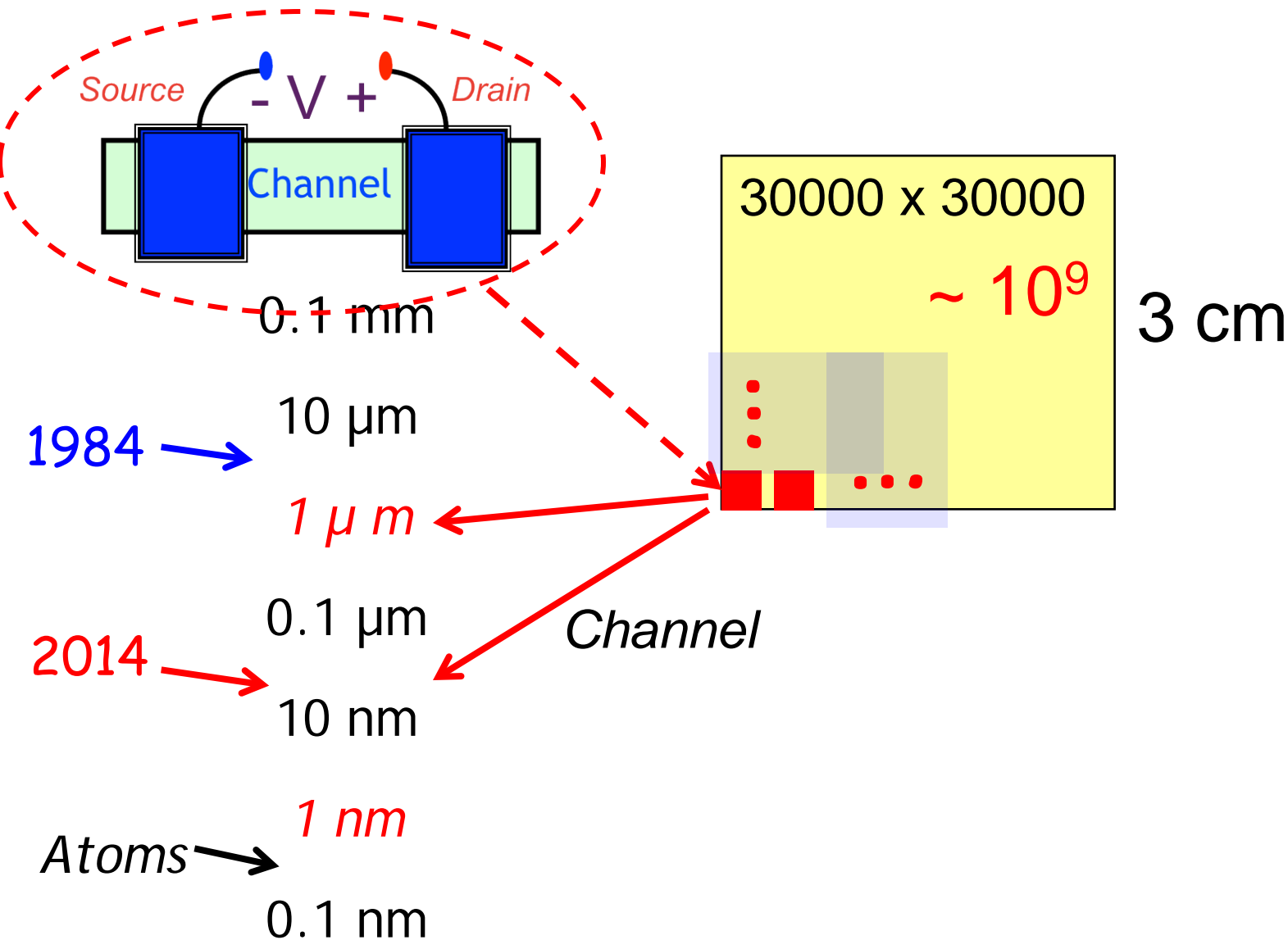
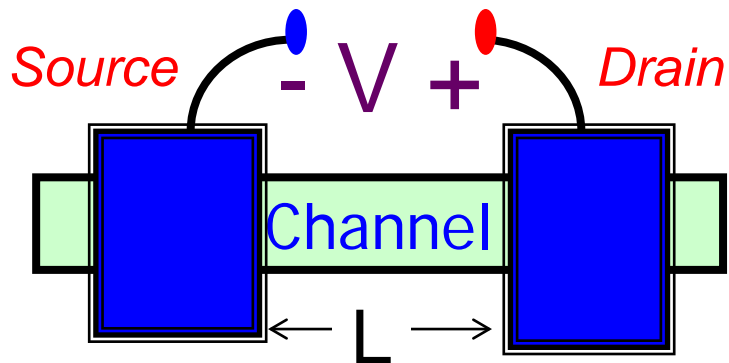


