

# Fundamentals of Nanotransistors

## Unit 2: MOS Electrostatics

### **Lecture 2.6: Mobile Charge: ETSOI**

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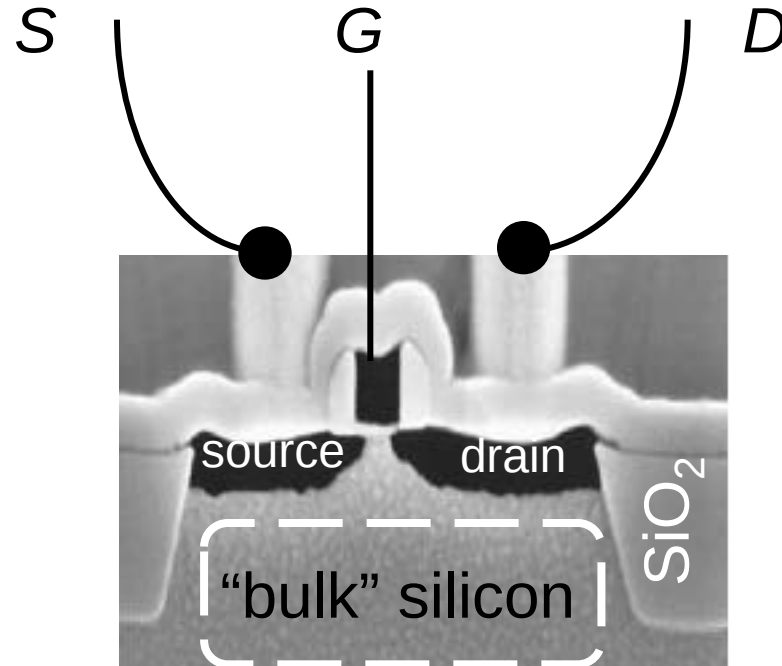
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# Bulk MOSFETs

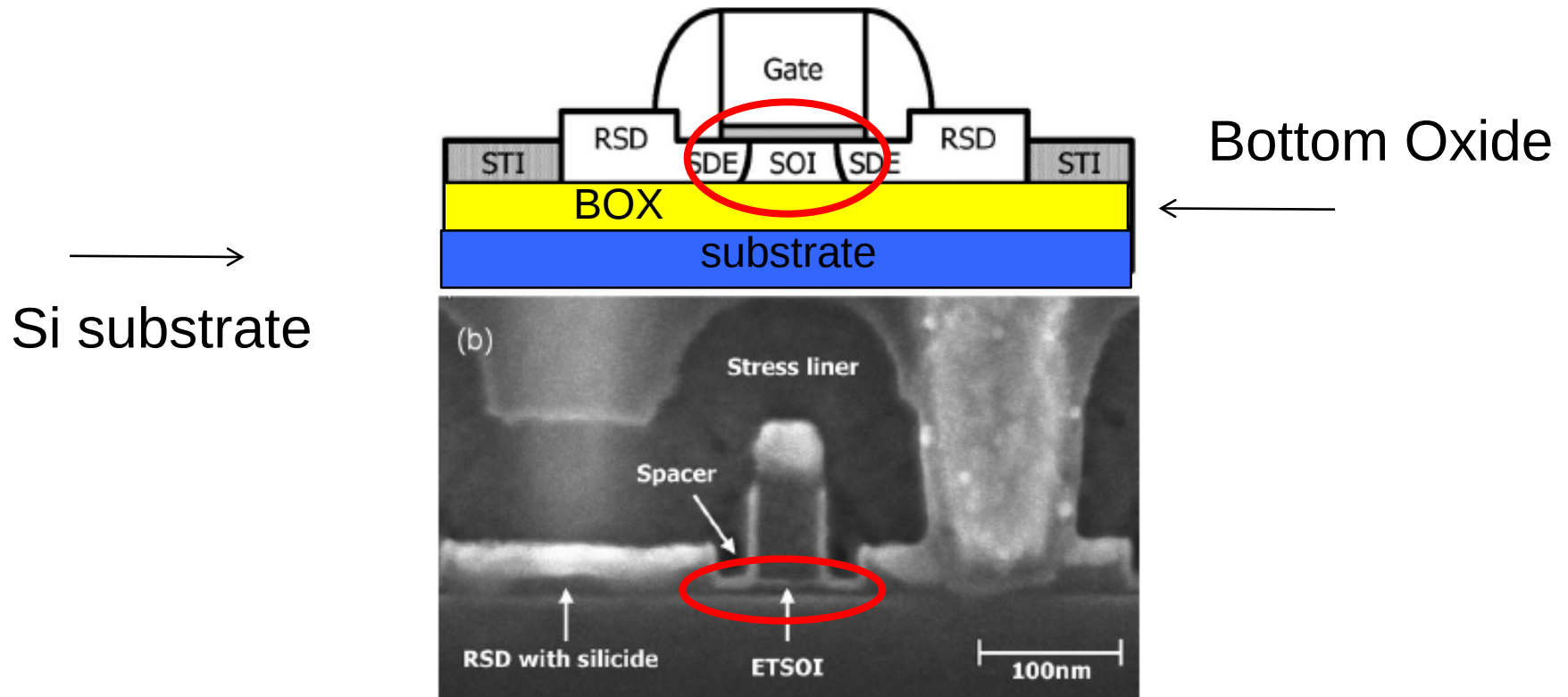
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(Texas Instruments, ~ 2000)

12" wafers are 775 micrometers thick

# Silicon on Insulator (SOI) MOSFETs



A. Majumdar, Z. Ren, S. J. Koester, and W. Haensch, Undoped-Body Extremely Thin SOI MOSFETs With Back Gates, *IEEE Trans. Electron Dev.*, **56**, 2270-2276, 2009.

