

FUNDAMENTALS OF NANO ELECTRONICS

Basic Concepts

The New Perspective



2. Energy Band Model

3. What and Where

is the Voltage?

4. Heat & Electricity:

Second Law & Information

1.1. Introduction

1.2. Two Key Concepts

1.3. Why Electrons Flow

1.4. Conductance Formula

1.5. Ballistic(B) Conductance

1.6. Diffusive(D) Conductance

1.7. Connecting B to D

1.8. Angular Averaging

1.9. Drude Formula

1.10. Summing up ..

1.1a Introduction

Drude
formula

τ : mean free time

m : effective mass

n : "free" electrons

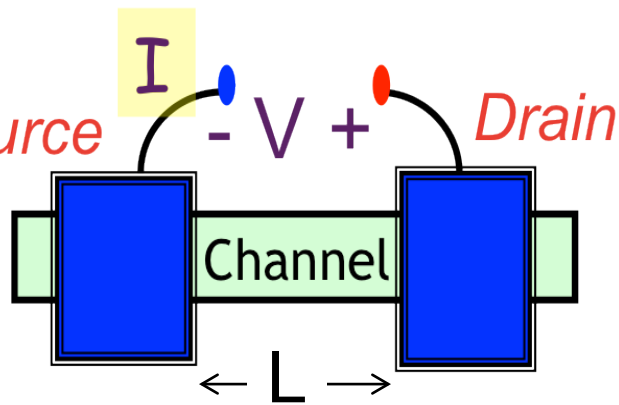
$$\sigma = \frac{q^2 n \tau}{m}$$

$$G \equiv \frac{1}{R} = \frac{\sigma A}{L} \leftarrow R \equiv \frac{V}{I}$$

$$\sigma A = G_B \lambda$$

$$G = \underbrace{\frac{q^2}{h} M}_{G_B} \times \frac{\lambda}{L + \lambda}$$

Mean free path



0.1 mm

Diffusive



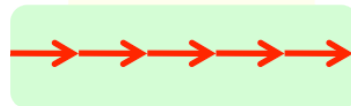
10 μm

1 μm

0.1 μm

10 nm

Ballistic