# FUNDAMENTALS OF NANOEELECTRONICS



# New Perspective on Transport



Drude formula:  $\frac{m}{nq^2\tau}$

$$\frac{V}{I} \equiv R = \frac{\rho}{A} L$$

0.1 mm

Diffusive

1984 →

10 μm

1 μm

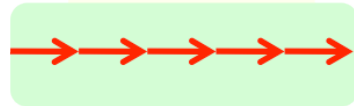


Ballistic

2014 →

0.1 μm

10 nm



Atoms →

1 nm

0.1 nm

$$\frac{h}{q^2} \approx 25 \text{ K}\Omega$$

$q$ : Electronic charge (magnitude)

$h$ : Planck's constant

$\lambda$ : Mean free path

$M$ : Number of "modes"

$$R = \frac{h}{q^2} \frac{1}{M} \left( 1 + \frac{L}{\lambda} \right)$$

Clear ↑

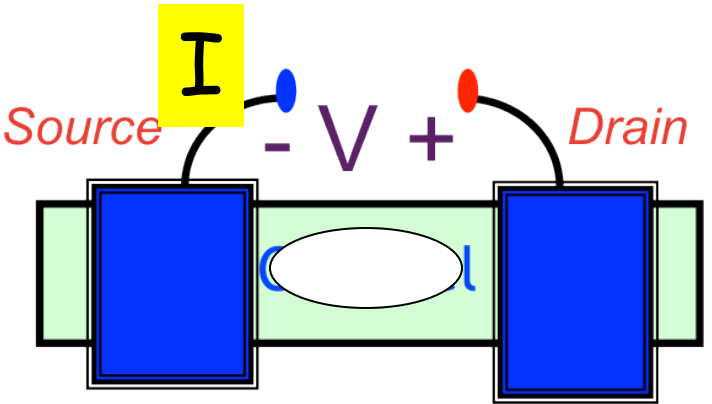
# Where is the Resistance?

1. The new perspective
2. Energy band model

Resistance is associated with

~~➤ Joule Heating:  $I^2 R$~~

➤ Voltage drop:  $IR$

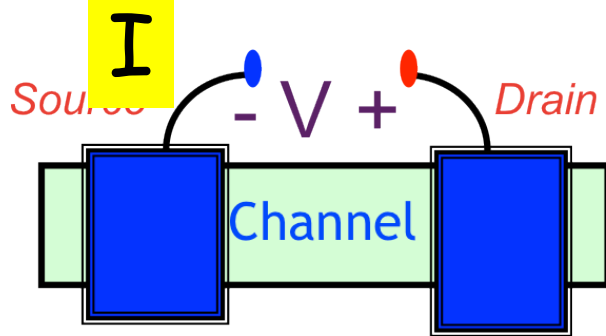


The diagram shows a quantum transport device with two blue electrodes (Source and Drain) connected by a central channel. A voltage  $V$  is applied across the electrodes, and a current  $I$  flows. Below the device, an equivalent circuit is shown with three resistors in series:  $\frac{R_B}{2}$ ,  $R_B$ , and  $\frac{R_B}{2}$ . Red arrows indicate the mapping of these resistors to the total resistance formula  $R = R_B \left(1 + \frac{L}{\lambda}\right)$ . Specifically, the two  $\frac{R_B}{2}$  resistors map to the  $R_B$  term, and the central  $R_B$  resistor maps to the  $R_B \frac{L}{\lambda}$  term.

