided by
area of the heat source

T_{source} , Input heat flux

TE Module

Heat Sink
(e.g.
microchannel)



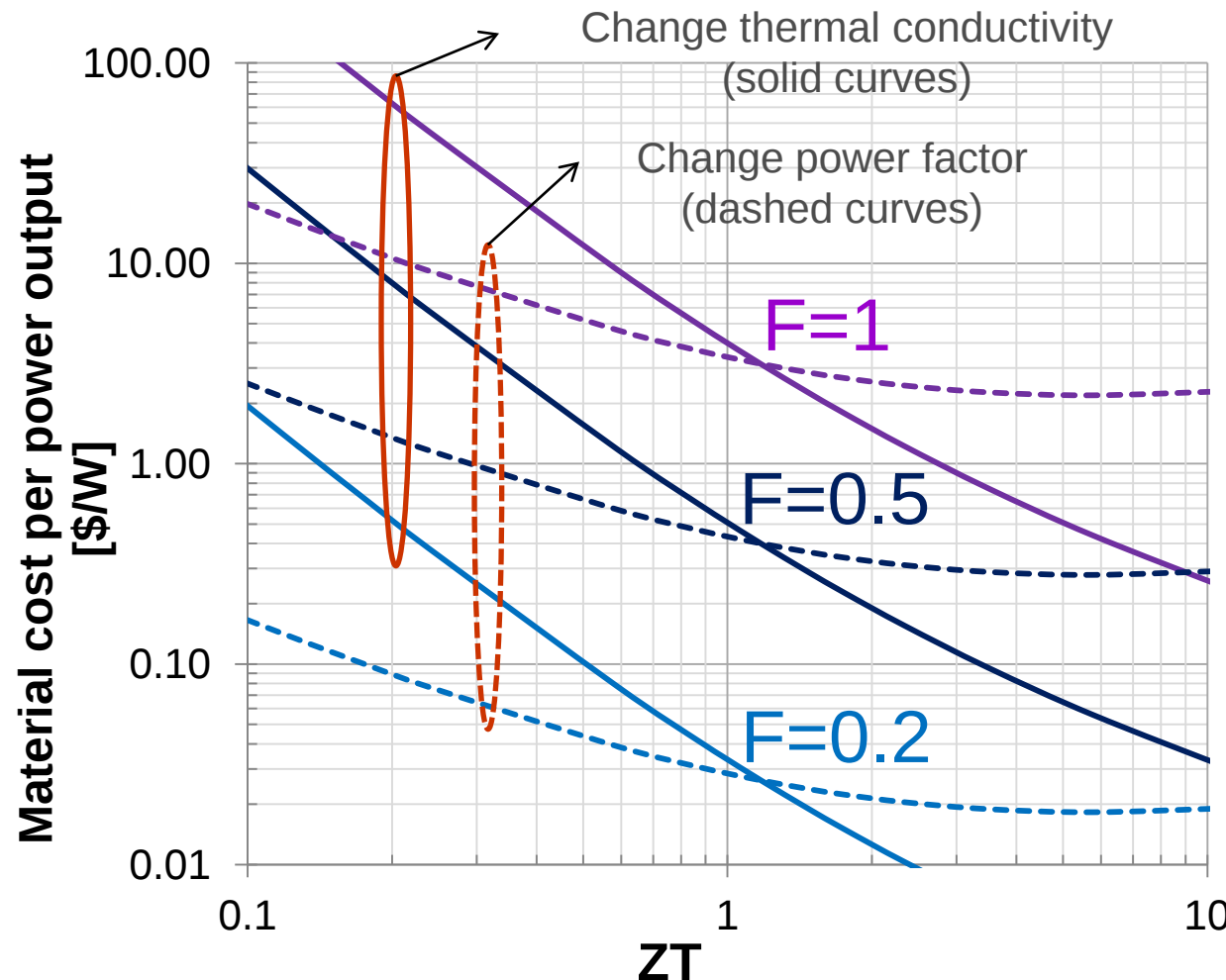
T_{ambient}

Yazawa and Shakouri, Env. Science and Technology (July 2011)

TE Module/Heat Sink Material Cost per Watt (car exhaust application)

Yazawa & Shakouri; Journal of Material Research 2012

DOE/EFRC CEEM Center



$$ZT=1, \quad \beta=1.5 \text{ W/mK}, \\ \beta_{\text{sub}} = 23 \text{ W/mK}, \\ t_{\text{sub}} = 0.2 \text{ mm},$$