1 nm

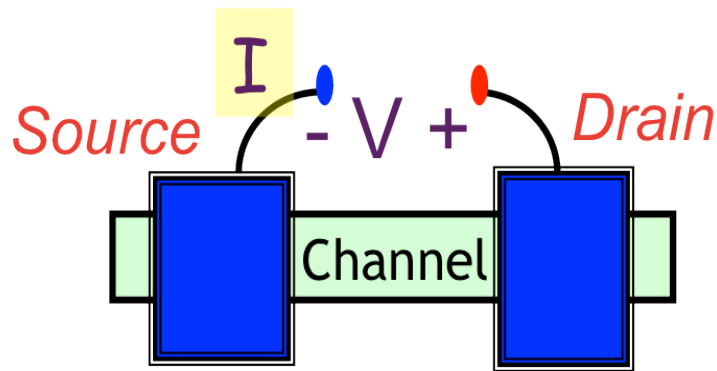
0.1 nm

Atoms

1984

2014

1.1b Introduction



Drude
formula

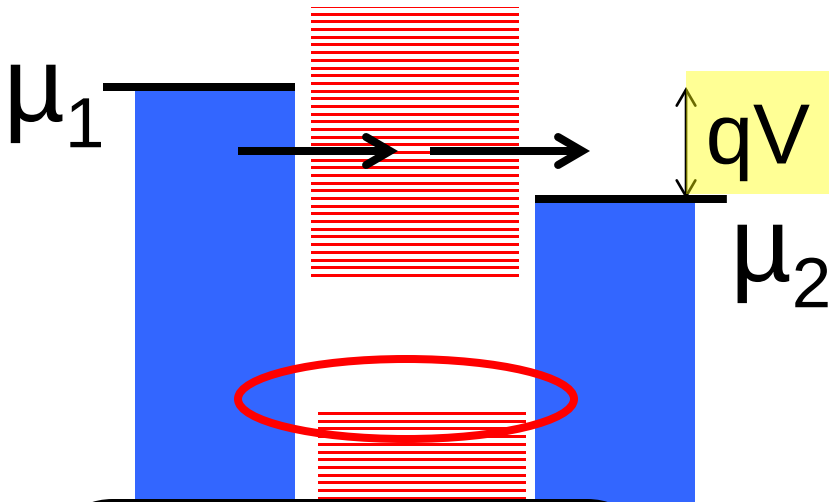
$$\sigma = \frac{q^2 n \tau}{m}$$

$$m \frac{dv_d}{dt} = qF - \frac{mv_d}{\tau}$$

$$\rightarrow v_d = \left(\frac{q\tau}{m} \right) F$$

mobility

$$I = Aqn v_d = A \frac{q^2 n \tau}{m} F$$



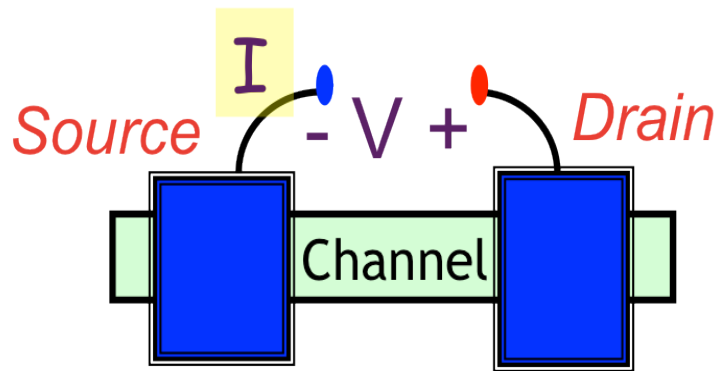
$$G = \frac{q^2 D}{2t}$$

D: Density of states
t : transfer time

“ Filled bands
do not conduct ”

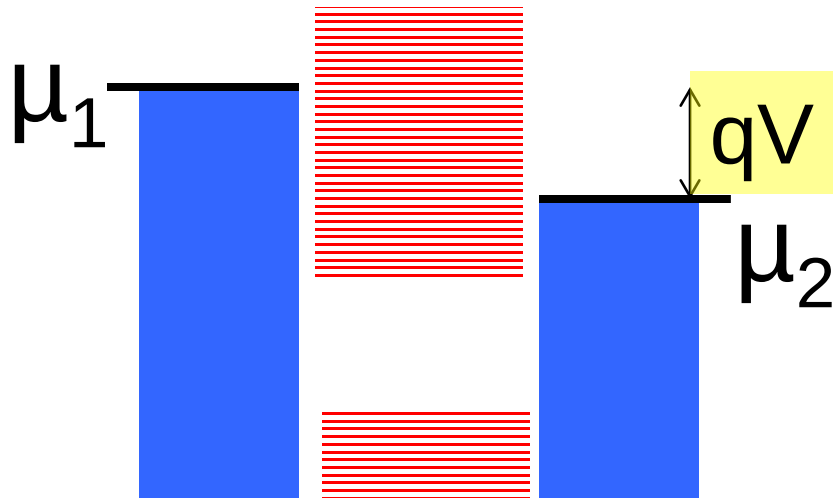
n: “free” electrons

1.1c Introduction



*Drude
formula*

$$\sigma = \frac{q^2 n \tau}{m}$$



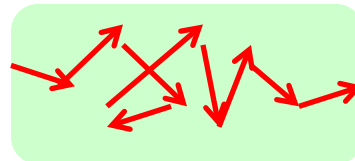
$$G = \frac{q^2 D}{2t} \rightarrow \frac{q^2}{h} M$$

D: Density of states
t : transfer time

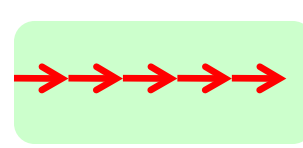
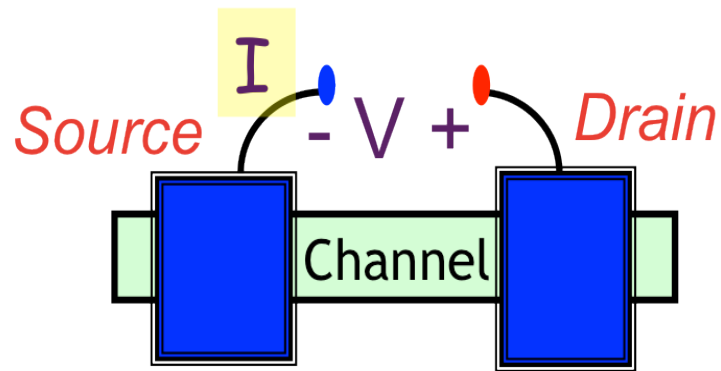
*More general result
usually obtained from
advanced formalisms*