$$R = R_B \left(1 + \frac{L}{\lambda}\right)$$

*M: Number  
of "modes"*

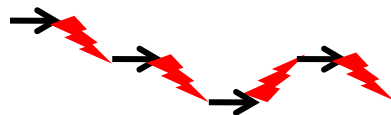
$$R_B = \frac{h}{q^2} \frac{1}{M}$$



$$\frac{R_B}{2} \quad R_B \quad \frac{L}{\lambda} \quad \frac{R_B}{2}$$

*Mechanics:  
Force driven*

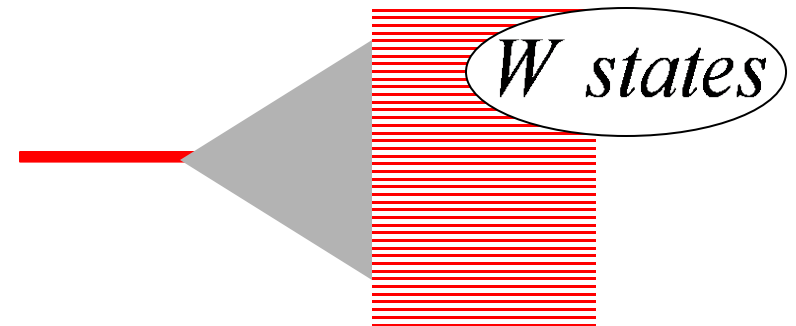
*Thermodynamics:  
Entropy driven*



Usually all mixed up !!

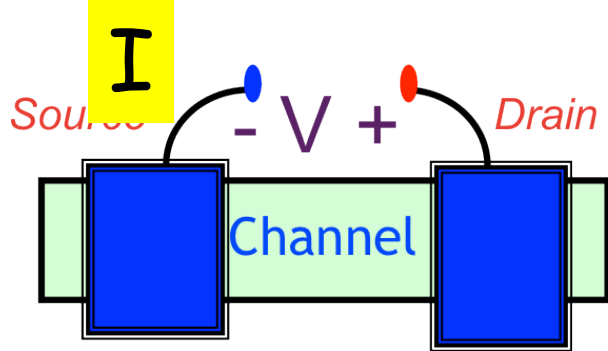
## “Elastic Resistor”

1. The new perspective
2. Energy band model
3. What and where is the voltage?



*Landauer's  
Principle*

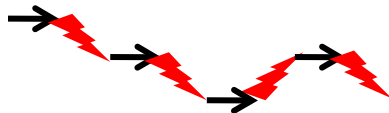
$$S = k \ln W$$



$$\frac{R_B}{2} \quad R_B \quad \frac{L}{\lambda} \quad \frac{R_B}{2}$$

*Mechanics:  
Force driven*

*Thermodynamics:  
Entropy driven*



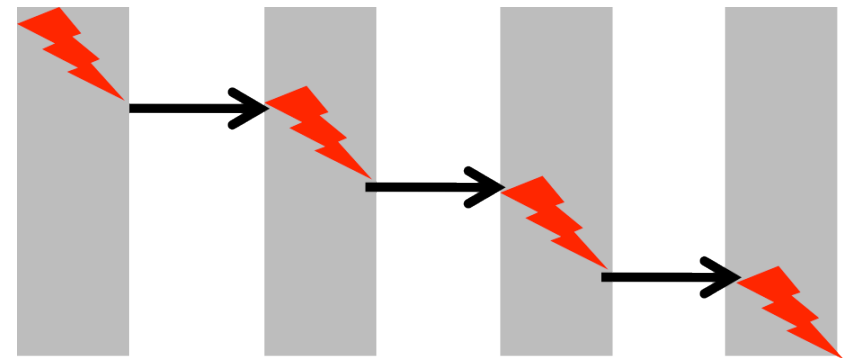
Usually all mixed up !!