$$T_s=900\text{K}, T_a=330\text{K}, \\ \text{Pump efficiency } 30\%$$

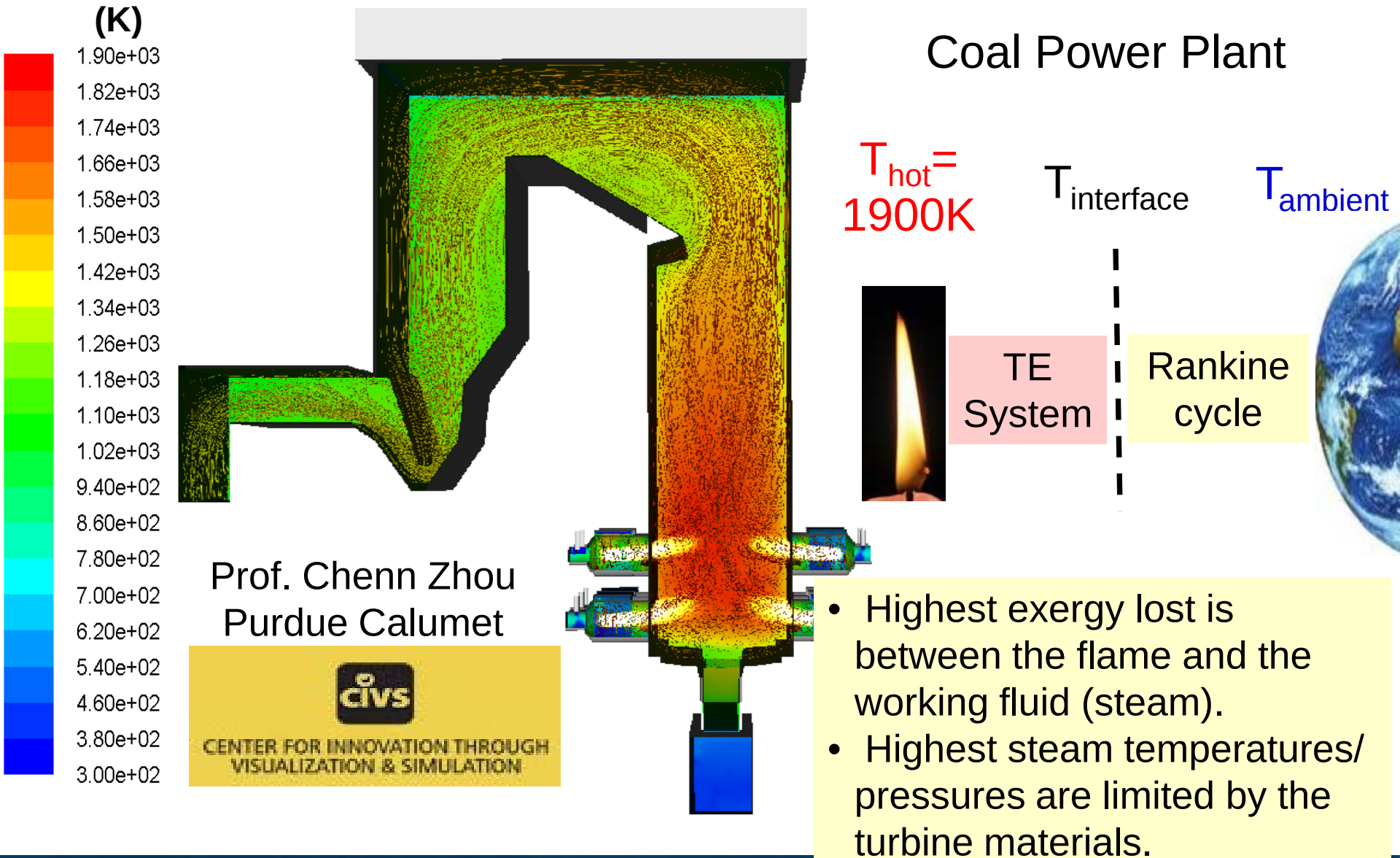
$$\text{TE: } \$500/\text{kg}, \\ \text{Alumina substrate: } \$5/\text{kg}, \\ \text{Copper heat sink: } \$20/\text{kg}$$

$$U_h=4.6 \times 10^2 \text{ W/m}^2\text{K} \\ U_c=1.5 \times 10^3 \text{ W/m}^2\text{K} \quad (U_c/U_h=0.3)$$

- TE material with $ZT=0.5-1$ can have a big impact in high heat flux waste heat recovery applications if the source of heat is free (neglect impact on the topping cycle).