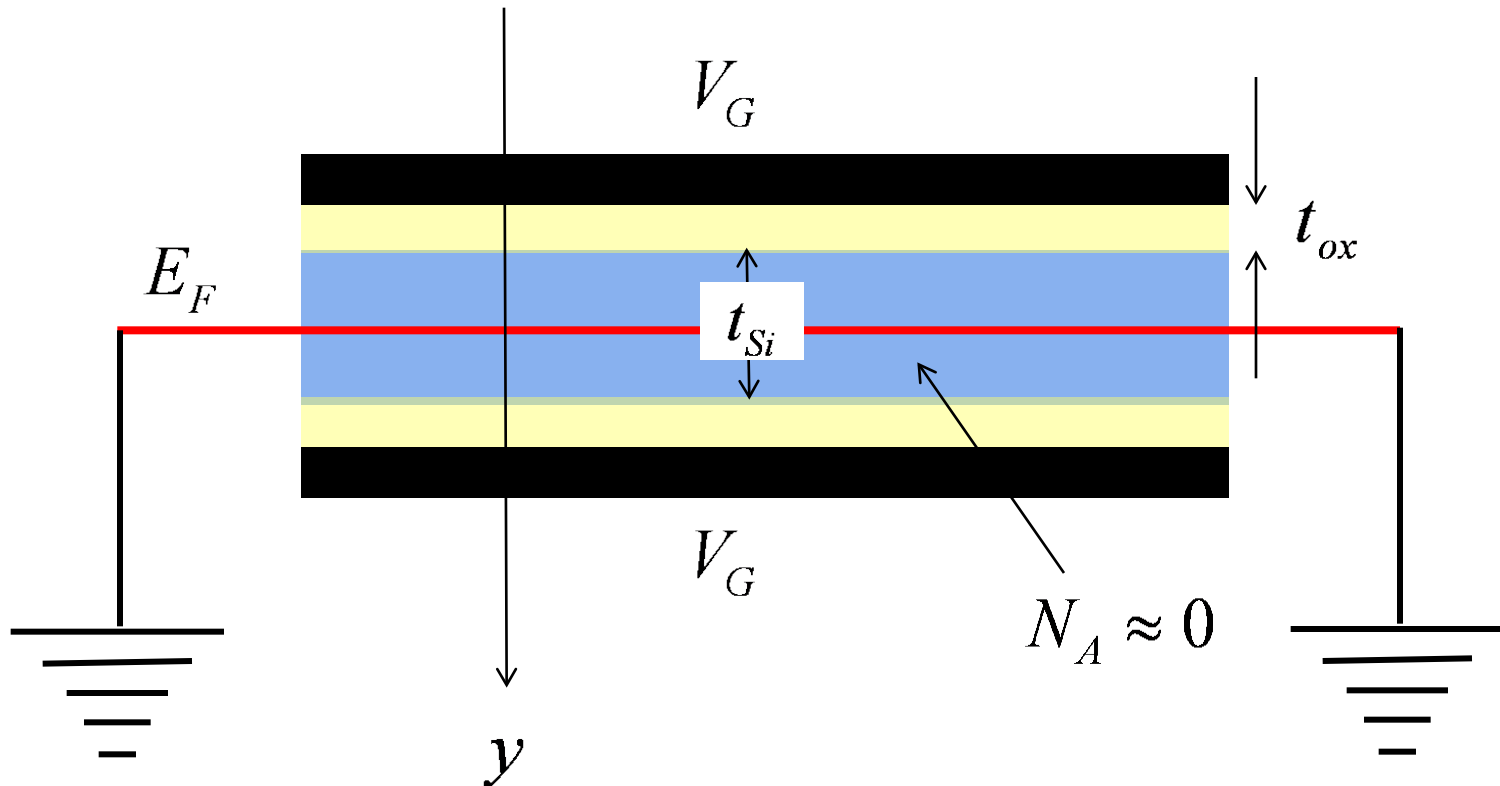
# The question

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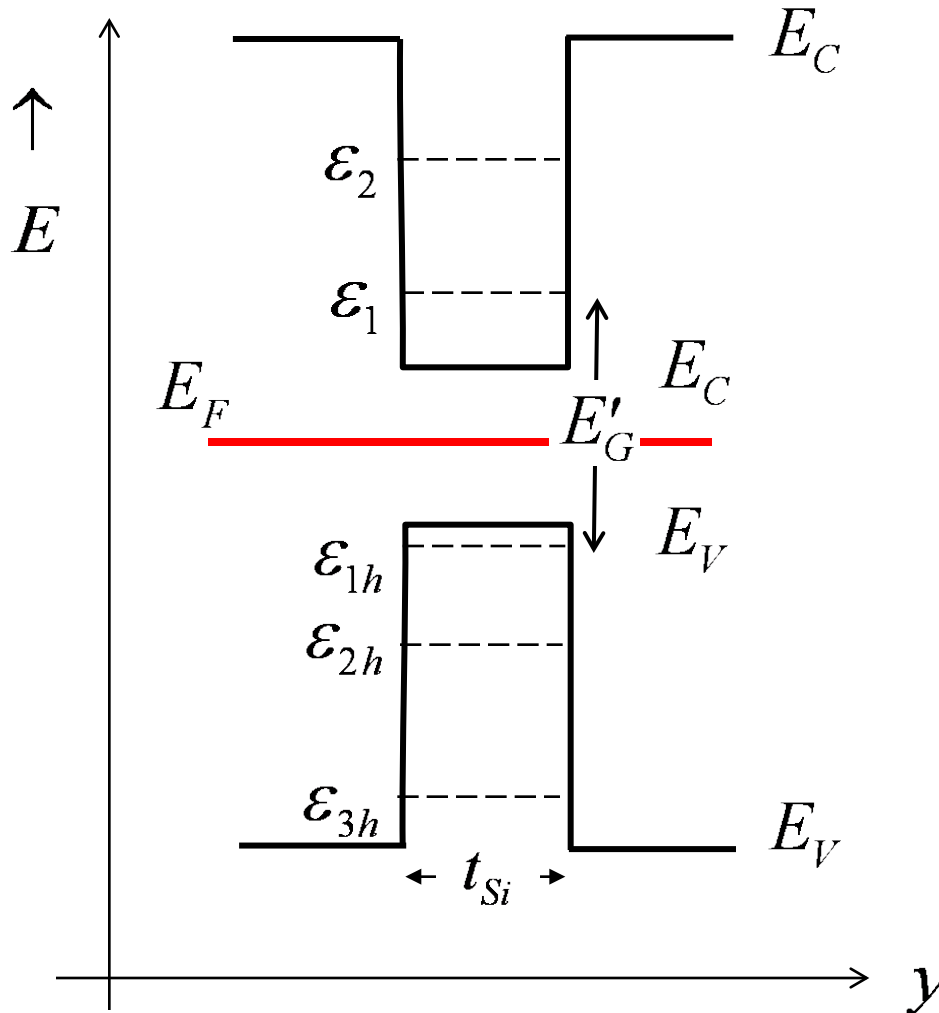
What are the  $Q_n(\psi_S)$  and  $Q_n(V_{GS})$  relations for an **Extremely Thin Silicon On Insulator (ETSOI)** MOSFET?