## Longer Resistors

➤ *Provides approximate physical picture in general*

➤ *Agrees with rigorous theory for low bias*

### Long Resistors



## Part A: Semiclassical Transport

Newton +  =



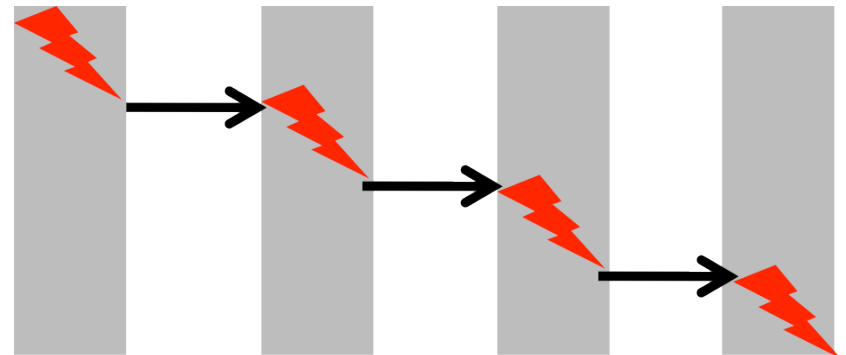
Schrodinger +  = NEGF

## Part B: Quantum Transport

➤ Provides approximate physical picture in general

➤ Agrees with rigorous theory for low bias

*Long Resistors*



# Why Approximate Pictures

## A: Semiclassical

Newton +  =



Schrodinger +  =

## B: Quantum

NEGF

*Usual Physical Picture*

$$J = \sigma F \rightarrow \sigma = \frac{nq^2\tau}{m}$$

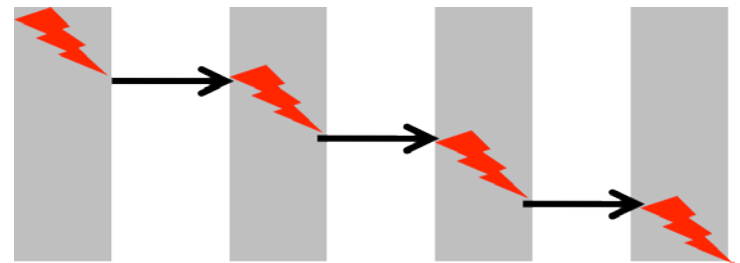
*From Feynman Lectures, 2-1*

“ .. people.. say there is nothing which is not contained in the equations .. if I understand them mathematically, I will understand the physics ..

*Only it doesn't work that way.*

A physical understanding is completely unmathematical, imprecise and inexact .. but absolutely necessary for a physicist. ”

*A Different Physical Picture*



# FUNDAMENTALS OF NANOEELECTRONICS

*Prerequisite: Calculus,  
Elementary Differential Equations  
Part B requires Matrix Algebra*

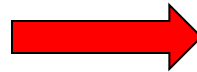
*First offered on nanoHUB-U,  
Spring 2012*

*Text:  
Lessons From Nanoelectronics:  
A New Perspective on  
Transport  
World Scientific (2012)*

*II Edition 2015:  
Manuscript will be available  
to registered students*

## A. Basic Concepts: Semiclassical Model

1. The new perspective
2. Energy band model
3. What and where is the voltage?
4. Heat & electricity:  
Second law & information



From  
Semi-  
classical  
To  
Quantum



## B. Quantum Model

1. Schrodinger Equation
2. Contact-ing Schrodinger
3. NEGF Method
4. Spin Transport