TE for topping cycle applications

Coal Power Plant



$T_{hot} = 1900K$

$T_{interface}$

$T_{ambient}$

TE
System

Rankine
cycle

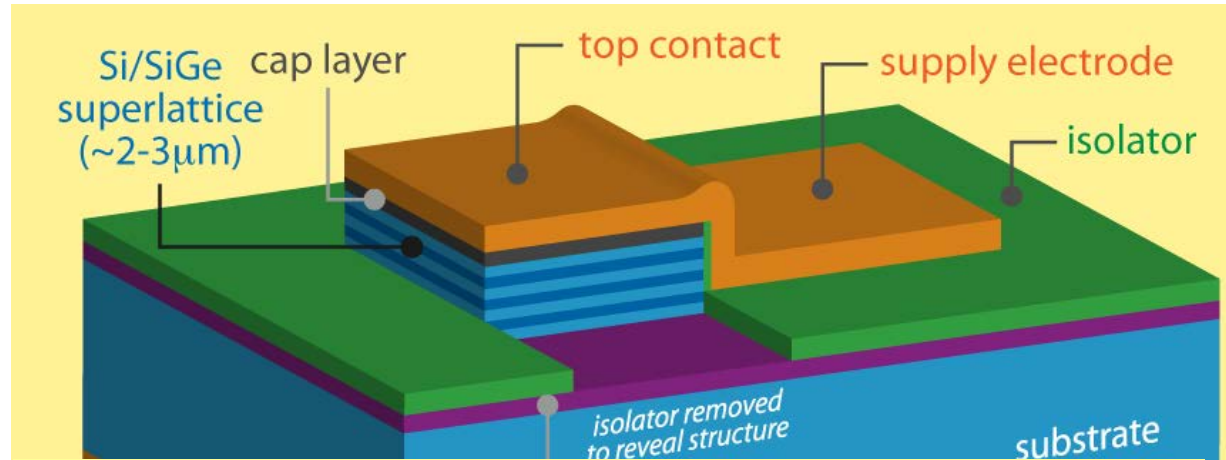
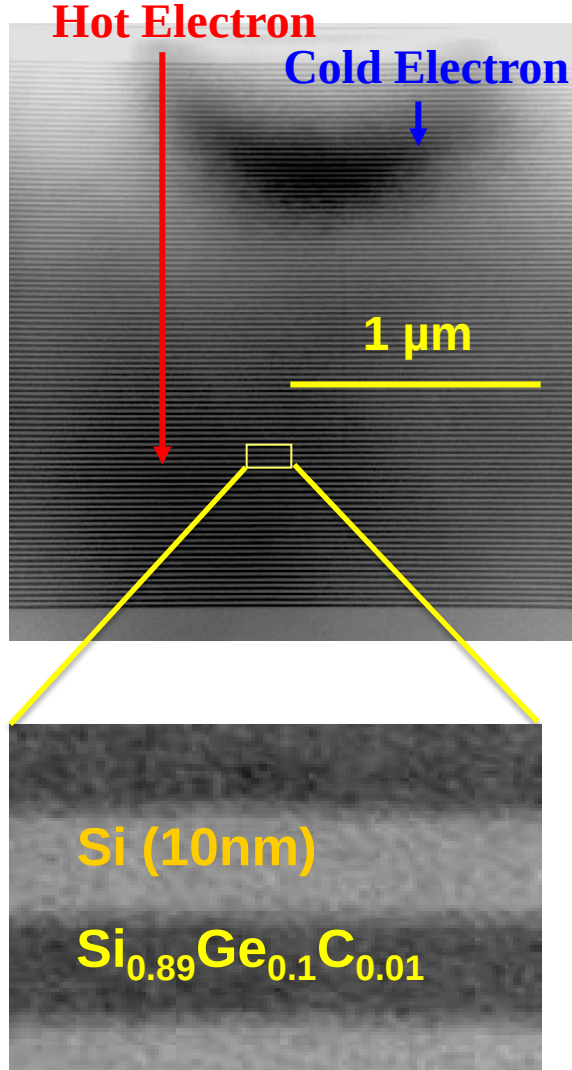
Prof. Chenn Zhou
Purdue Calumet



CENTER FOR INNOVATION THROUGH
VISUALIZATION & SIMULATION

- Highest exergy lost is between the flame and the working fluid (steam).
- Highest steam temperatures/ pressures are limited by the turbine materials.

Microrefrigerators on a chip

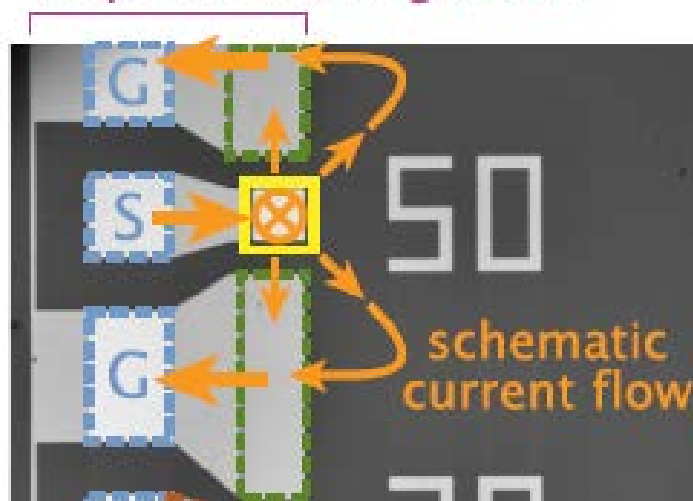


- Monolithic integration on silicon
- $ZT=0.08\text{-}0.1$; $\Delta T_{\text{max}} \sim 4\text{C}$ at room temp. (7C at 100C)
- Cooling power density $> 500 \text{ W/cm}^2$

Heterostructure Integrated Thermionic Coolers; A. Shakouri and John Bowers, **Appl. Phys. Lett.** 1997

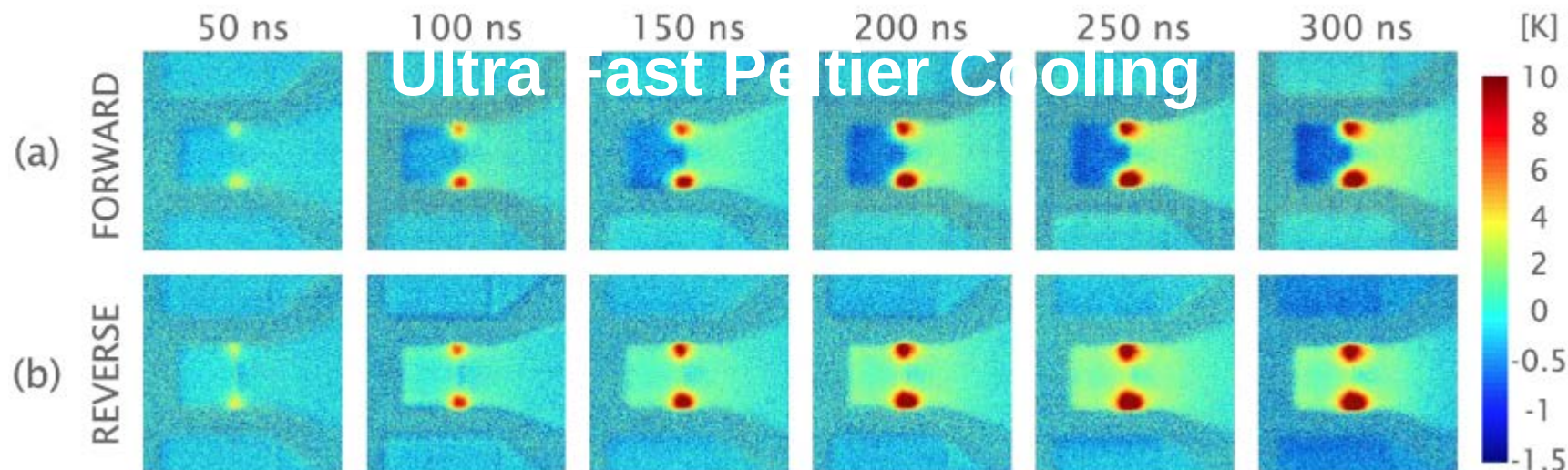
Nanoscale heat transport and microrefrigerators on a chip; A. Shakouri, **Proceedings of IEEE**, July 2006

