

FUNDAMENTALS OF NANO-ELECTRONICS

Basic Concepts

1. The New Perspective
2. Energy Band Model
3. What and Where

is the Voltage?

**Heat & Electricity:
Second Law & Information**



4.1. Introduction

4.2. Seebeck Coefficient

4.3. Heat Current

4.4. One-level Device

4.5. Second Law

4.6. Entropy

4.7. Law of Equilibrium

4.8. Shannon Entropy

4.9. Fuel Value of Information

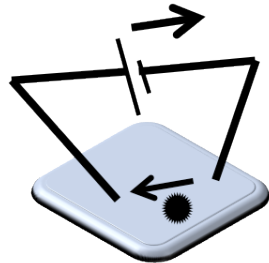
4.10. Summing up ..

$$I \sim G(E) \left(f_1(E) - f_2(E) \right)$$

4.2a Seebeck Coefficient

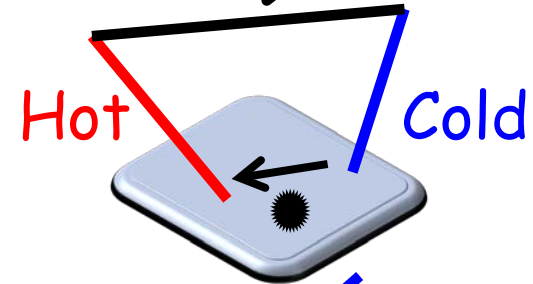
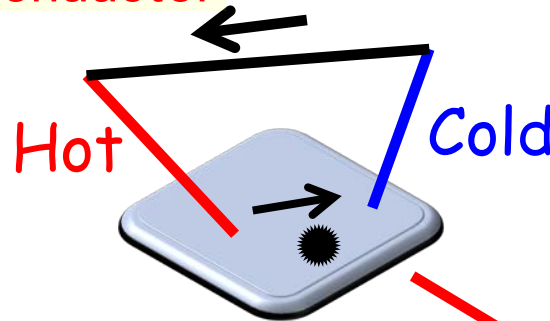
All
conductors

Electron Current

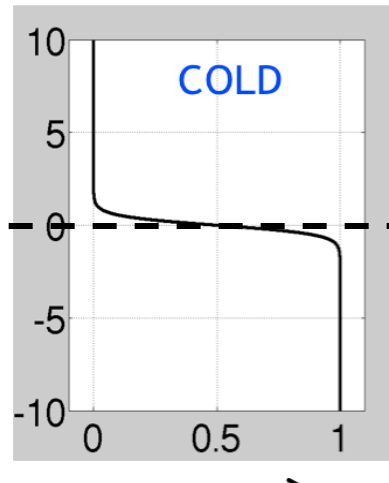
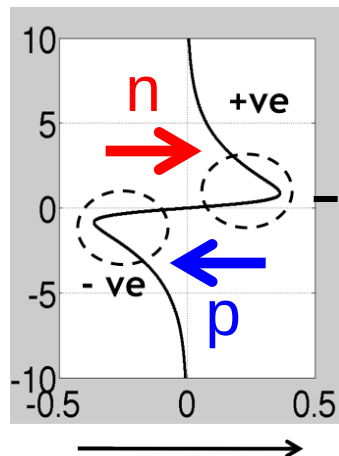
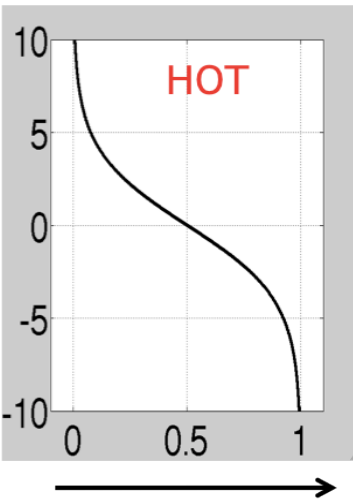