We will assume a symmetrical, double gate geometry, which makes this discussion relevant to FinFETs as well.

# Extremely-thin body double gate-C



# ETSOI energy band diagram

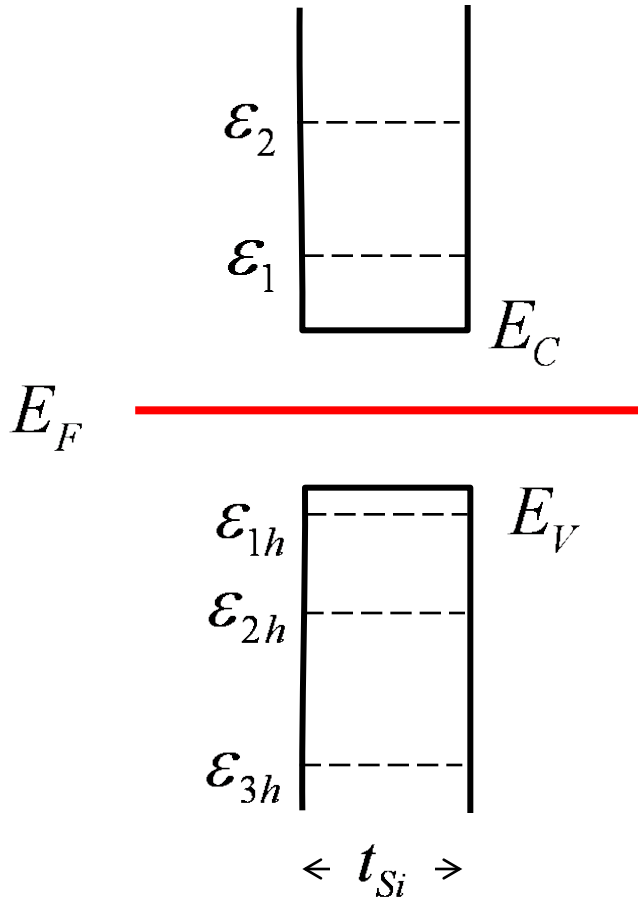


$$\epsilon_n = \frac{\hbar^2 n^2 \pi^2}{2m^* t_{Si}^2}$$

$$E'_G = E_G + \epsilon_1 + \epsilon_{1h}$$

(Neglect band bending, so the potential is constant.)

# 2D carrier densities



$$n_{S1} = N_C^{2D} \mathcal{F}_0(\eta_{F1}) \text{ cm}^{-2}$$

$$N_C^{2D} = g_V \frac{m_n^* k_B T}{\pi \hbar^2} \text{ cm}^{-2}$$

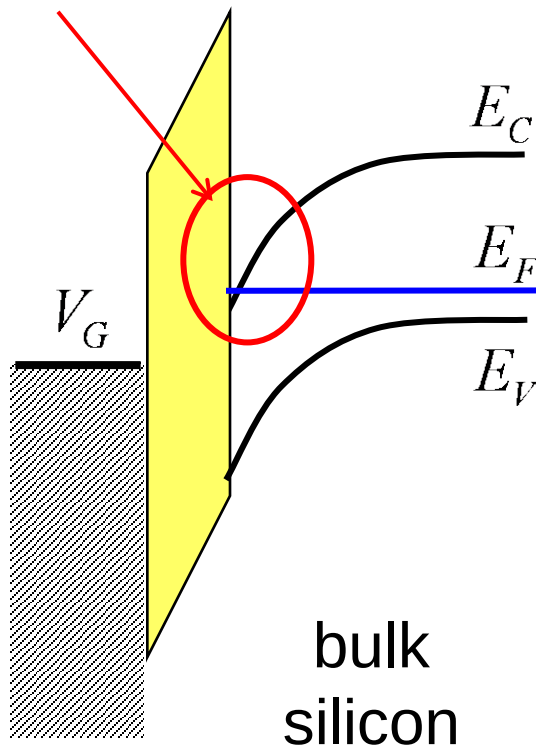
$$\eta_{F1} = \frac{(E_F - E_C - \epsilon_1)}{k_B T}$$