coplanar waveguides



B. Vermeersch et al. JAP 2013

DURING BIAS PULSE



Material	Seebeck Coefficient, S ($\mu\text{V/K}$)	Electrical Conductivity, σ (Ωcm) ⁻¹	Thermal Conductivity, β (W/mK)	Power Factor, $S^2\sigma$ ($10^{-3}\text{ W/K}^2\text{m}$)	Figure-of-Merit, $ZT = S^2\sigma T/\beta$
Si _{0.8} Ge _{0.2} alloy (Micro refrigerator $\Delta T_{\text{max}}=4.0\text{K}$)	210	367	5.9	1.6	0.08
Superlattice Si/Si _{0.7} Ge _{0.3} (10nm/5nm) (Micro refrigerator $\Delta T_{\text{max}}=3.5\text{K}$)	200 ($\parallel$)	300 ($\parallel$)	10.7-12.9 ($\perp$)	1.8 ($\perp$, estimated) 1.2 ($\parallel$)	0.07 ($\perp$, estimated)
Superlattice Si/Si _{0.75} Ge _{0.25} (3nm/12nm) (Micro refrigerator $\Delta T_{\text{max}}=4.2\text{K}$)	200-220 ($\perp$) 180 ($\parallel$)	384 ($\parallel$)	6.8-8.7 ($\perp$)	2.2 ($\perp$, estimated) 1.2 ($\parallel$)	0.085 ($\perp$, estimated)

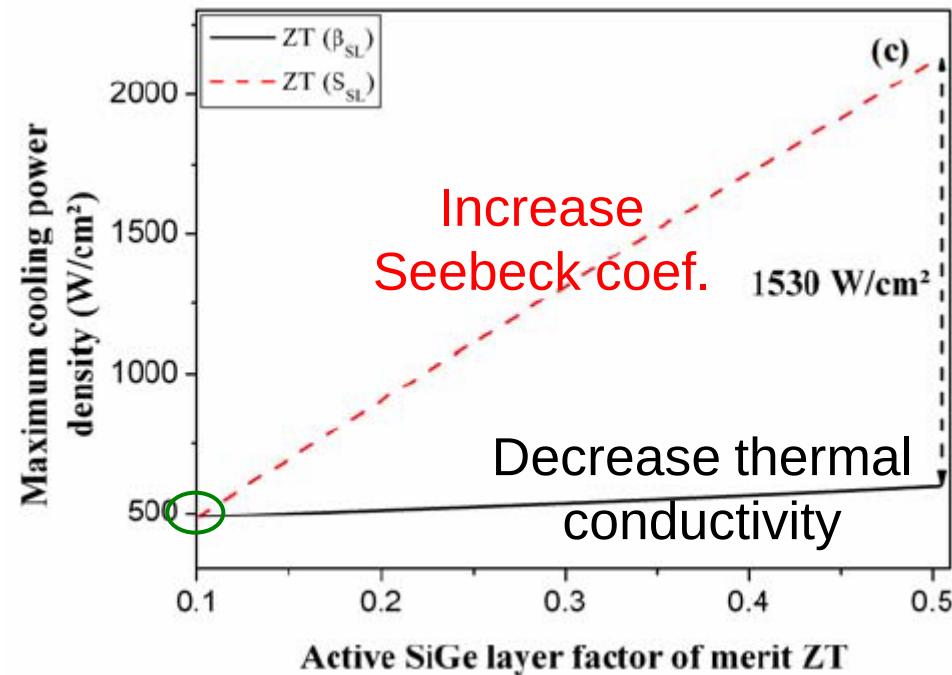
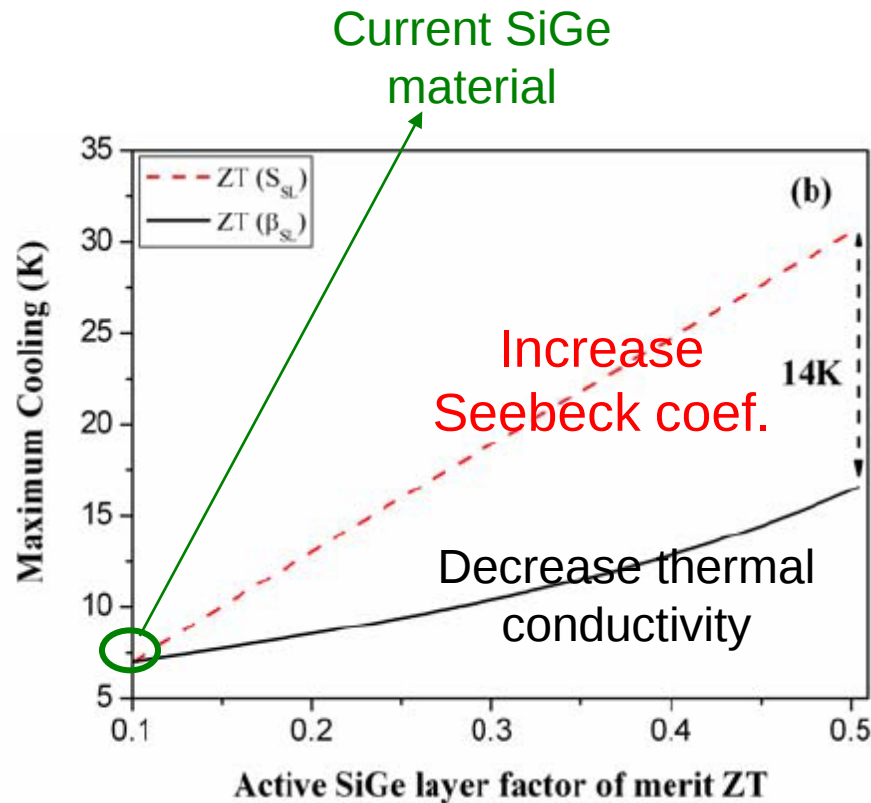
A. Shakouri, **Proceedings of IEEE**, July 2006