$$\sigma = q^2 \frac{D}{A L} \bar{D}$$

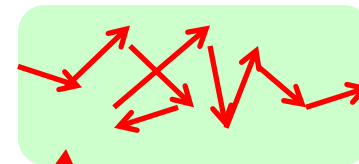
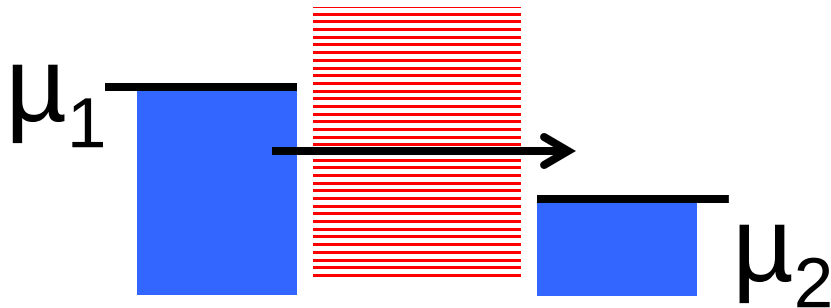
Diffusive



$$t = \frac{L^2}{2\bar{D}}$$



Elastic

NOT
BallisticLong
ResistorsMechanics:
Force drivenThermodynamics:
Entropy driven

➤ Results agree exactly
with BTE for low bias

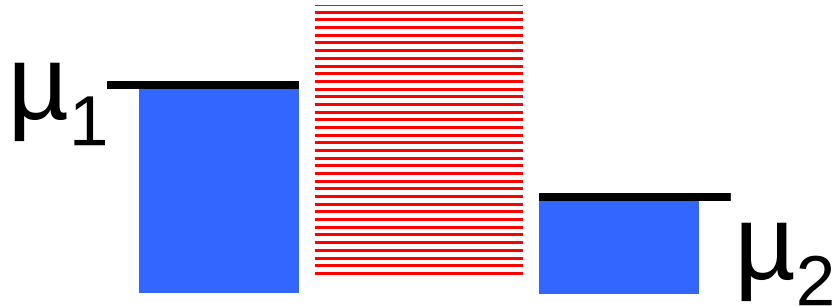
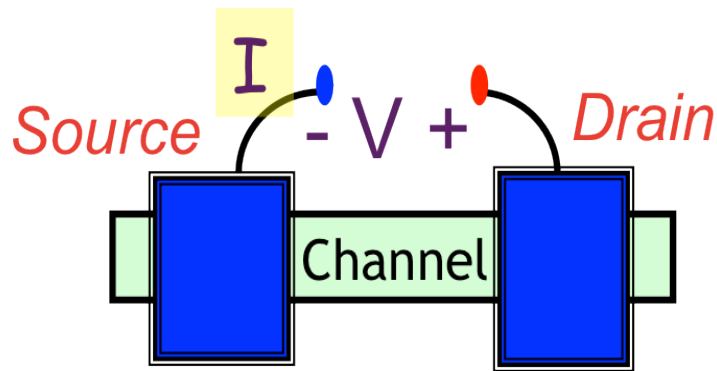
Newton +  =

BTE



Elastic or Landauer Resistor

Coming up next ..



1. *Density of States*

2. *Fermi function* $f(E) = \frac{1}{1 + e^{(E-\mu)/kT}}$

- 1.1. Introduction
- 1.2. Two Key Concepts
- 1.3. Why Electrons Flow
- 1.4. Conductance Formula
- 1.5. Ballistic(B) Conductance
- 1.6. Diffusive(D) Conductance
- 1.7. Connecting B to D
- 1.8. Angular Averaging
- 1.9. Drude Formula
- 1.10. Summing up ..