Boltzmann statistics:

$$n_{S1} = N_C^{2D} e^{(E_F - E_C - \epsilon_1)/k_B T} \text{ cm}^{-2}$$

# Quantum confinement in a bulk MOS-C

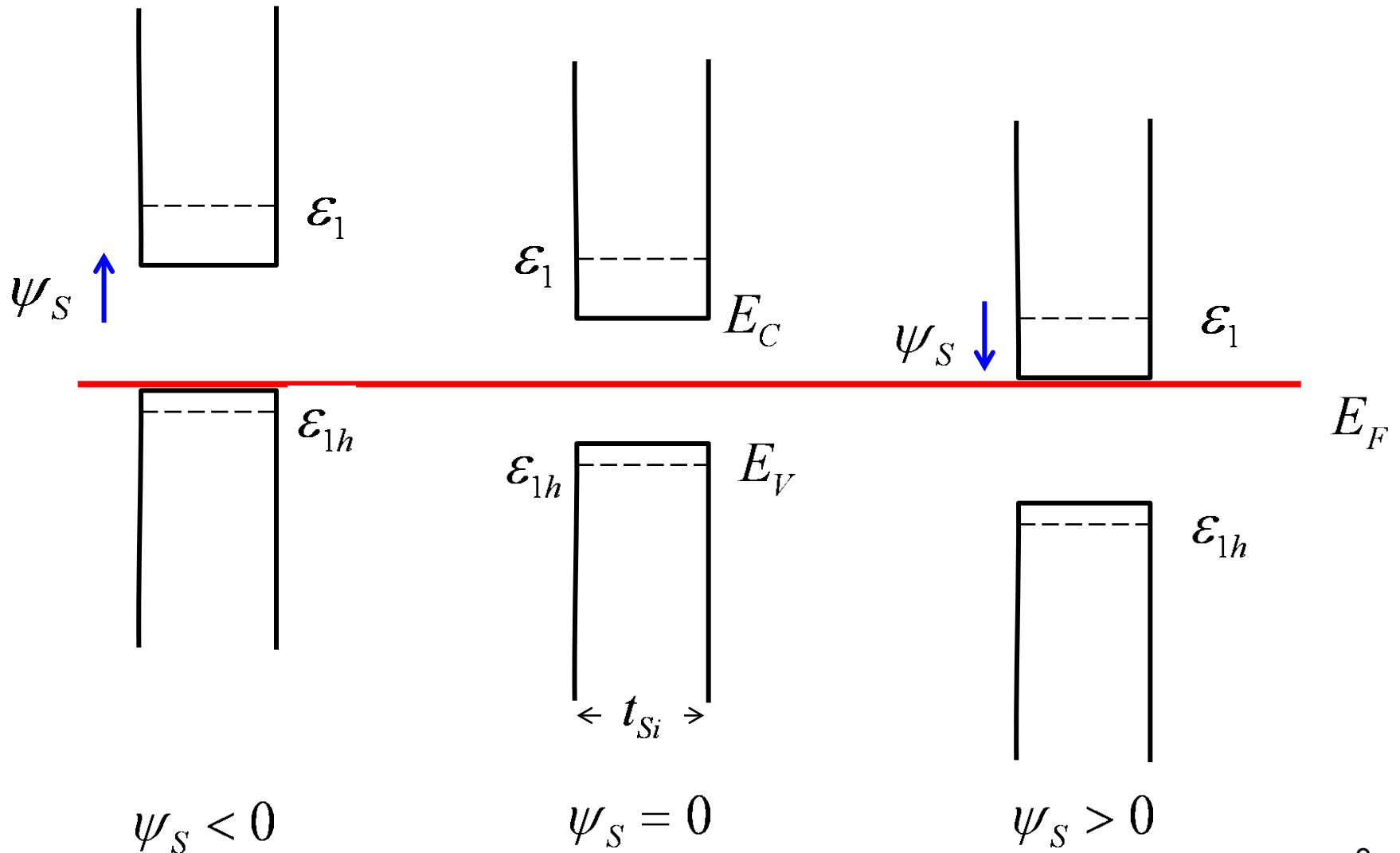
*“quantum well”*



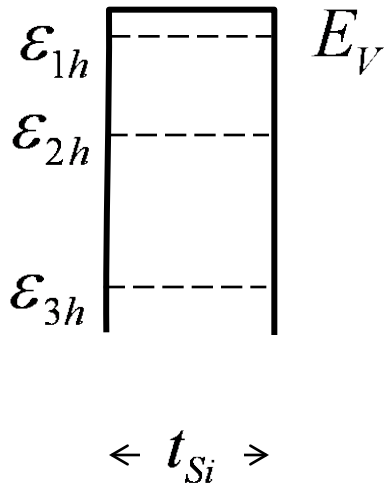
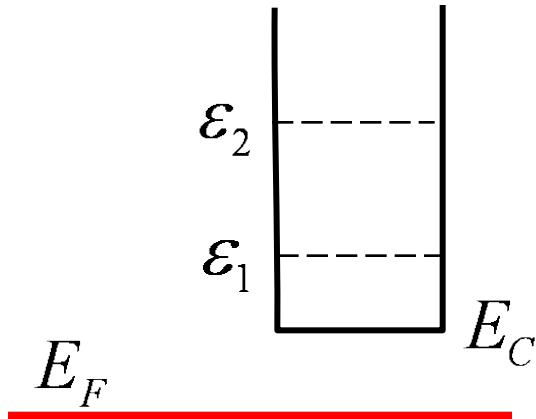
In the bulk, the confining potential is due to electrostatics.

In Extremely Thin SOI, the confining potential is due to the physical structure.

# ETSOI for various potentials



# Carrier densities and potential



$$n_{S1} = N_C^{2D} e^{(E_F - E_C - \epsilon_1)/k_B T} \text{ cm}^{-2}$$

$$E_C = E_{C0} - q\psi_S$$

$$n_{S1} = N_C^{2D} e^{(E_F - E_{C0} - \epsilon_1 + q\psi_S)/k_B T}$$

$$n_{S1} = N_C^{2D} e^{(E_F - E_{C0} - \epsilon_1)/k_B T} e^{q\psi_S/k_B T}$$

$$n_S = n_{S0} e^{q\psi_S/k_B T}$$

$$p_S = p_{S0} e^{-q\psi_S/k_B T}$$

(These eqns. assume that only 1 subband is occupied.)