Thin Film Microrefrigerator Optimization



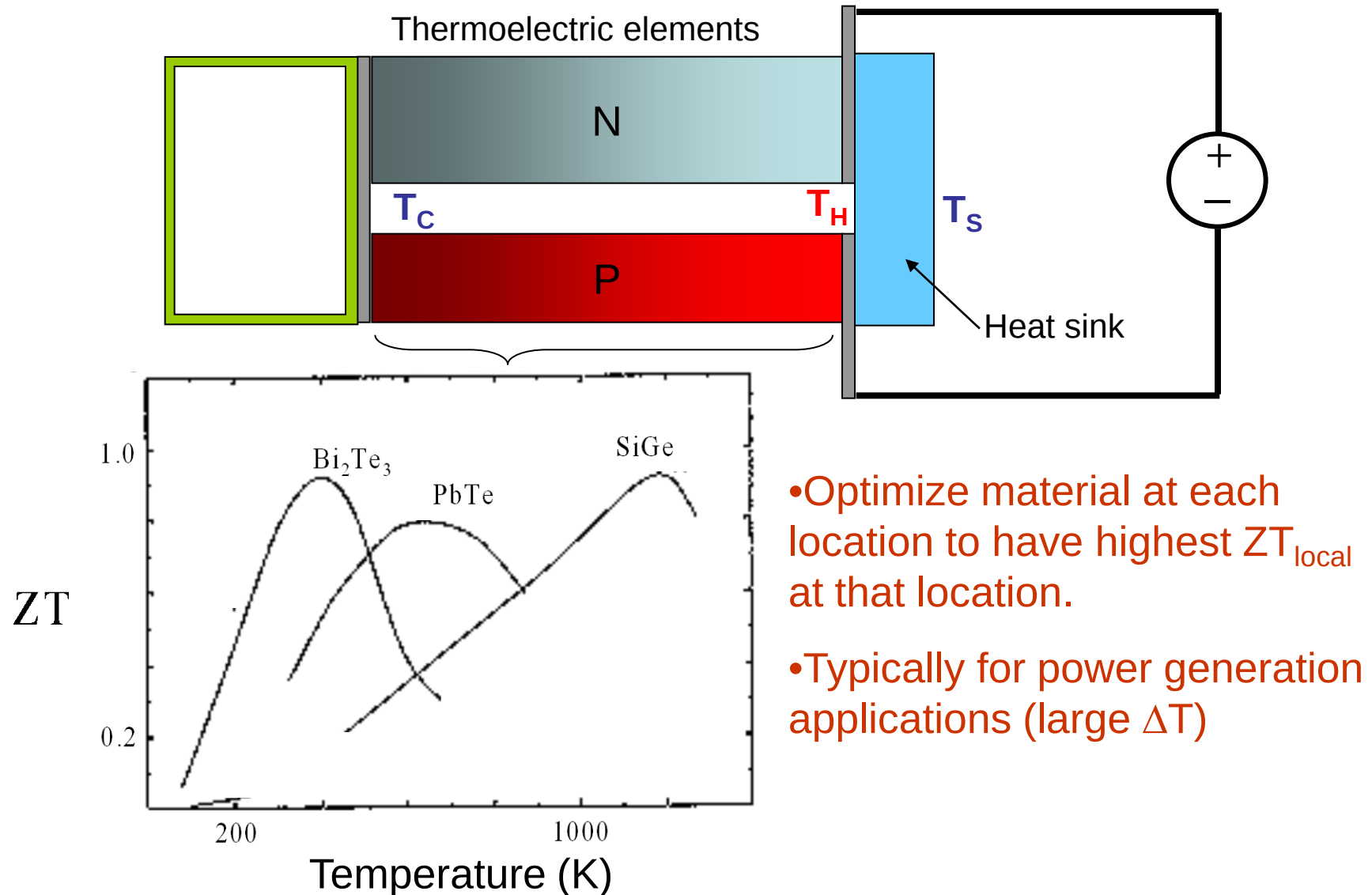
Younes
Ezzahri

10 microns thick, $50 \times 50 \mu\text{m}^2$ monolithic microrefrigerator with $ZT \sim 0.5$ can cool a 1000 W/cm^2 hot spot by $>15^\circ\text{C}$.