(a) n-type
conductor

(b) p-type
conductor



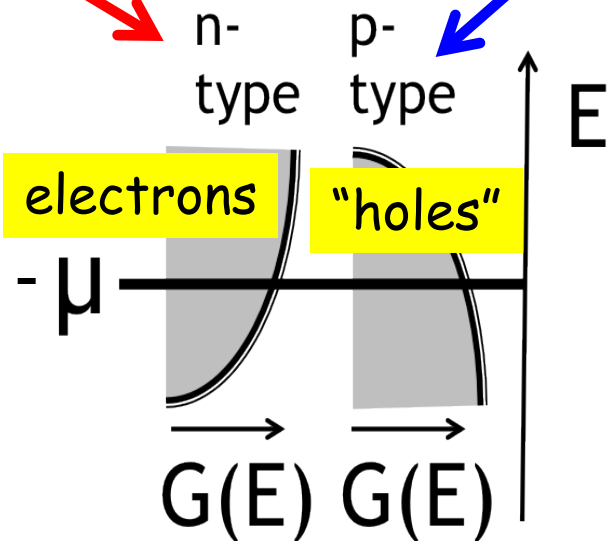
$$\frac{E - \mu}{kT}$$



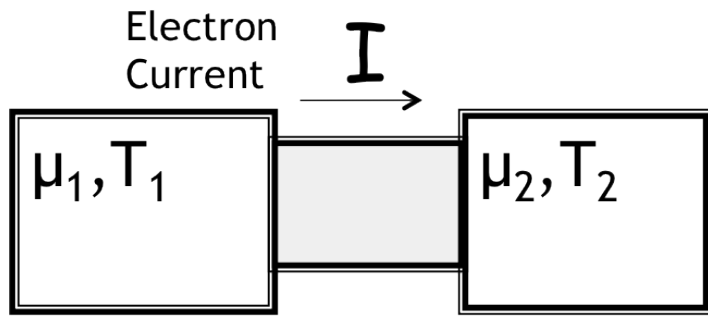
$f_1(E)$

$f_1 - f_2$

$f_2(E)$



4.2b Seebeck coefficient



$$I \sim G(E) (f_1(E) - f_2(E))$$

Fermi function

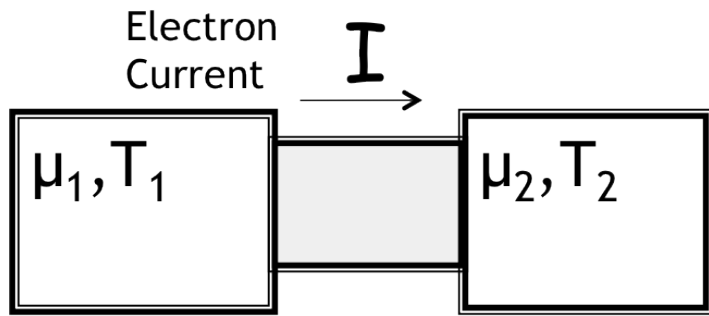
$$f(E, \mu, T) = \frac{1}{1 + e^x} \quad x \equiv \frac{E - \mu}{kT}$$

$$\begin{aligned} \frac{\partial f}{\partial \mu} &= \frac{df}{dx} \frac{\partial x}{\partial \mu} \leftarrow -\frac{1}{kT} \\ \frac{\partial f}{\partial E} &= \frac{df}{dx} \frac{\partial x}{\partial E} \leftarrow +\frac{1}{kT} \\ \frac{\partial f}{\partial T} &= \frac{df}{dx} \frac{\partial x}{\partial T} \leftarrow -\frac{E - \mu}{kT^2} \end{aligned}$$

$$\begin{aligned} &f(E, \mu_1, T_1) - f(E, \mu_2, T_2) \\ &\approx \left(\frac{\partial f}{\partial \mu} \right)_{\mu=\mu_0, T=T_0} (\mu_1 - \mu_2) \\ &\quad + \left(\frac{\partial f}{\partial T} \right)_{\mu=\mu_0, T=T_0} (T_1 - T_2) \\ &= \left(-\frac{\partial f_0}{\partial E} \right) \times \left(\Delta \mu + \frac{E - \mu_0}{T_0} \Delta T \right) \end{aligned}$$



4.2c Seebeck coefficient



Fermi function

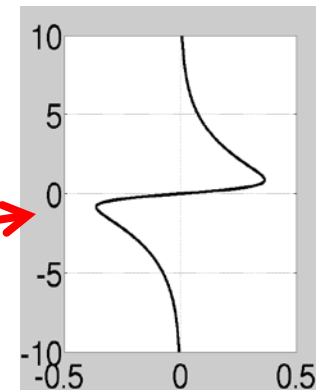
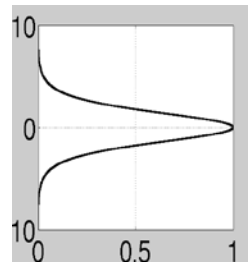
$$f(E, \mu, T) = \frac{1}{1 + e^x} \quad x \equiv \frac{E - \mu}{kT}$$