# Mobile sheet charge (per cm<sup>2</sup>)

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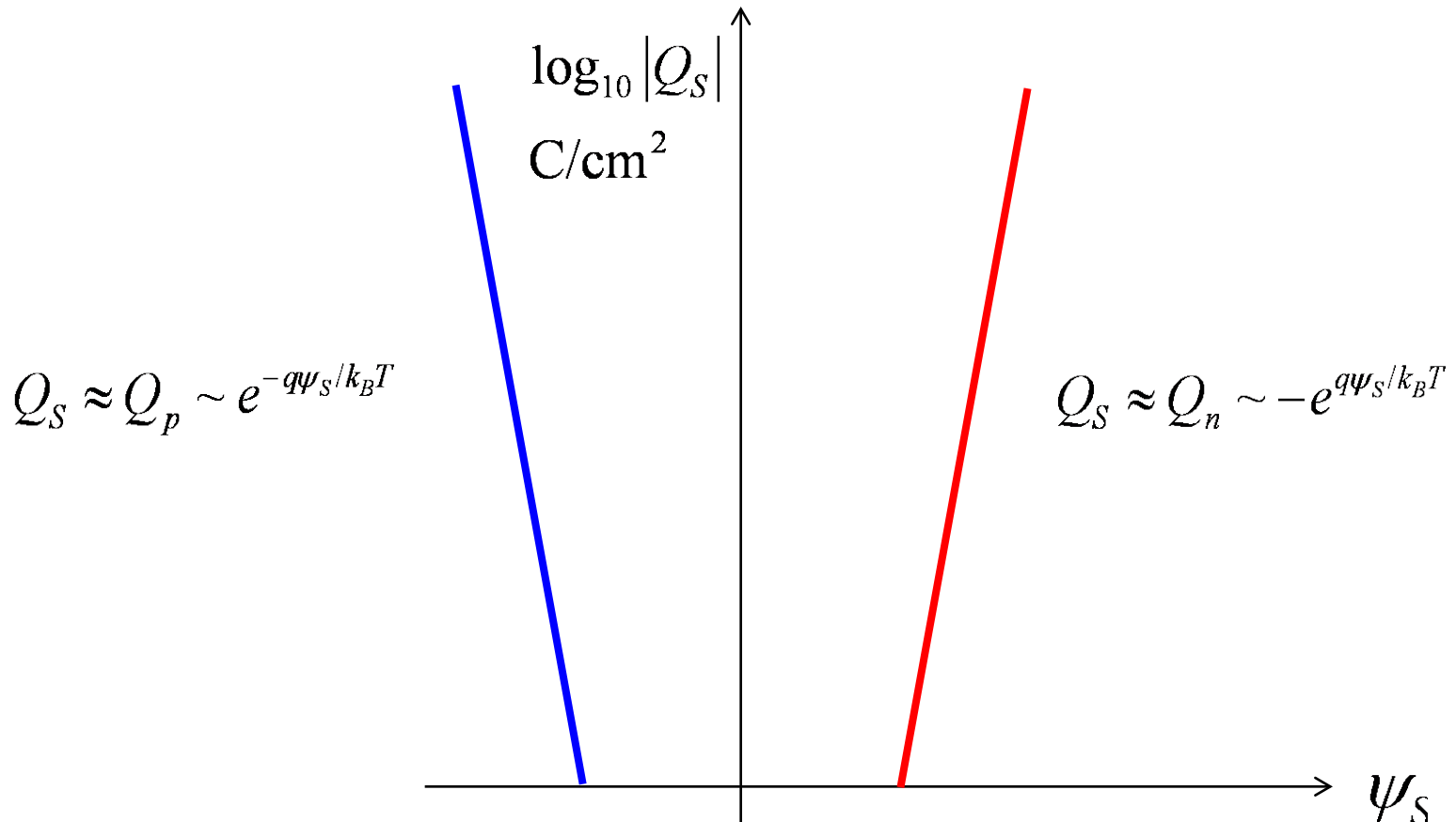
$$Q_s = q(p_s - n_s) \quad \text{C/cm}^2$$