Younes Ezzahri, Ali Shakouri et al. InterPACK07, Vancouver, Canada

Conventional Functionally Graded or Segmented Thermoelectric Materials



Thermoelectric properties of a composite medium

David J. Bergman and Ohad Levy

We study the thermoelectric properties of a composite medium. ... We prove that $Z_{\text{effective}}$ of the composite can never exceed the largest value of Z in any component.

(rigorous proof for two-component system)

$$Q_{e11} = \frac{1}{V} \int dV (Q_{11} E_1^{(1)^2} + 2Q_{12} \mathbf{E}_1^{(1)} \cdot \mathbf{E}_2^{(1)} + Q_{22} E_2^{(1)^2})$$

Journal of Applied Physics -- December 1, 1991 – V.70 (11), pp. 6821-6833

Assumption: power factor and thermal conductivity are constant through the materials, small ZT

$$S^2 \sigma = \text{constant}$$

- If $I = ST/R$, Joule heating and Peltier cooling are cancelled inside material



L	L/4	L/9
S	2S	3S
σ	$\sigma/4$	$\sigma/9$
R	R	R

$$\Delta T_{\max} = \frac{1}{2} Z T_c^2 \sum_{n=1} \frac{1}{n^2}$$

n = number of sections

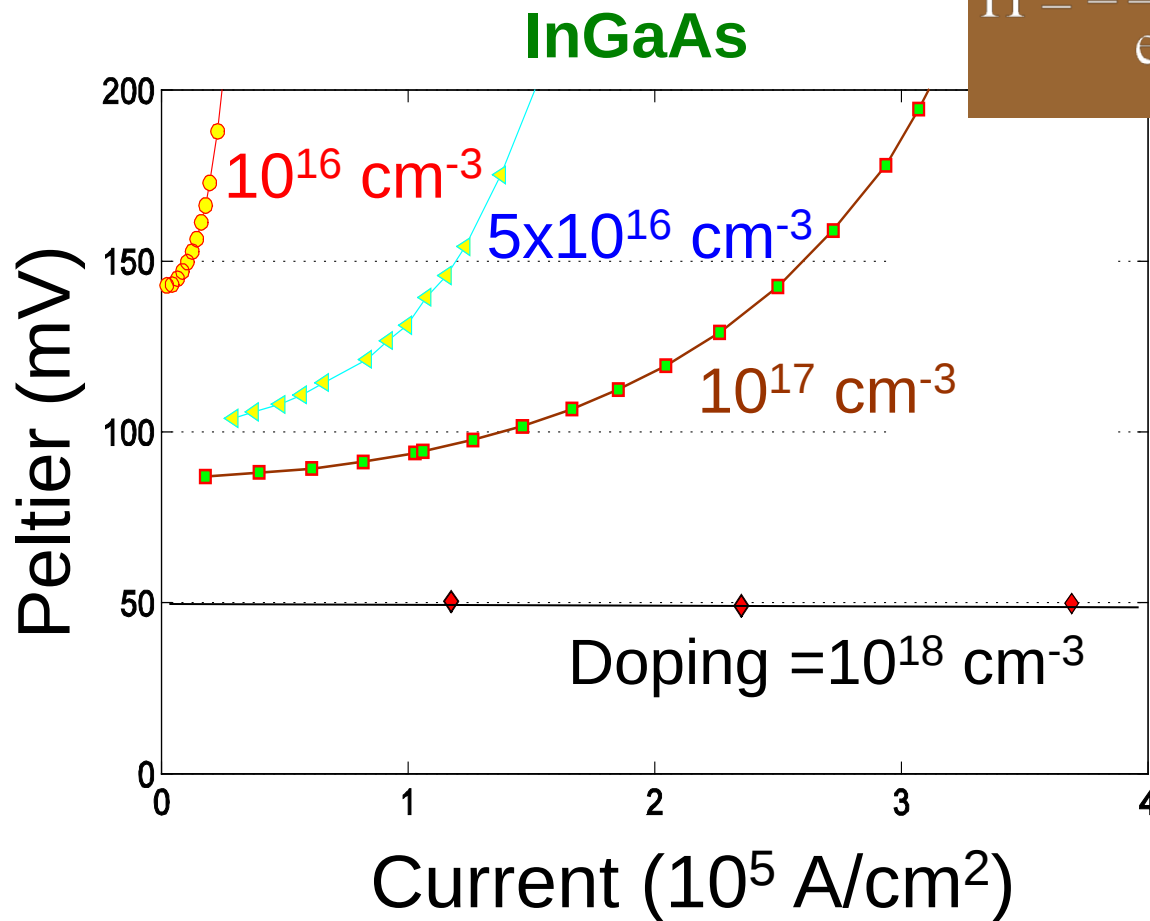
Maximum cooling can be 33-78% times larger for 2-5 sections ($S_{\max}/S_{\min} \sim 10$).