$$I = \frac{1}{q} \int_{-\infty}^{+\infty} dE G(E) (f_1(E) - f_2(E))$$

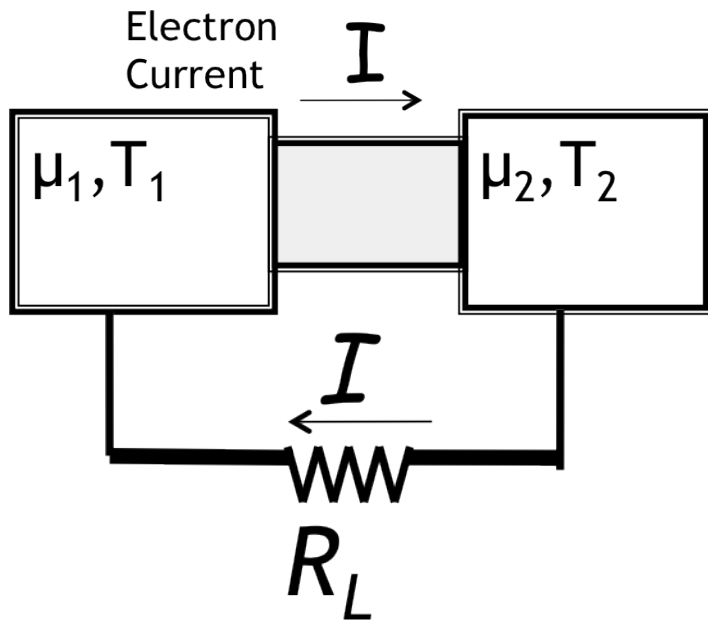
$$I \approx G_0 \Delta V + G_S \Delta T \quad \left| \quad = \left(-\frac{\partial f_0}{\partial E} \right) \times \left(\Delta \mu + \frac{E - \mu_0}{T_0} \Delta T \right) \right.$$

$$G = \int_{-\infty}^{+\infty} dE \left(-\frac{\partial f_0}{\partial E} \right) G(E)$$

$$G_S = \int_{-\infty}^{+\infty} dE \left(-\frac{\partial f_0}{\partial E} \right) \frac{E - \mu_0}{qT_0} G(E)$$



4.2d Seebeck coefficient



(Temperature Difference)

Heat → Electricity

Electricity → Temperature Difference

$$I \approx G_0 \Delta V + G_S \Delta T \quad I = 0$$

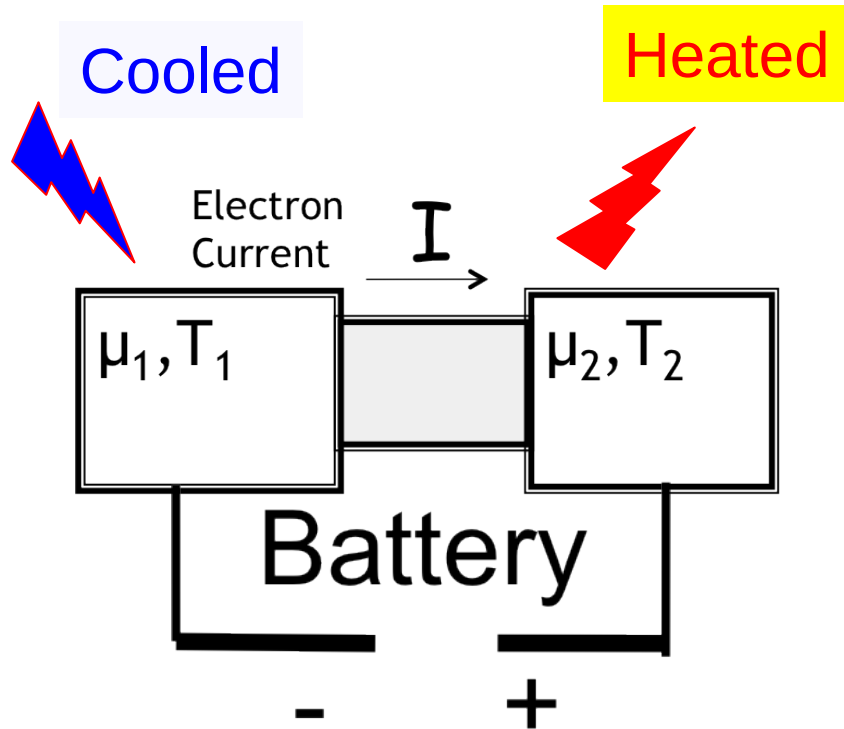
$$G_0 = \int_{-\infty}^{+\infty} dE \left(-\frac{\partial f_0}{\partial E} \right) G(E)$$

$$G_S = \int_{-\infty}^{+\infty} dE \left(-\frac{\partial f_0}{\partial E} \right) \frac{E - \mu_0}{qT_0} G(E)$$

$$S \equiv \frac{\Delta V}{\Delta T} \approx -\frac{G_S}{G_0}$$

Open circuit voltage
Temperature difference

Coming up next ..



Electricity $\rightarrow$ Temperature Difference

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