$$Q_n(\psi_s) = -qn_{s0} e^{q\psi_s/k_B T}$$

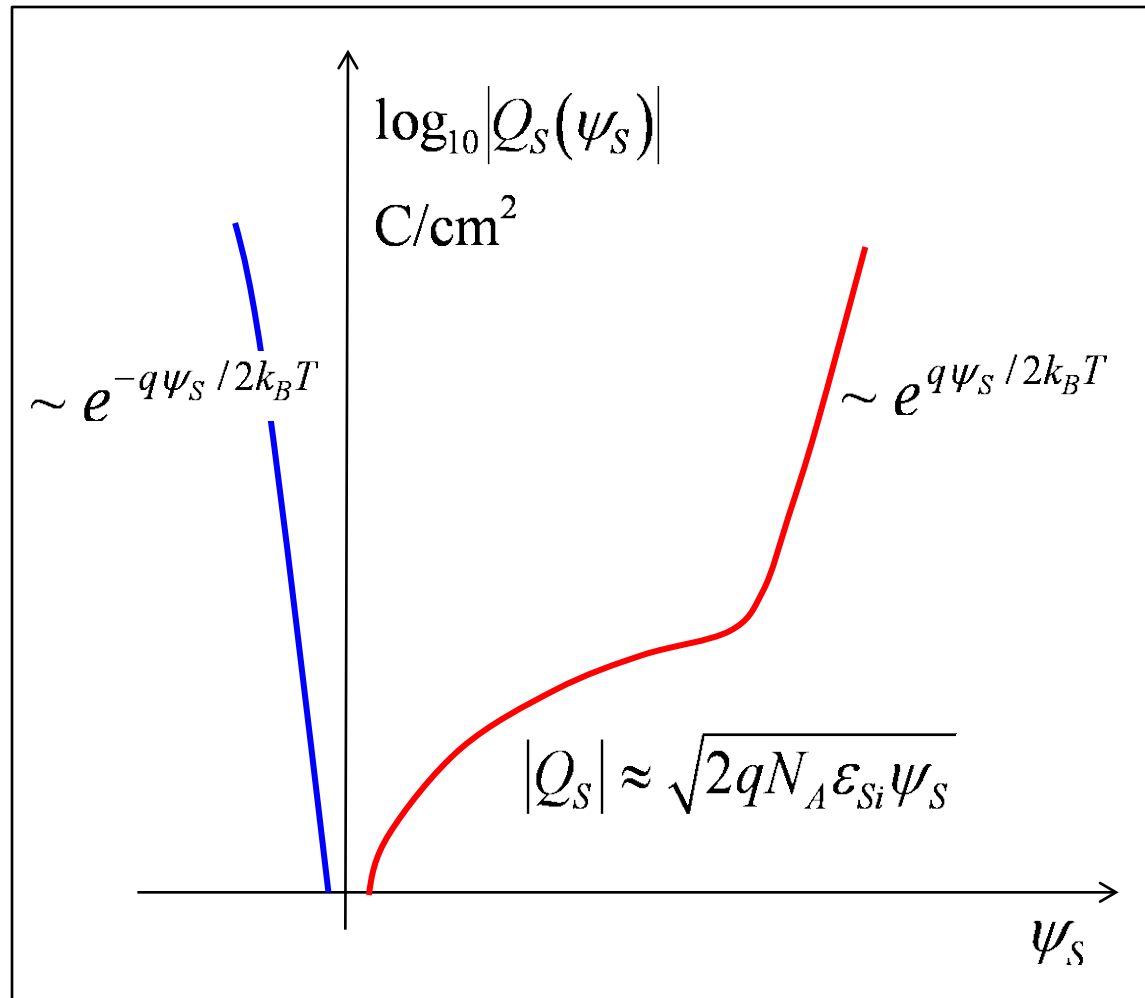
Valid above and below threshold.

# Charge vs. potential

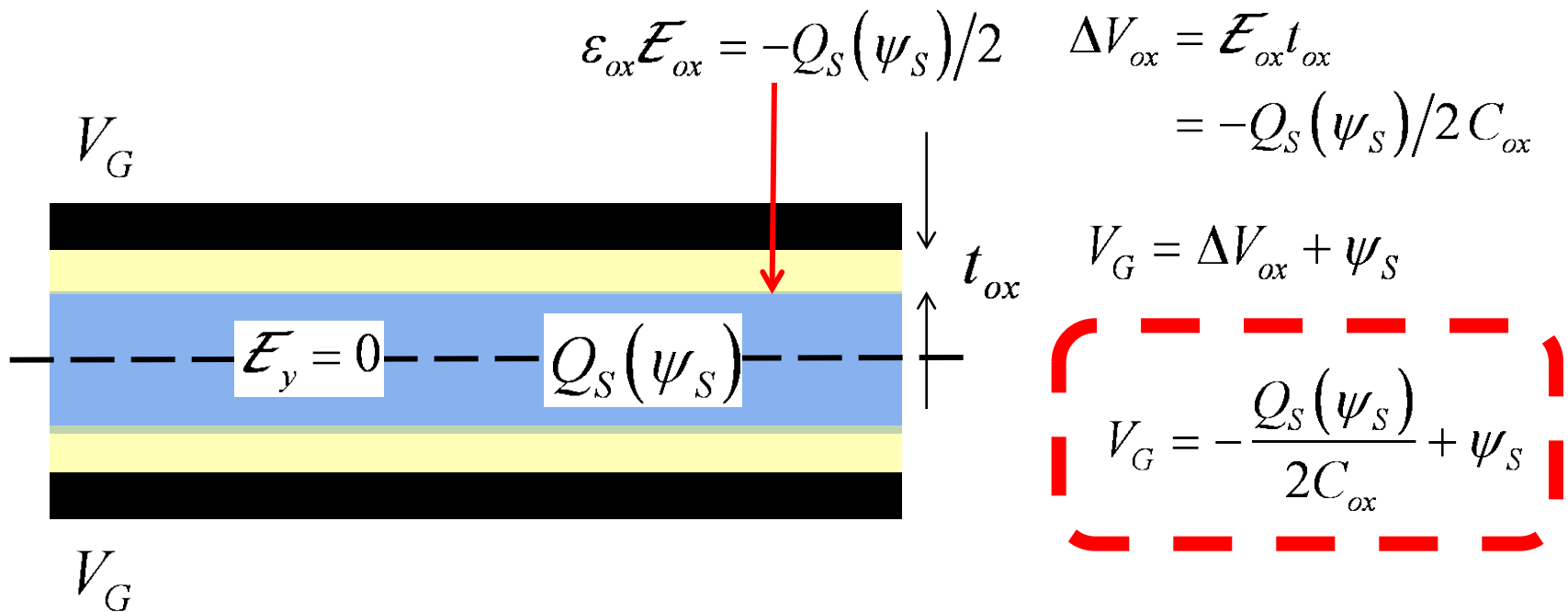
$$Q_S(\psi_S) = q(p_{S0} e^{-q\psi_S/k_B T} - n_{S0} e^{q\psi_S/k_B T})$$