Zhixi Bian et al. Applied Physics Letters 2006



Zhixi Bian

Nonlinear Peltier Coefficient



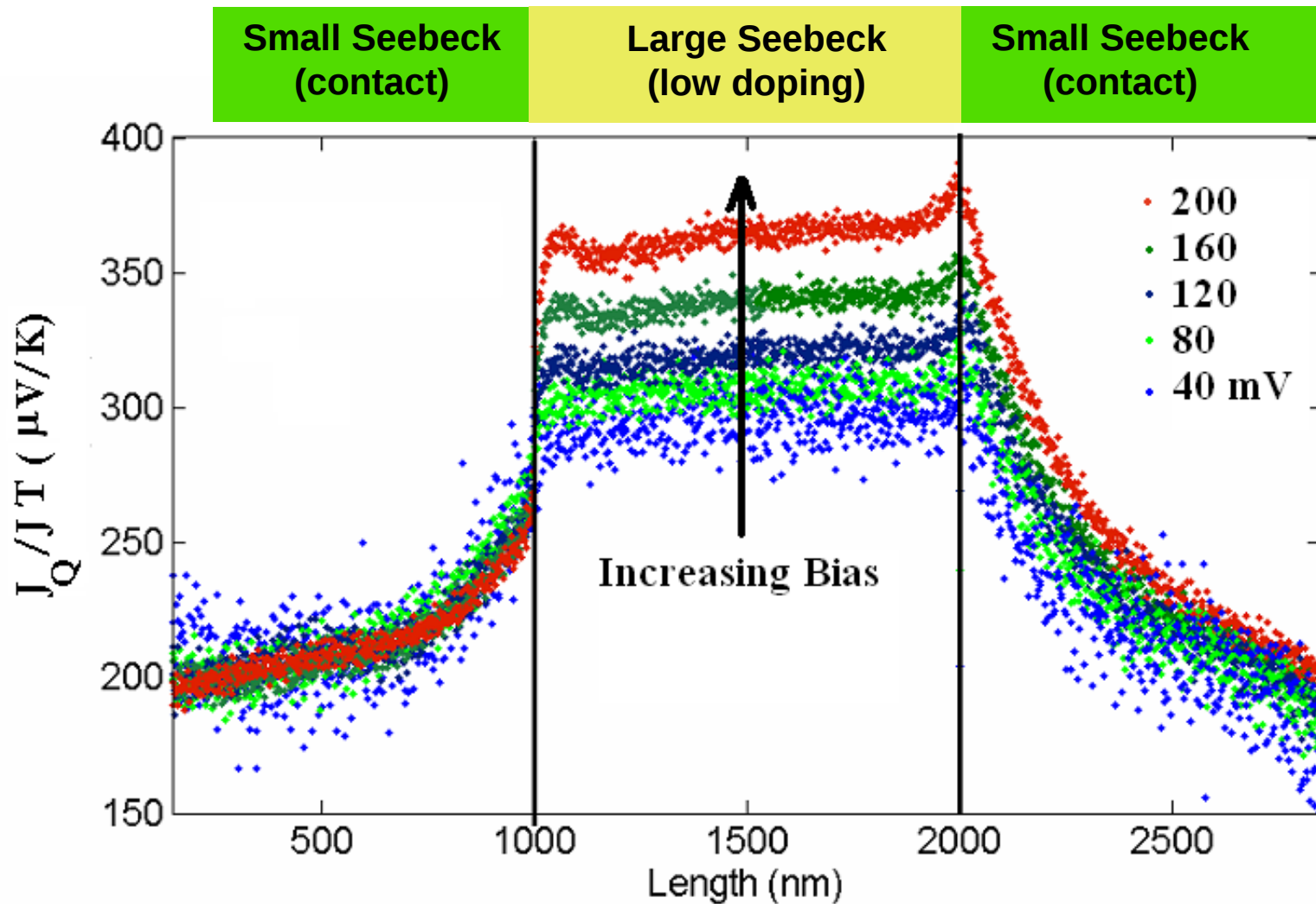
$$\Pi = -\frac{\mu}{e} + \frac{5k_B T}{2e} + \frac{m}{e^3 n^2 \tau} \left(\frac{\tau}{2} + \frac{5\tau_E}{3} \right) J^2$$

Peltier coefficient can increase significantly with bias, especially at low temperatures.



Mona Zebarjadi

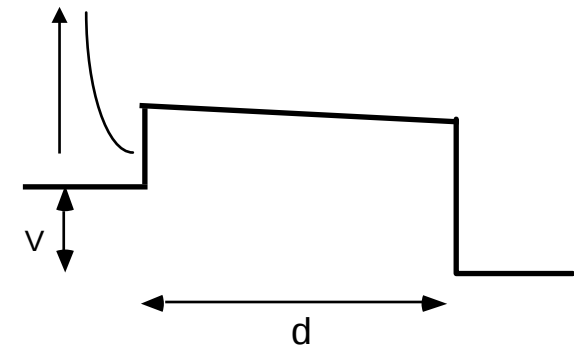
M. Zebarjadi, K. Esfarjani & A. Shakouri, Appl. Phys. Lett., 91, 122104 (2007)