# Recall: $Q_S(\psi_S)$ for bulk MOS



# Gate voltage vs. potential



**subthreshold**

$$V_G = -\frac{Q_S(\psi_S)}{2C_{ox}} + \psi_S \quad Q_S(\psi_S) \approx 0 \rightarrow V_G \approx \psi_S$$

$$\psi_S = \frac{V_G}{m} \quad \text{bulk}$$

$$m = 1 + C_D / C_{ox}$$

# Subthreshold charge vs. gate voltage

$$Q_n(\psi_s) = -qn_{s0} e^{q\psi_s/k_B T} \quad V_G \approx \psi_s \quad (\text{subthreshold})$$

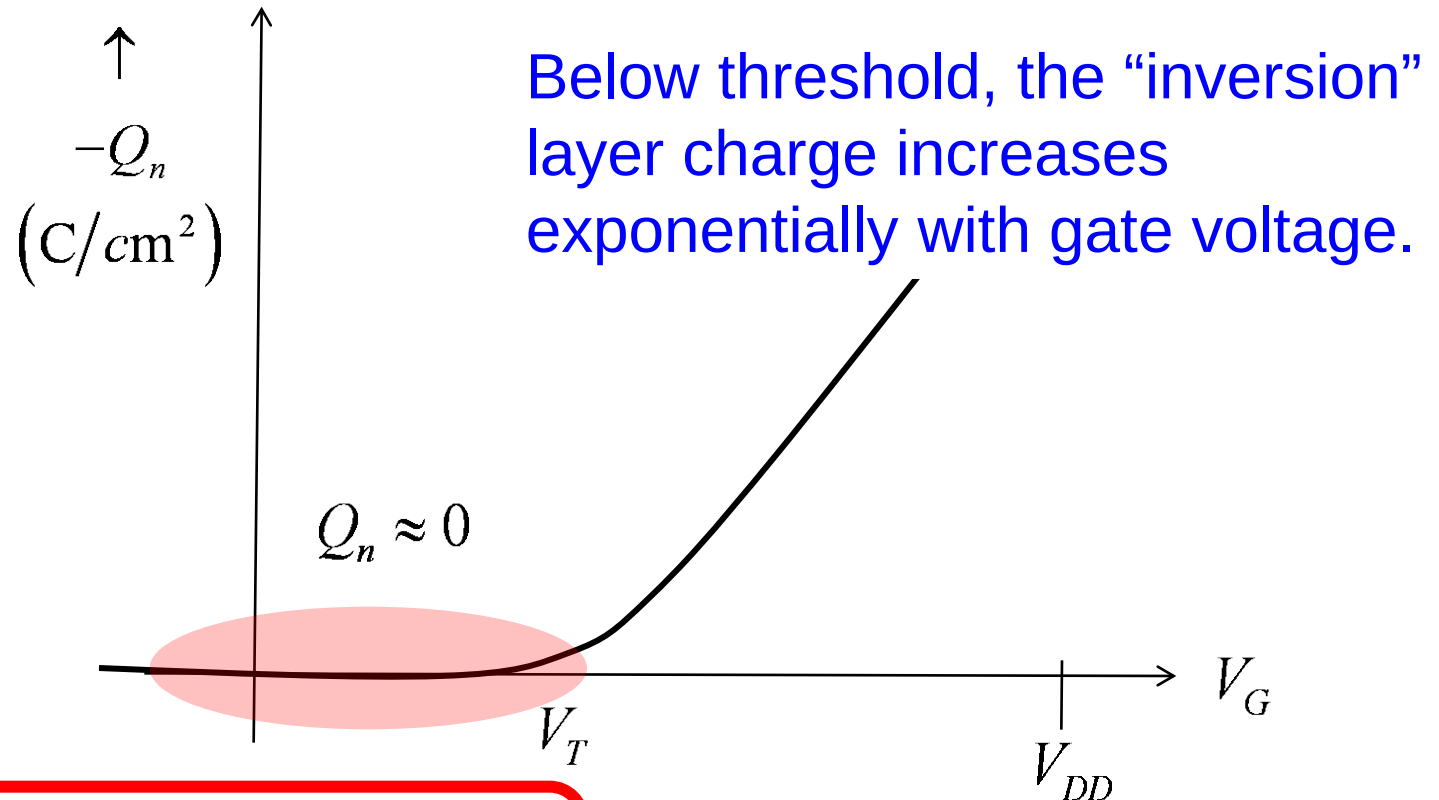
$$Q_n(V_G) \approx -qn_{s0} e^{qV_{GS}/k_B T} \quad m = 1$$

$$Q_n(V_G) \approx -C_Q \left( \frac{k_B T}{q} \right) e^{q(V_G - V_T)/k_B T} \quad V_T \equiv \frac{k_B T}{q} \ln \left( \frac{N_C^{2D}}{n_{s0}} \right)$$

“quantum capacitance”

$$C_Q \equiv q^2 D_{2D}(E_F)$$

# Subthreshold charge vs. gate voltage

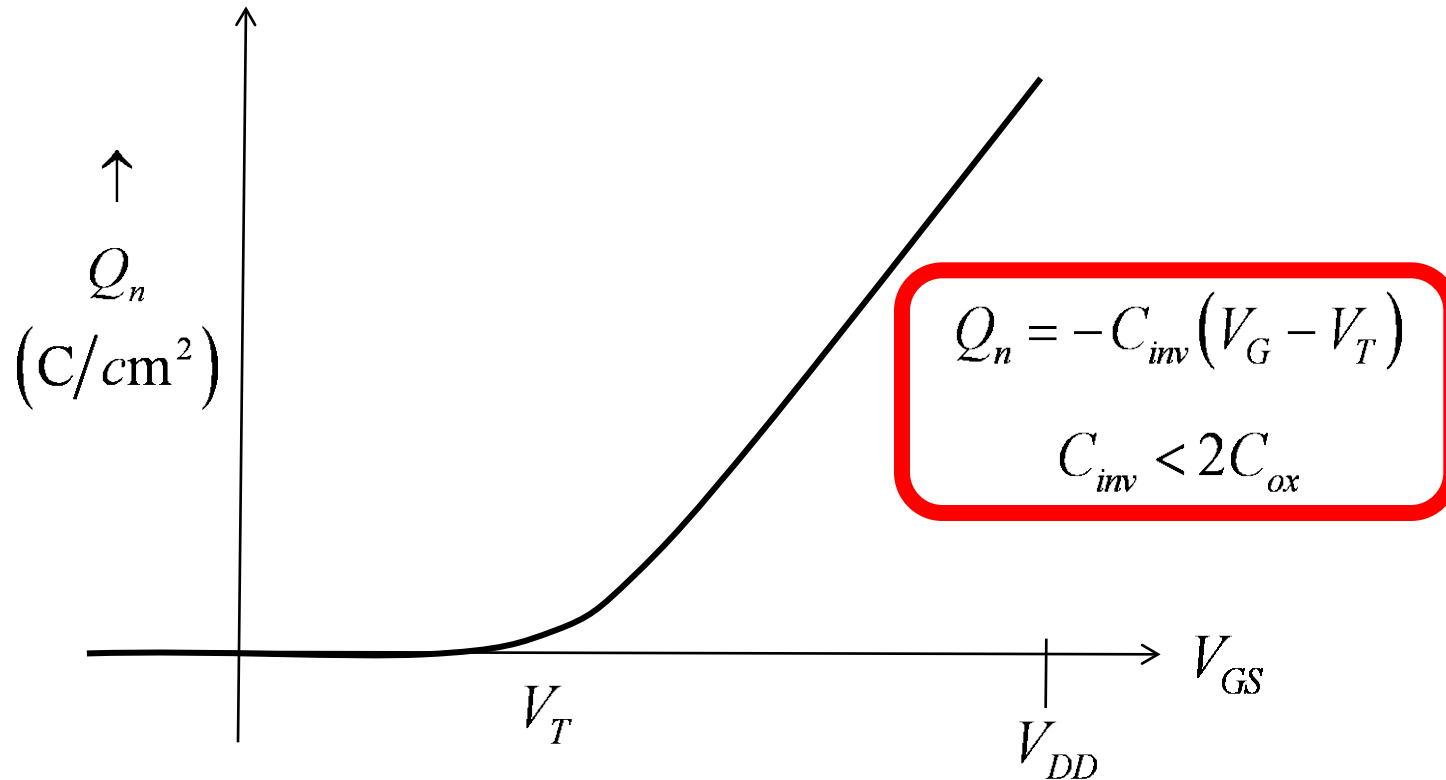


$$Q_n(V_G) \approx -C_Q \left( \frac{k_B T}{q} \right) e^{q(V_G - V_T)/k_B T}$$

$$Q_n(V_G) = -(m-1)C_{ox} \left( \frac{k_B T}{q} \right) e^{q(V_G - V_T)/mk_B T}$$

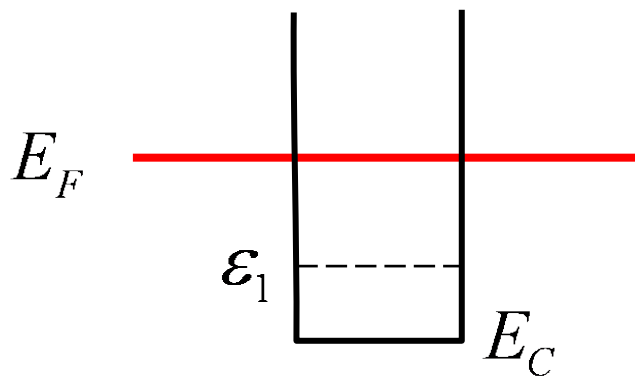
(bulk MOS)

# Charge vs. gate voltage **above threshold**



$$\frac{1}{C_{inv}} = \frac{1}{2C_{ox}} + \frac{1}{C_S(\text{inv})} \qquad C_S = \frac{d(-Q_S)}{d\psi_S}$$

# Quantum capacitance ( $T = 0$ K)



$$n_S = D_{2D} (E_F - E_C - \varepsilon_1)$$

$$E_C = E_{C0} - q\psi_S$$

$$n_S = D_{2D} (E_F - E_{C0} + q\psi_S - \varepsilon_1)$$

$$C_S = \frac{d(-Q_n)}{d\psi_S} = \frac{d(qn_S)}{d\psi_S} = q^2 D_{2D} = C_Q$$

$$C_{inv} = \frac{2C_{ox}C_Q}{2C_{ox} + C_Q} < 2C_{ox}$$

$$C_Q = q^2 D_{2D}$$

# Mobile charge vs. gate voltage

$$V_G \ll V_T : \quad Q_n(V_G) = -C_Q \left( \frac{k_B T}{q} \right) e^{q(V_G - V_T)/k_B T} \quad \text{ETSOI}$$

$$V_G \gg V_T : \quad Q_n(V_G) = -C_{inv}(V_G - V_T) \quad C_{inv} \approx 2C_{ox}$$

$$V_G \ll V_T : \quad Q_n(V_G) = -(m-1)C_{ox} \left( \frac{k_B T}{q} \right) e^{q(V_G - V_T)/mk_B T} \quad \text{bulk}$$

$$V_G \gg V_T : \quad Q_n = -C_{inv}(V_G - V_T) \quad C_{inv} \approx C_{ox}$$

# Aside

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$$SS = \left( \left. \frac{\partial \log_{10} I_{DS}}{\partial V_{GS}} \right|_{V_{DS}} \right)^{-1} = 2.3mk_B T$$

$m = 1$  for fully depleted structures.

# Summary

We have considered 1D MOS electrostatics – in the direction normal to the channel.

We now understand how the mobile charge varies with gate voltage above and below threshold.

**Next Lecture:** How does two-dimensional electrostatics affect MOSFETs?