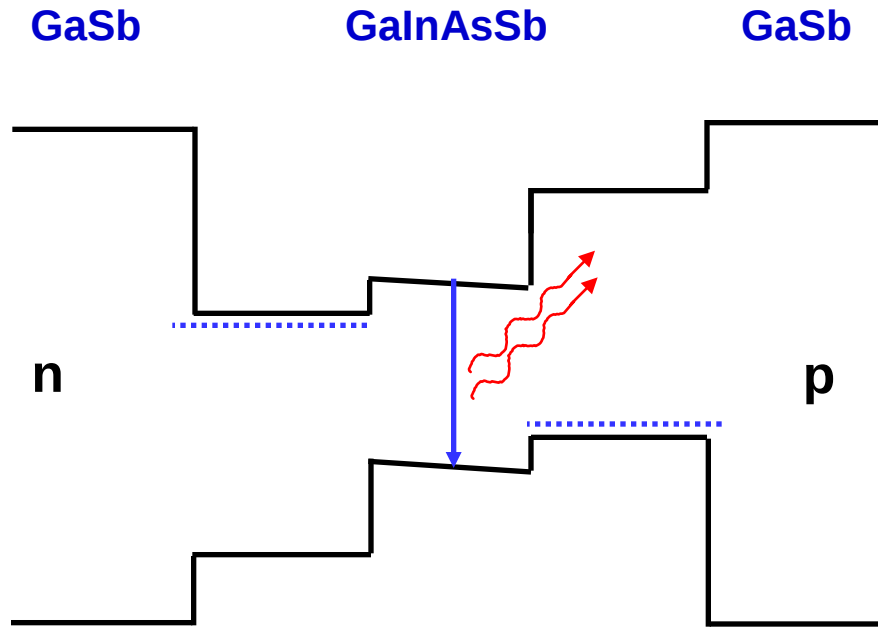


M. Zebarjadi, K. Esfarjani & A. Shakouri, PRB (2007)

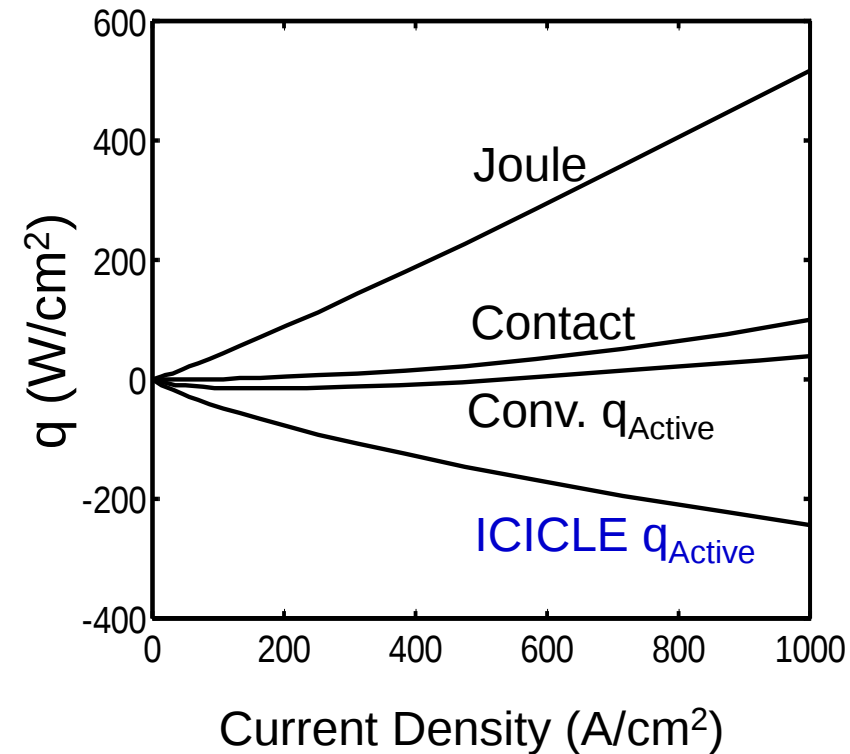
Quest
DISCOVERY PARK

A 3D schematic diagram illustrating a device structure. The structure consists of a blue substrate at the base. A green layer is deposited on top of the substrate. A purple layer, labeled "Isolator removed to reveal structure", is shown being removed from the green layer. The removal process reveals a layered structure on the substrate, which includes a blue layer and a brown layer. The brown layer is shown in two states: one where it is being removed and another where it is fully removed, revealing the underlying blue layer. The green layer is also shown in two states: one where it is being removed and another where it is fully removed, revealing the underlying blue layer. The diagram uses various colors to represent different materials and layers.





**Electrically pumped
“optical refrigeration”**



**Kevin Pipe, Rajeev Ram and Ali Shakouri,
Photonic Techn. Lett., Apr. 2002**

- 4.1 • TE's for waste heat recovery and for localized cooling
- 4.2 • New TE module designs with fractional area coverage can reduce the cost significantly (\$1-2/W $\rightarrow$ \$0.10-0.20/W)
 - Topping cycle thermoelectrics with $ZT \sim 0.3-1$ can improve power plant efficiency by 2-8%
- 4.3 • SiGe Microrefrigerator on a chip (7C cooling)
 - Fully integrated cooler with $ZT \sim 0.5$ can achieve $\Delta T \sim 15C$, cooling power density $> 1kW/cm^2$
- 4.4 • Maximum cooling of Peltier devices can be increased using graded material (uniform efficiency criterion)
 - 3D Peltier devices has high cooling power density
- 4.5 • Nonlinear and bipolar Peltier effects
 - Internal cooling in electronic and optoelectronic devices